

Giant Resonance Studies

Perspectives

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□ Introduction

Giant resonances: Fundamental modes of nuclear excitation

□ Importance of studying compression modes in nuclei

ISGMR and ISGDR excitation

□ Experimental studies

Incompressibility of nuclear matter

Asymmetry term

□ Conclusions and outlook

In the following:

IS = Iso-Scalar

IV = Iso-Vector

S = Spin

G = Giant

M = Monopole

D = Dipole

Q = Quadrupole

O = Octupole

E.g. ISGMR = Isoscalar giant monopole resonance

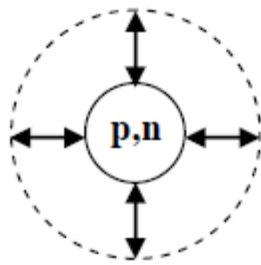
ISGDR = Isoscalar giant dipole resonance

IVGDR = Isovector giant dipole resonance

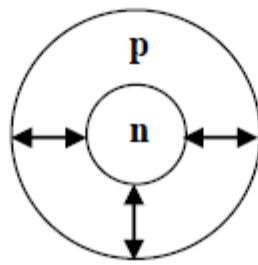
IVSGMR = Isovector spin giant monopole resonance

IVSGDR = Isovector spin giant dipole resonance

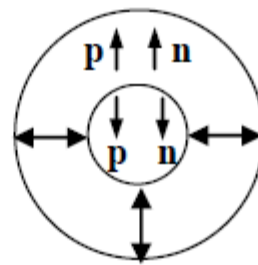
$\Delta L = 0$



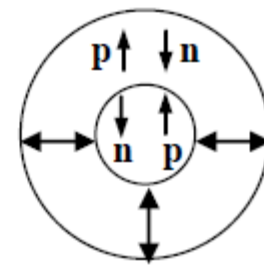
ISGMR



IVGMR



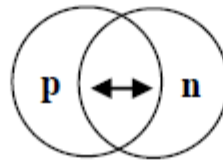
ISSGMR



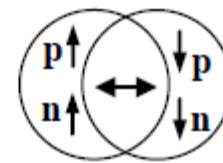
IVSGMR

$\Delta L = 1$

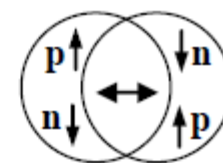
ISGDR
??



IVGDR

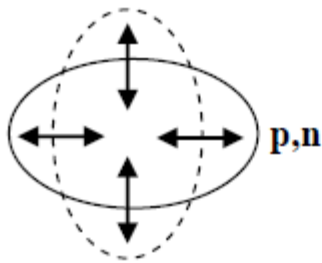


ISSGDR



IVSGDR

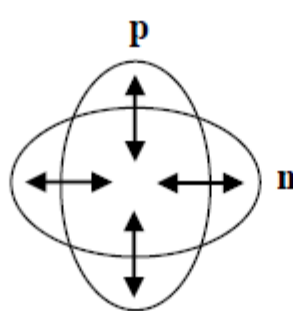
$\Delta L = 2$



ISGQR

$\Delta T = 0$

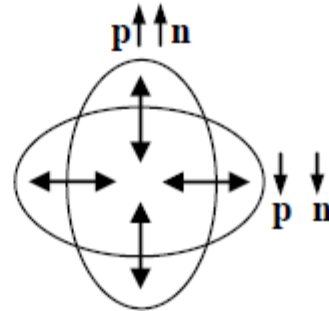
$\Delta S = 0$



IVGQR

$\Delta T = 1$

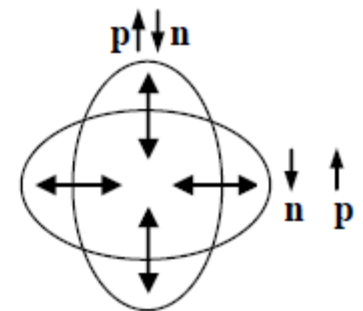
$\Delta S = 0$



ISSGQR

$\Delta T = 0$

$\Delta S = 1$



IVSGQR

$\Delta T = 1$

$\Delta S = 1$

Microscopic picture: GRs are coherent (1p-1h) excitations induced by single-particle operators.

- **Excitation energy depends on**
 - i) multipole L ($L\hbar\omega$, since radial operator $\propto r^L$; **except for ISGMR and ISGDR, $2\hbar\omega$ & $3\hbar\omega$, respectively),***
 - ii) strength of effective interaction and*
 - iii) collectivity.*
- **Exhaust appreciable % of EWSR**
- **Acquire a width due to coupling to continuum and to underlying 2p-2h configurations.**

Microscopic structure of ISGMR & ISGDR

Transition operators:

$$O^{L=0} = \cancel{\sum_i r_i^0 Y_0^0} + \frac{1}{2} \sum_i r_i^2 Y_0^0 + \dots$$

Constant **Overtone**

2ħω excitation

$$O^{L=1} = \cancel{\sum_i r_i^1 Y_0^1} + \frac{1}{2} \sum_i r_i^3 Y_0^1 + \dots$$

Spurious **Overtone**
c.o.m. motion

3ħω excitation (overtone of c.o.m. motion)

Nucleus \longrightarrow **Many-body system with a finite size**

Vibrations \longrightarrow **Multipole expansion with r, Y_{lm}, τ, σ**

$\Delta S=0, \Delta T=0$ $\Delta S=0, \Delta T=1$ $\Delta S=0, \Delta T=1$ $\Delta S=1, \Delta T=1$ $\Delta S=1, \Delta T=1$

L=0: Monopole	ISGMR $r^2 Y_0$	IAS τY_0	IVGMR $\tau r^2 Y_0$	GTR $\tau \sigma Y_0$	IVSGMR $\tau \sigma r^2 Y_0$
L=1: Dipole	ISGDR $r^3 Y_1$		IVGDR $\tau r Y_1$		IVSGDR $\tau \sigma r Y_1$
L=2: Quadrupole	ISGQR $r^2 Y_2$		IVGQR $\tau r^2 Y_2$		IVSGQR $\tau \sigma r^2 Y_2$
L=3: Octupole	LEOR, HEOR $r^3 Y_3$				



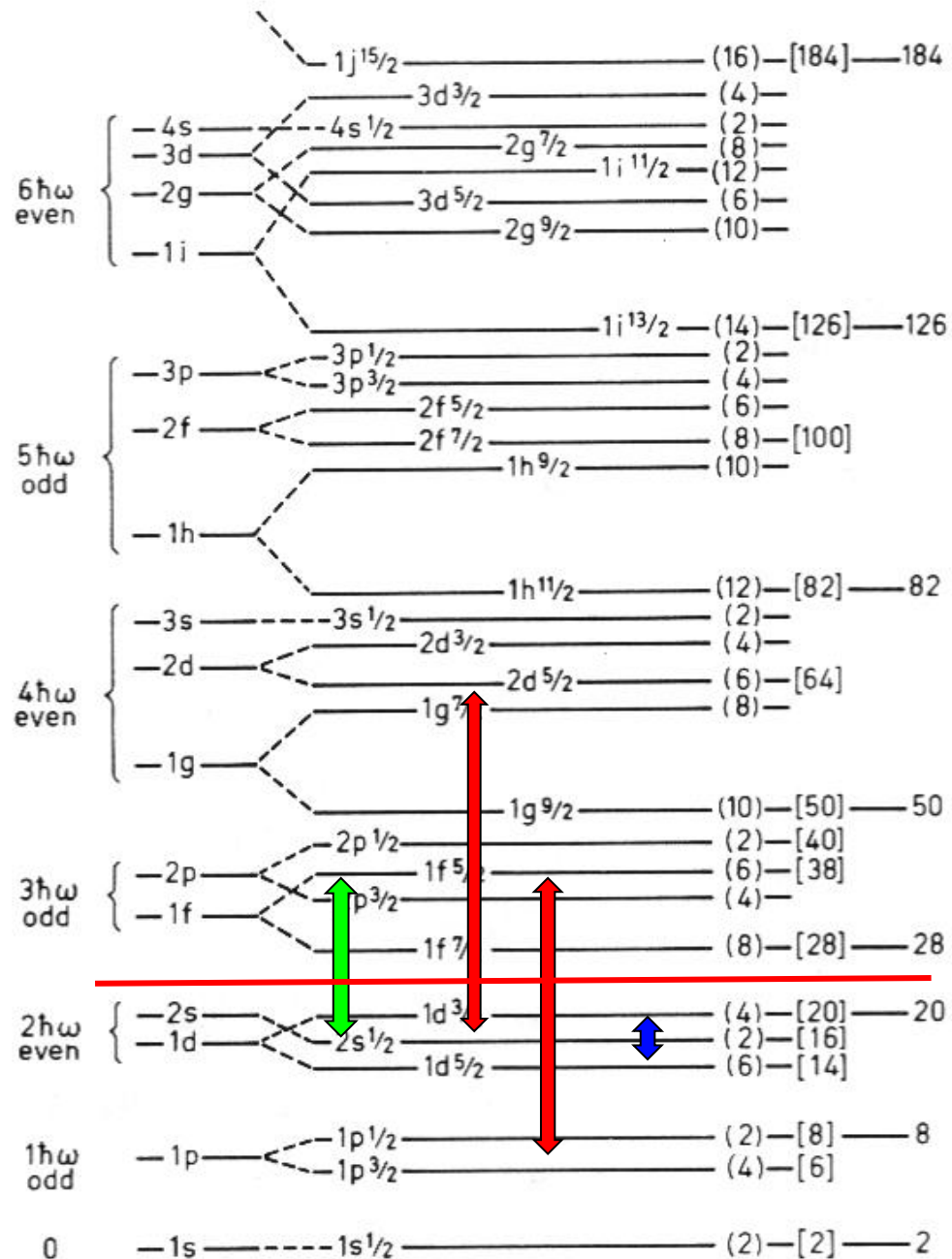
$\Delta N = 1$ E1 (IVGDR)



$\Delta N = 2$ E2 (ISGQR)



$\Delta N = 0$ E0 (ISGMR)



Decay of giant resonances

- Width of resonance

$\Gamma, \Gamma^\uparrow, \Gamma^\downarrow$ ($\Gamma^\downarrow^\uparrow, \Gamma^\downarrow^\downarrow$)

- Γ^\uparrow : direct or escape width

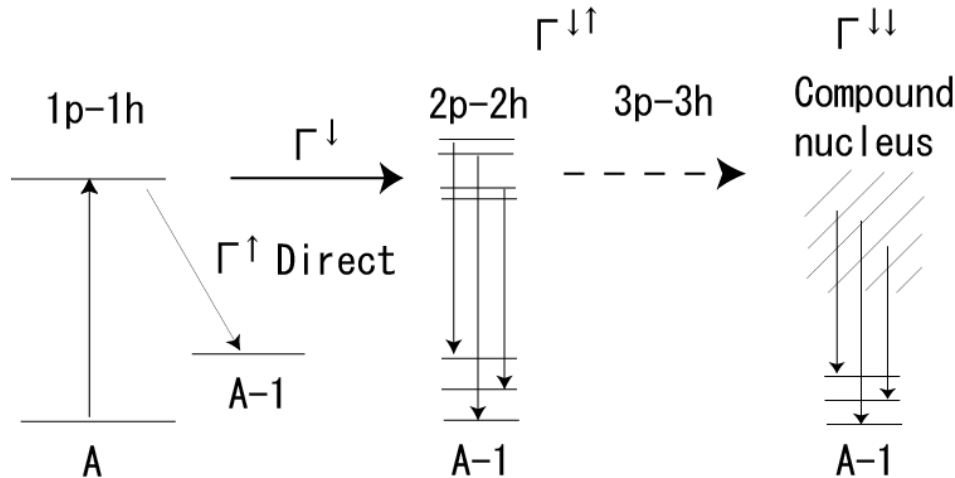
- Γ^\downarrow : spreading width

$\Gamma^\downarrow^\uparrow$: pre-equilibrium, $\Gamma^\downarrow^\downarrow$: compound

- Decay measurements

⇒ Direct reflection of damping processes

Allows detailed comparison with theoretical calculations



The collective response of the nucleus

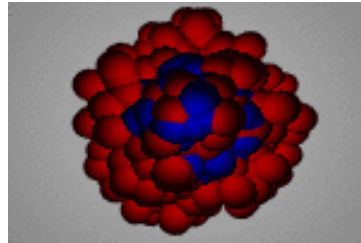
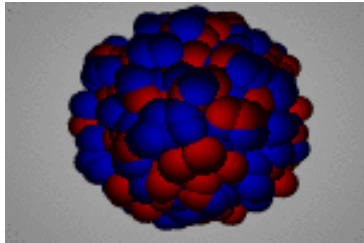
Giant Resonances

Electric giant resonances

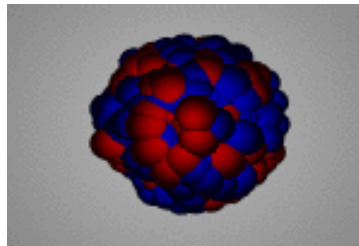
Isoscalar

Isovector

Monopole
(GMR)



Dipole
(GDR)



Quadrupole
(GQR)

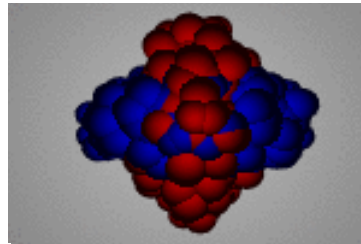
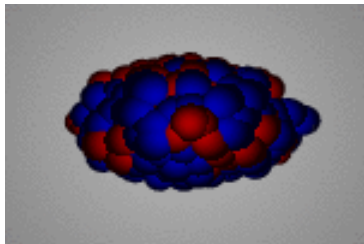
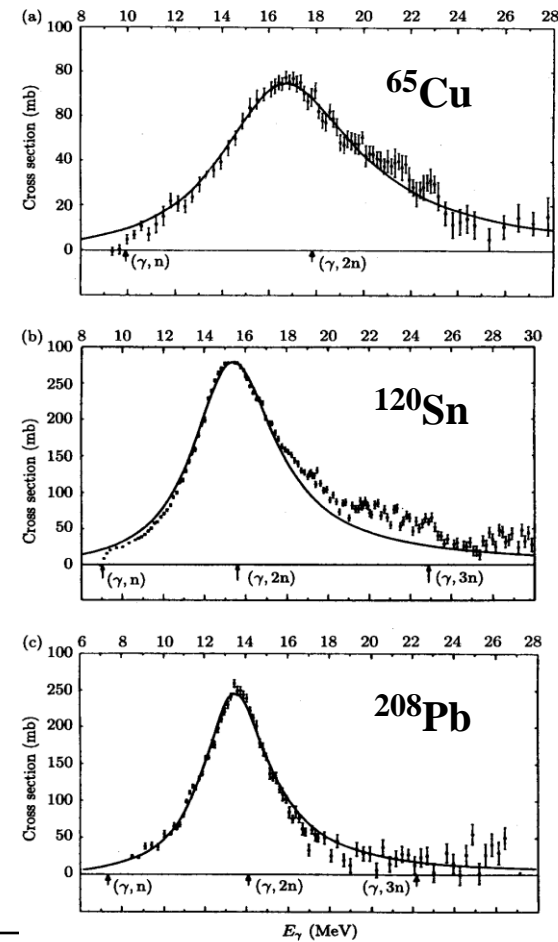


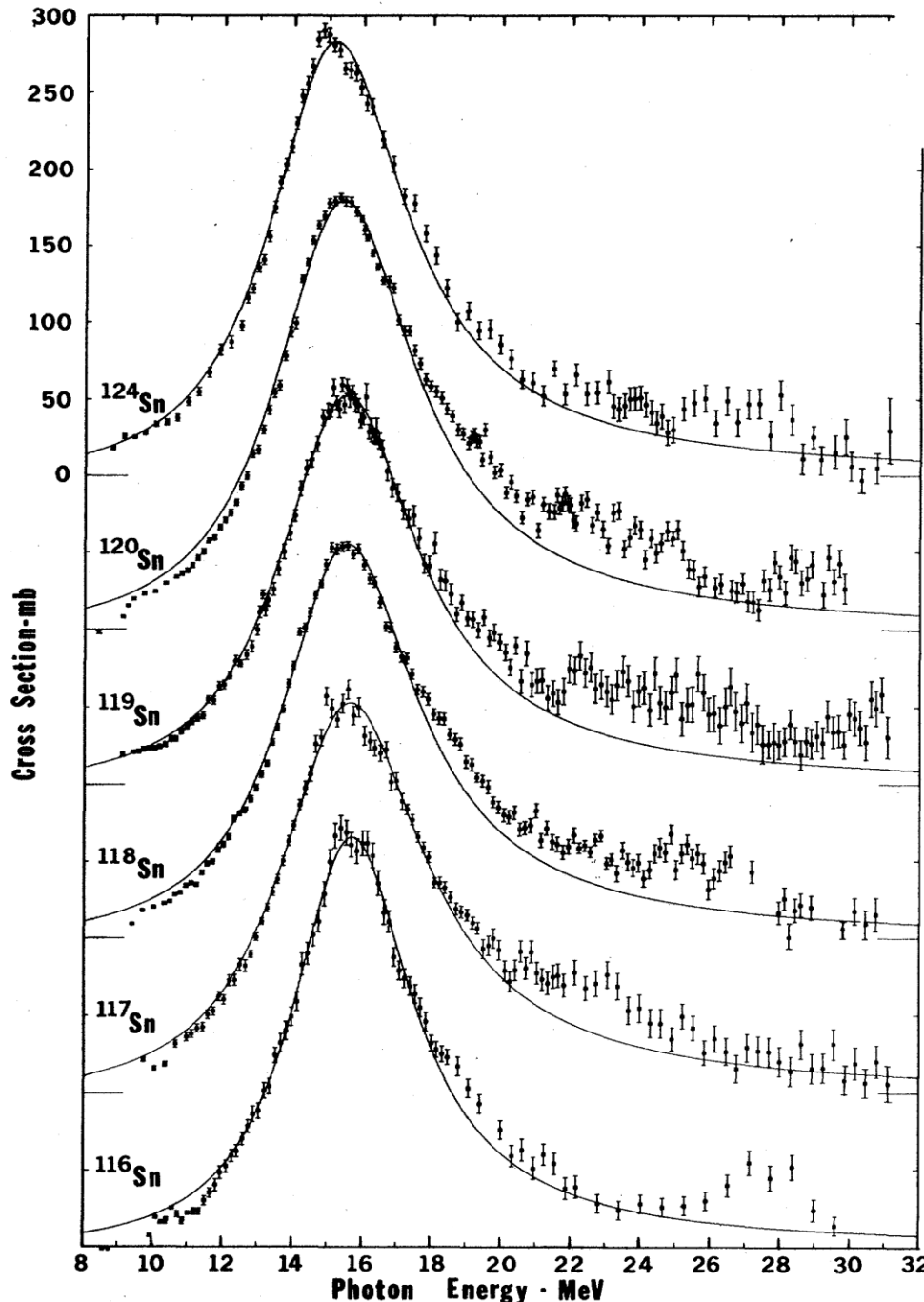
Photo-neutron
cross sections



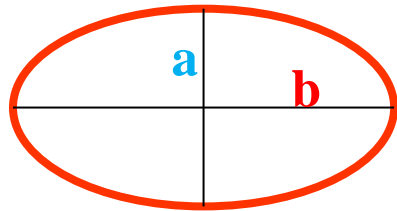
Berman and Fulz, Rev. Mod. Phys. 47 (1975) 47

Measurement of the giant dipole resonance with mono-energetic photons

B.L. Berman and S.C. Fultz
Rev. Mod. Phys. 47 (1975) 713



Nucleus	Centroid (MeV)	Width (MeV)
^{116}Sn	15.68	4.19
^{117}Sn	15.66	5.02
^{118}Sn	15.59	4.77
^{119}Sn	15.53	4.81
^{120}Sn	15.40	4.89
^{124}Sn	15.19	4.81

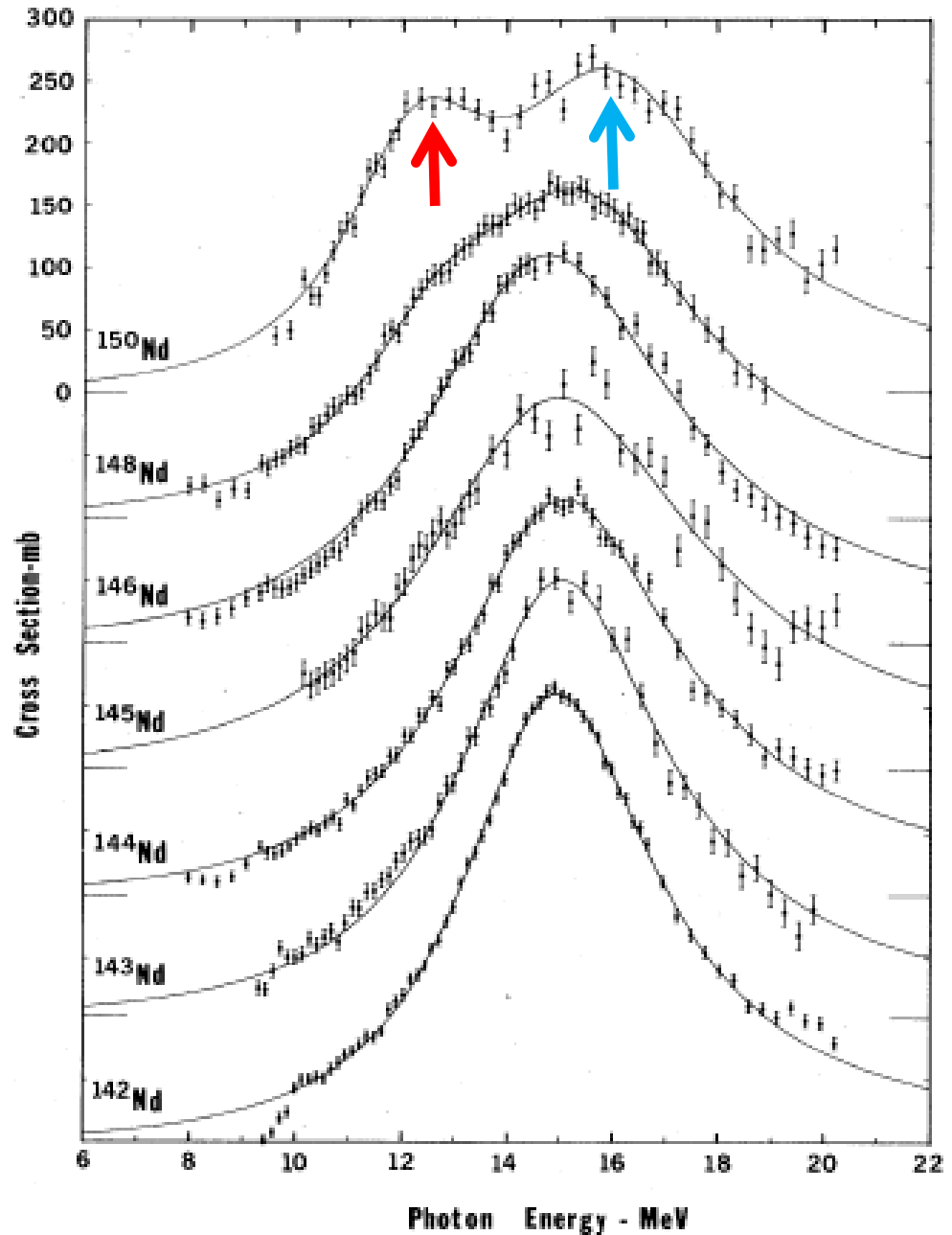
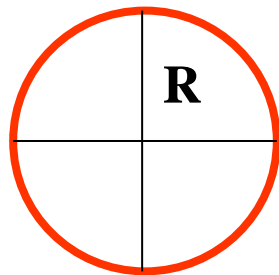


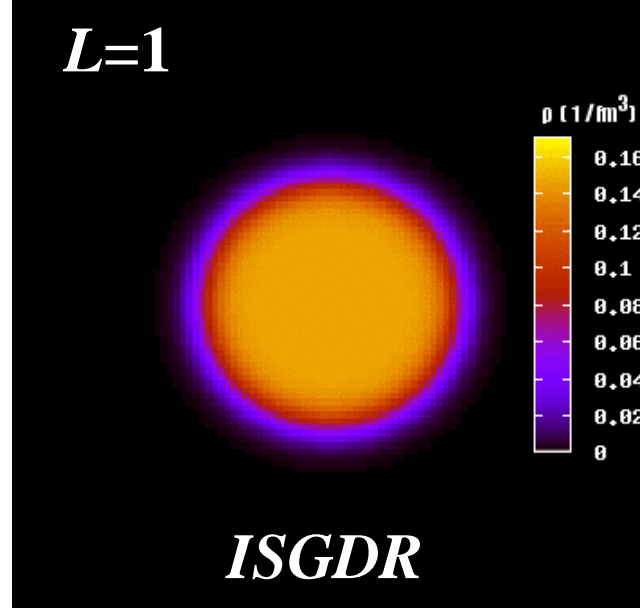
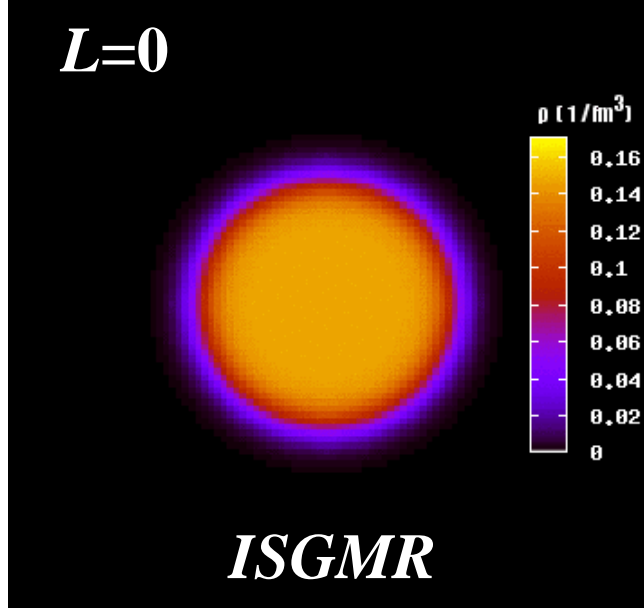
Quadrupole deformation:
 $\beta_2 = 0.275$

Excitation energies:
 $E_2/E_1 = 0.911\eta + 0.089$

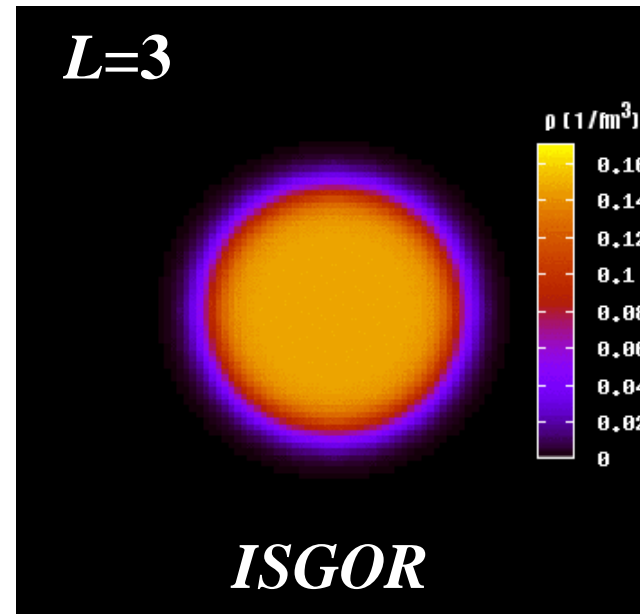
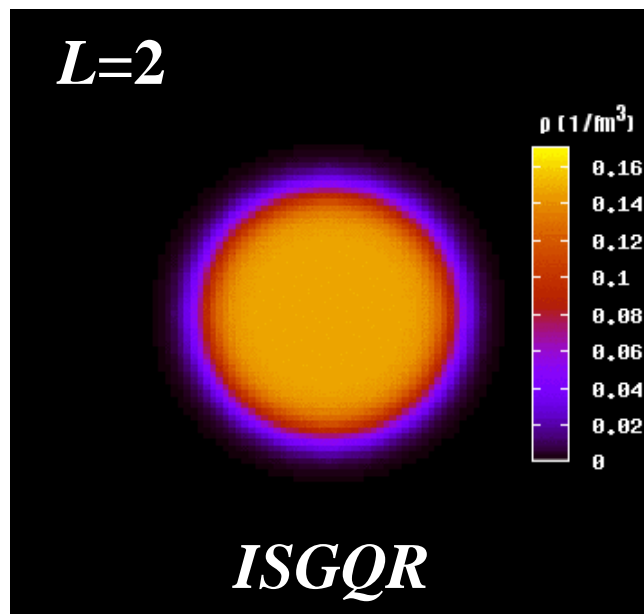
Where $\eta = b/a$

$s_1/s_2 = 1/2$





M. Itoh



In fluid mechanics, **compressibility** is a measure of the relative volume change of a fluid as a response to a pressure change.

$$\beta = - \frac{1}{V} \frac{\partial V}{\partial P}$$

where P is pressure, V is volume.

Incompressibility or **bulk modulus** (K) is a measure of a substance's resistance to uniform compression and can be formally defined:

$$K = - V \frac{\partial P}{\partial V}$$

For the equation of state of symmetric nuclear matter at saturation nuclear density:

$$\left[\frac{d(E/A)}{d\rho} \right]_{\rho = \rho_0} = 0$$

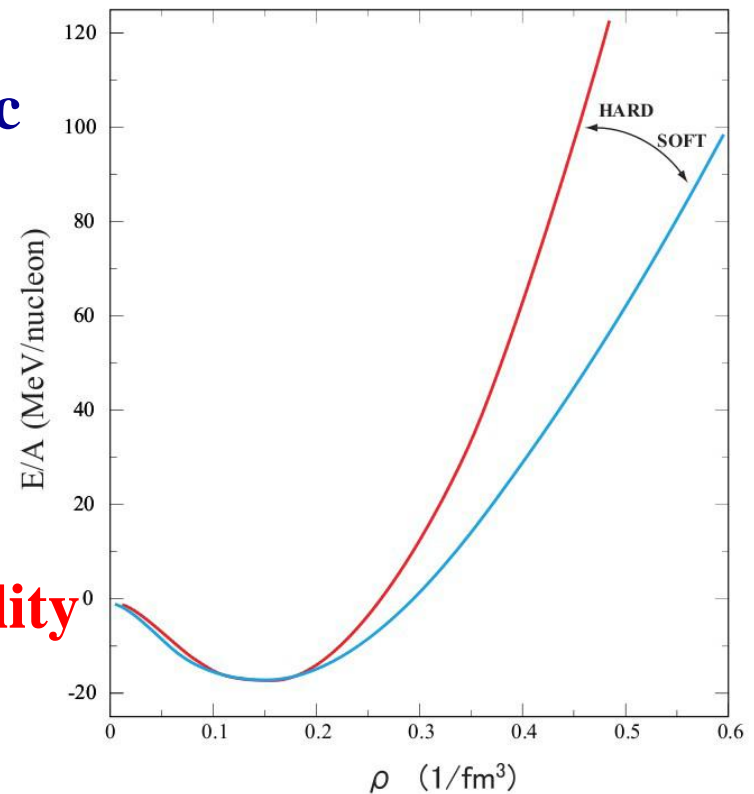
and one can derive the incompressibility of nuclear matter:

$$K_{nm} = \left[9\rho^2 \frac{d^2(E/A)}{d\rho^2} \right]_{\rho = \rho_0}$$

E/A : binding energy per nucleon

ρ : nuclear density

ρ_0 : nuclear density at saturation



J.P. Blaizot, Phys. Rep. 64 (1980) 171

Equation of state (EOS) of nuclear matter:

More complex than for infinite neutral liquids:

Neutrons and protons with different interactions

Coulomb interaction of protons

- 1. Governs the collapse and explosion of giant stars (supernovae)**
- 2. Governs formation of neutron stars (mass, radius, crust)**
- 3. Governs collisions of heavy ions.**
- 4. Important ingredient in the study of nuclear properties.**

Isoscalar Excitation Modes of Nuclei

Hydrodynamic models/Giant Resonances

Coherent vibrations of nucleonic fluids in a nucleus.

Compression modes : **ISGMR, ISGDR**

In Constrained and Scaling Models:

$$E_{ISGMR} = \hbar \sqrt{\frac{K_A}{m \langle r^2 \rangle}}$$

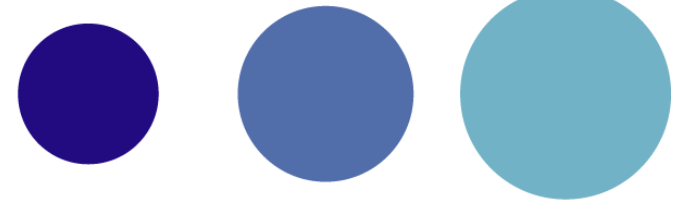
$$E_{ISGDR} = \hbar \sqrt{\frac{7}{3} \frac{K_A + \frac{27}{25} \varepsilon_F}{m \langle r^2 \rangle}}$$

ε_F is the Fermi energy and the nucleus incompressibility:

$$\rightarrow K_A = \left[r^2 \left(\frac{d^2(E/A)}{dr^2} \right) \right]_{r=R_0}$$

J.P. Blaizot, Phys. Rep. 64 (1980) 171

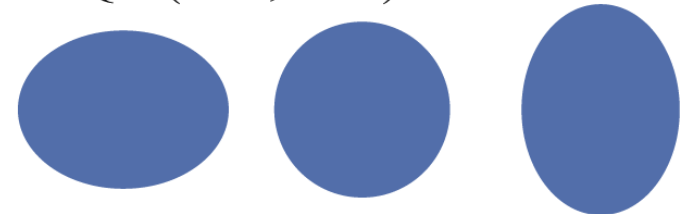
ISGMR (T=0, L=0)



ISGDR (T=0, L=1)



ISGQR (T=0, L=2)

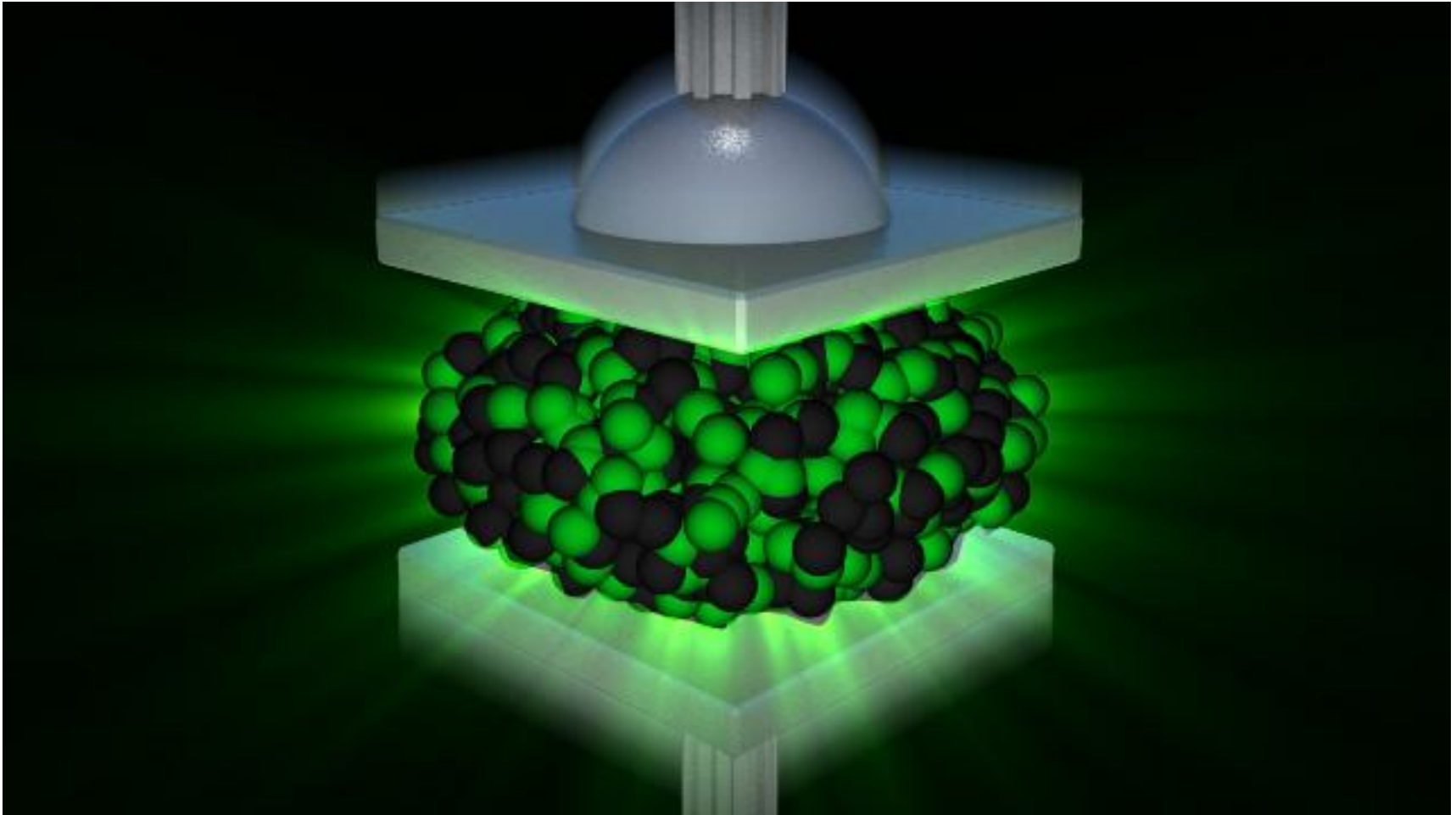


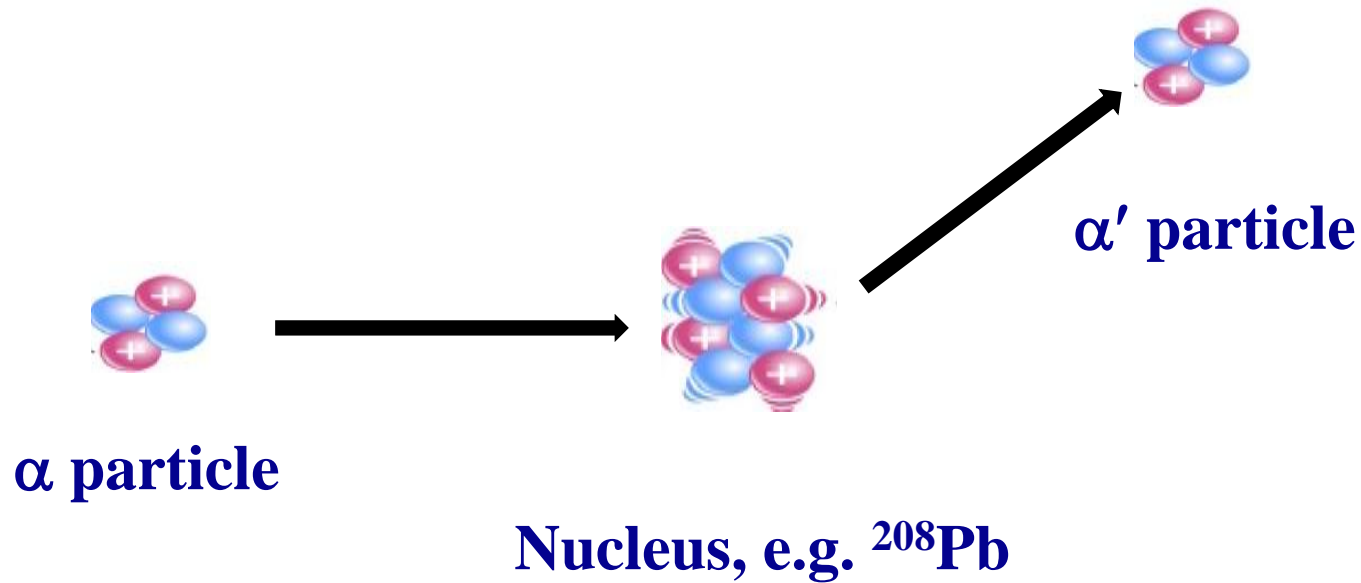
Giant resonances

- **Macroscopic properties: E_x , Γ , %EWSR**
- **Isoscalar giant resonances; compression modes**

ISGMR, ISGDR \Rightarrow Incompressibility, symmetry energy

$$K_A = K_{vol} + K_{surf}A^{-1/3} + K_{sym}((N-Z)/A)^2 + K_{Coul}Z^2A^{-4/3}$$

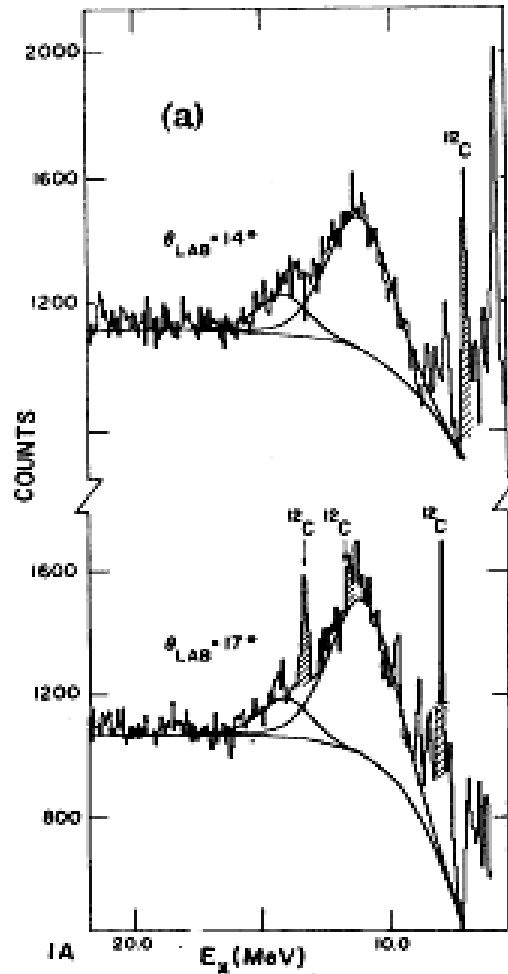




Inelastic α scattering

ISGQR, ISGMR

KVI (1977)



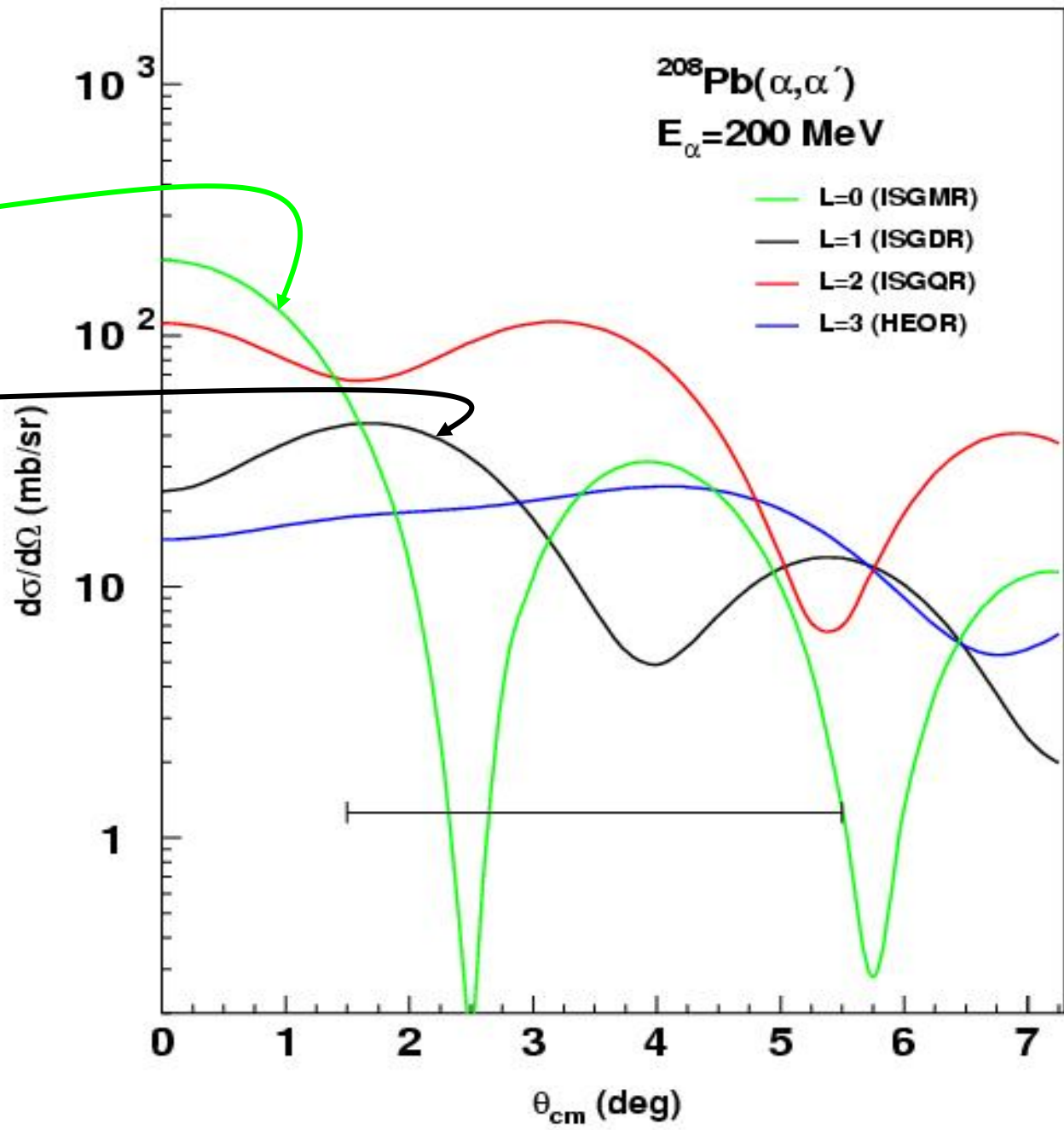
Large instrumental background!

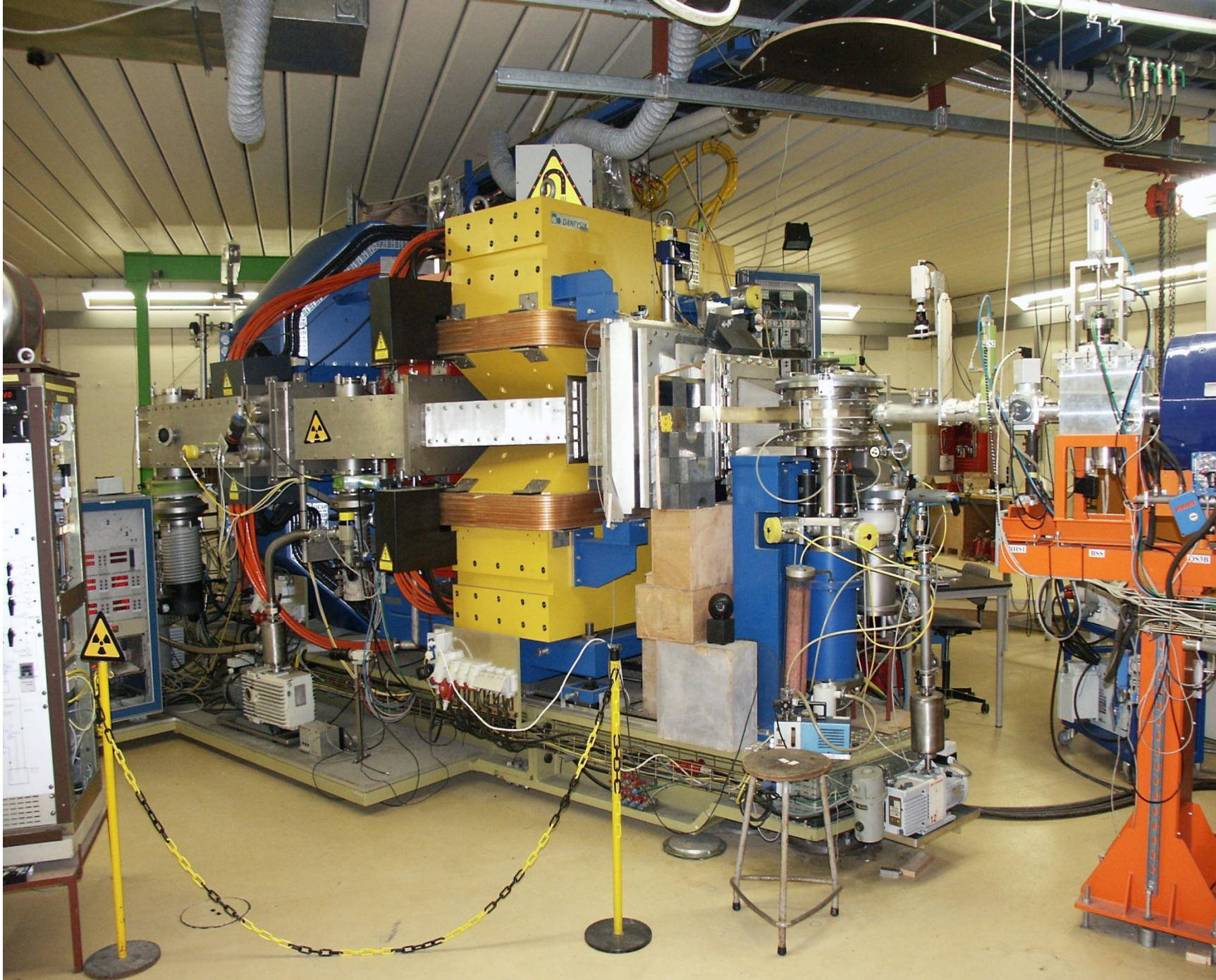
← $^{208}\text{Pb}(\alpha, \alpha')$ at $E_\alpha = 120$ MeV

M. N. Harakeh *et al.*, Phys. Rev. Lett. 38, 676 (1977)

ISGMR $L = 0$

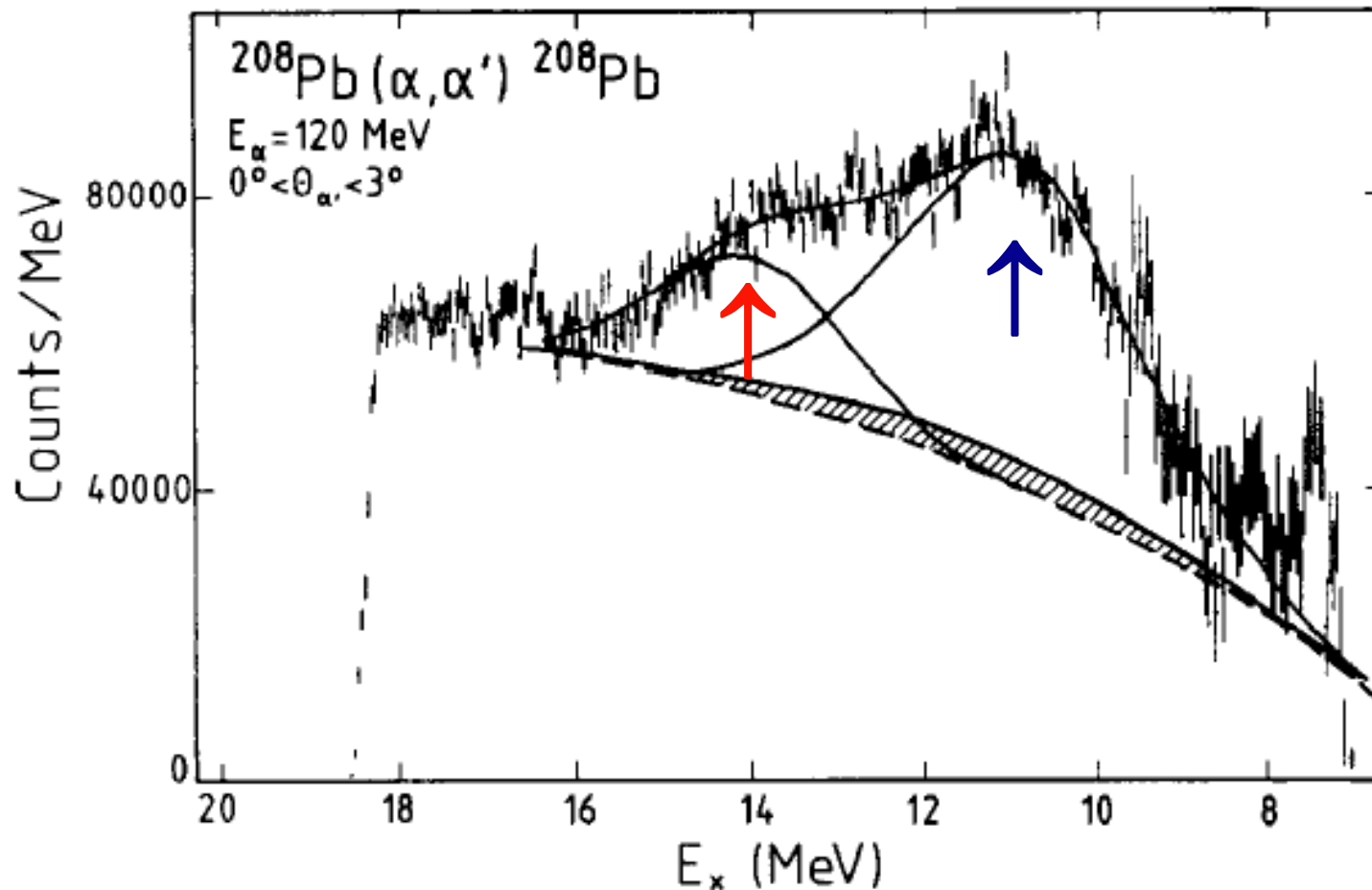
ISGDR $L = 1$





ISGQR at 10.9 MeV

ISGMR at 13.9 MeV



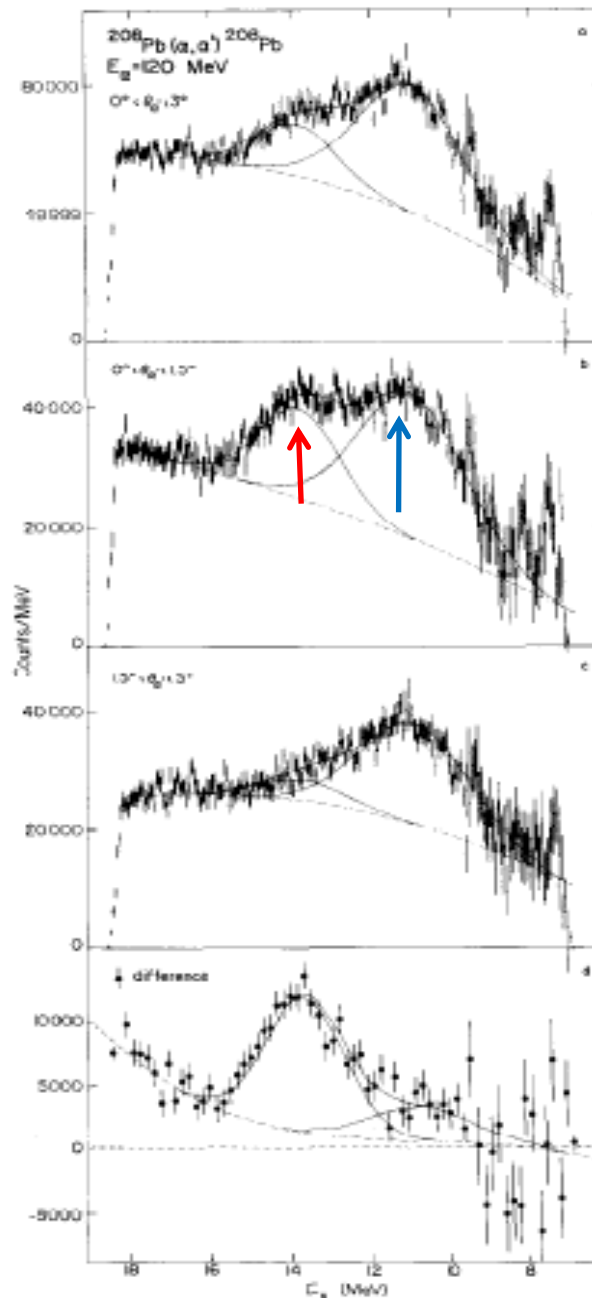
Difference of spectra

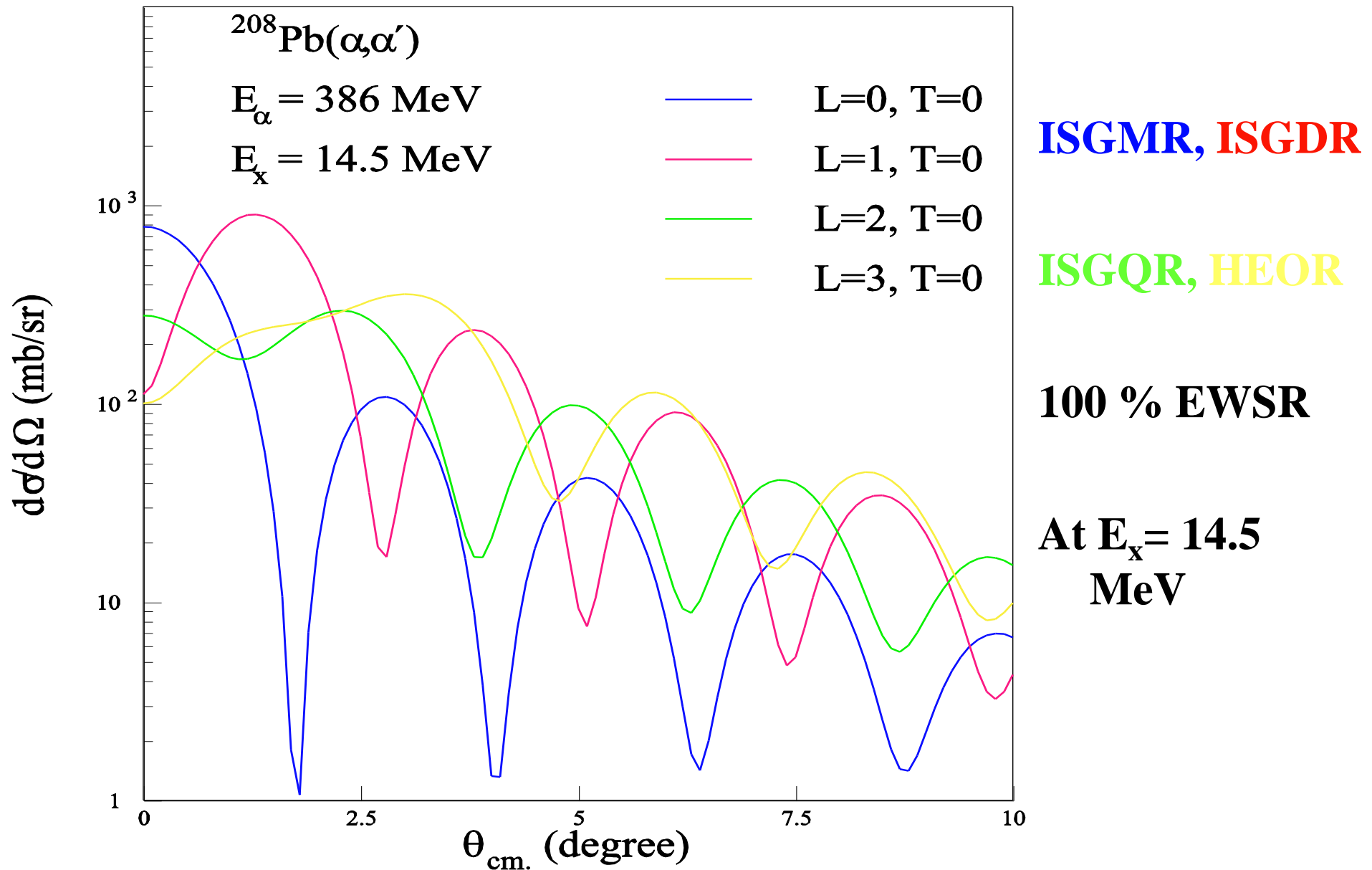
$$0^\circ < \theta_{\alpha'} < 3^\circ$$

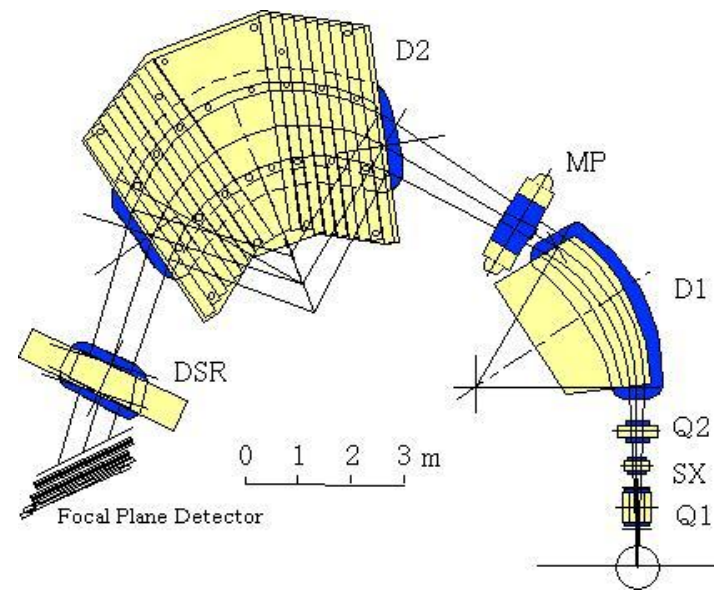
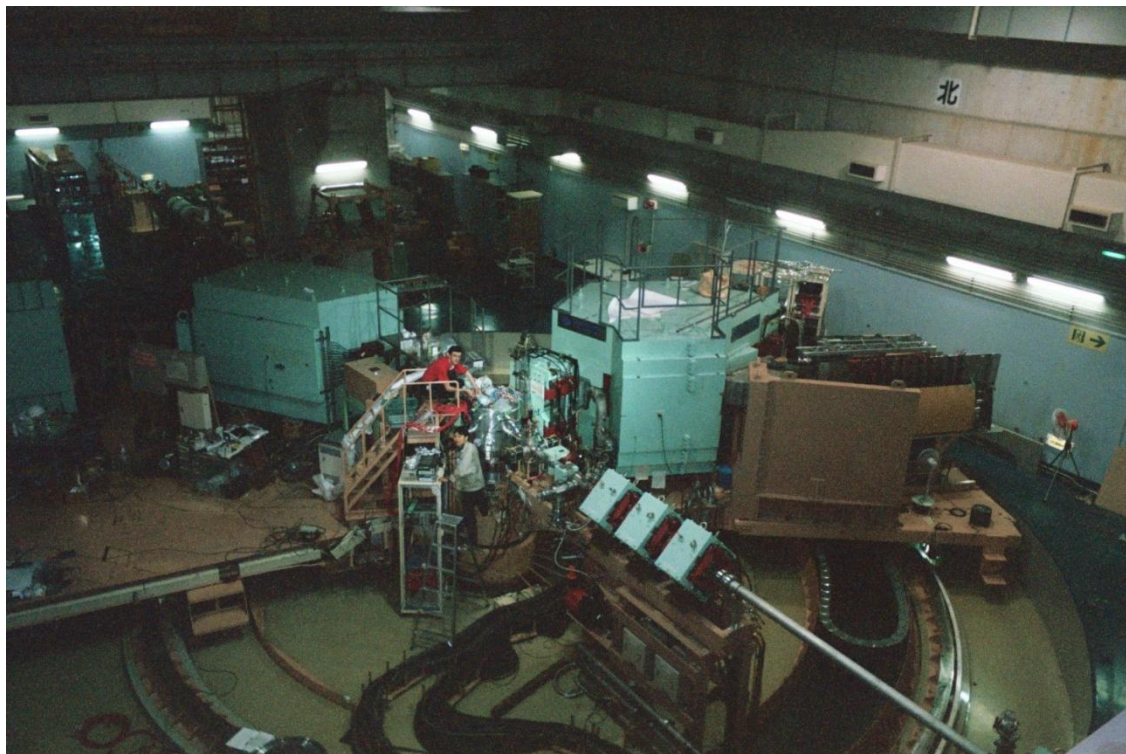
$$0^\circ < \theta_{\alpha'} < 1.5^\circ$$

$$1.5^\circ < \theta_{\alpha'} < 3^\circ$$

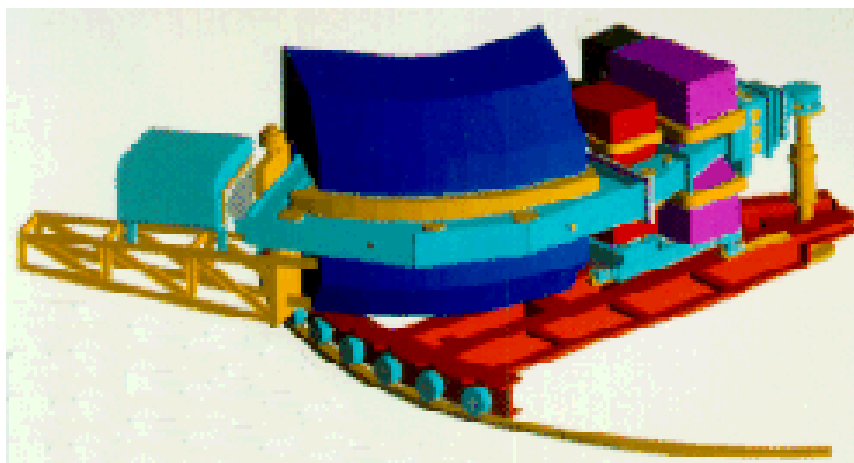
Difference





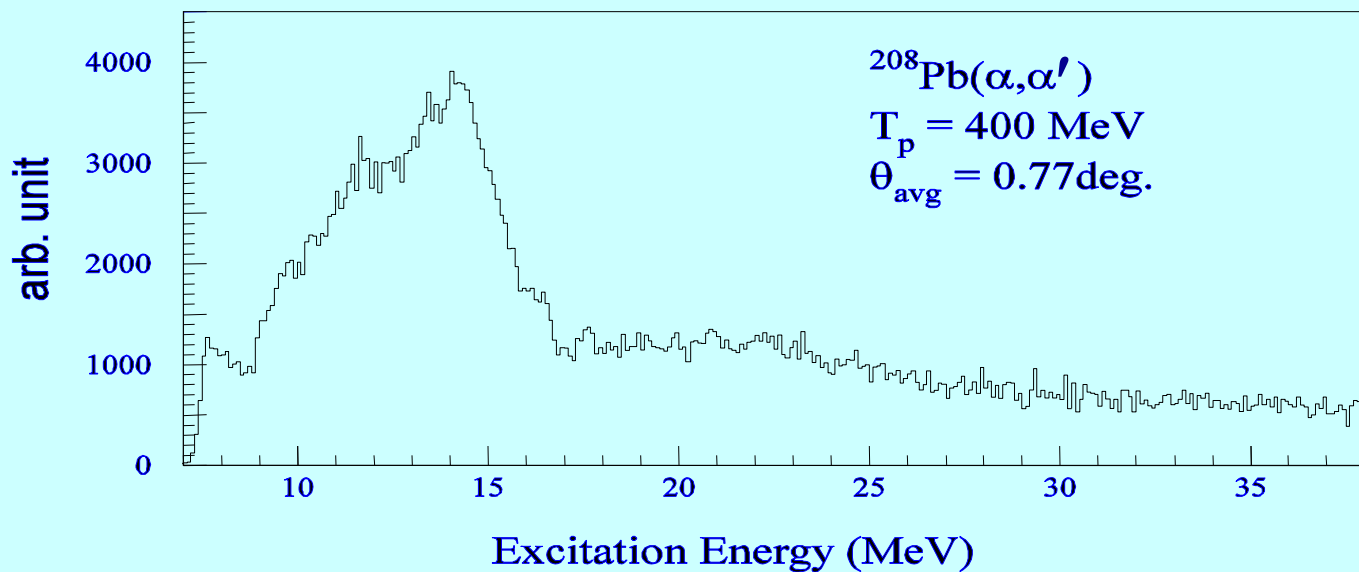
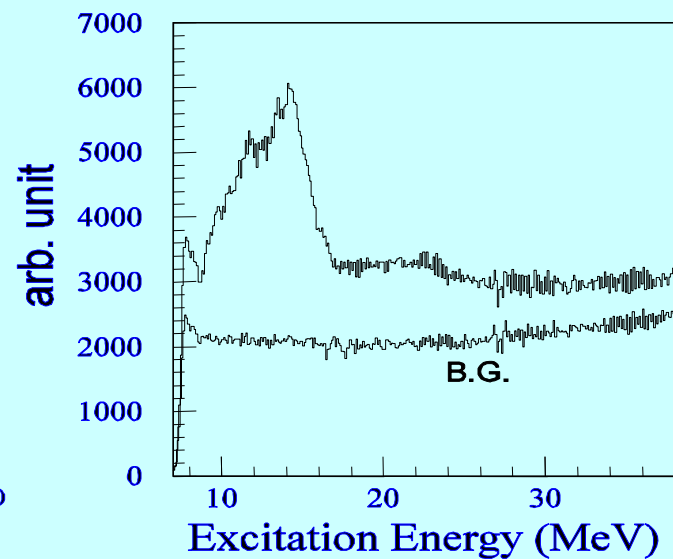
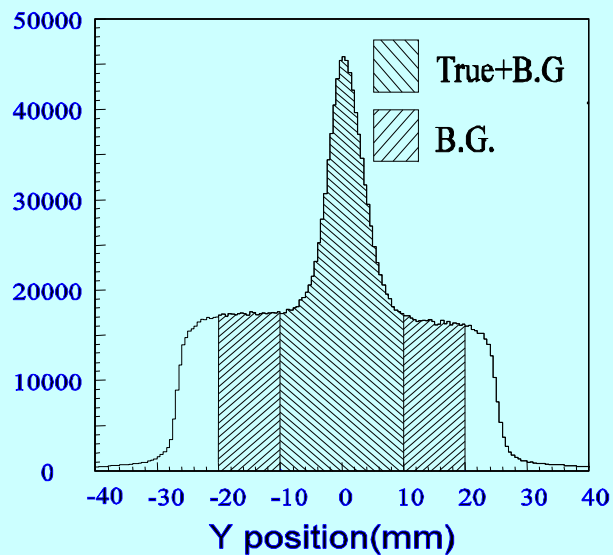


Grand Raiden@ RCNP



BBS@KVI

(α, α') at $E_\alpha \sim 400$
& **200** MeV at
RCNP & KVI,
respectively



Multipole decomposition analysis (MDA)

$$\left(\frac{d^2\sigma}{d\Omega dE}(\mathcal{G}_{c.m.}, E) \right)^{\text{exp.}} = \sum_L a_L(E) \left(\frac{d^2\sigma}{d\Omega dE}(\mathcal{G}_{c.m.}, E) \right)_L^{\text{calc.}}$$

$$\left(\frac{d^2\sigma}{d\Omega dE}(\mathcal{G}_{c.m.}, E) \right)^{\text{exp.}} : \text{Experimental cross section}$$

$$\left(\frac{d^2\sigma}{d\Omega dE}(\mathcal{G}_{c.m.}, E) \right)_L^{\text{calc.}} : \text{DWBA cross section (unit cross section)}$$

$a_L(E)$: EWSR fraction

- a. **ISGR (L<15)+ IVGDR (through Coulomb excitation)**
- b. **DWBA formalism; single folding \Rightarrow transition potential**

$$\delta U(r, E) = \int d\vec{r}' \delta\rho_L(\vec{r}', E) [V(|\vec{r} - \vec{r}'|, \rho_0(r')) + \rho_0(r') \frac{\partial V(|\vec{r} - \vec{r}'|, \rho_0(r'))}{\partial \rho_0(r')}]$$

$$U(r) = \int d\vec{r}' V(|\vec{r} - \vec{r}'|, \rho_0(r')) \rho_0(r')$$

Transition density

- ISGMR Satchler, Nucl. Phys. A472 (1987) 215

$$\delta\rho_0(r, E) = -\alpha_0\left[3 + r \frac{d}{dr}\right]\rho_0(r)$$

$$\alpha_0^2 = \frac{2\pi\hbar^2}{mA \langle r^2 \rangle E}$$

- ISGDR Harakeh & Dieperink, Phys. Rev. C23 (1981) 2329

$$\delta\rho_1(r, E) = -\frac{\beta_1}{R\sqrt{3}}\left[3r^2 + \frac{d}{dr} + 10r - \frac{5}{3} \langle r^2 \rangle \frac{d}{dr} + \varepsilon\left(r \frac{d^2}{dr^2} + 4 \frac{d}{dr}\right)\right]\rho_0(r)$$

$$\beta_1^2 = \frac{6\pi\hbar^2}{mAE} \frac{R^2}{(11 \langle r^4 \rangle - (25/3) \langle r^2 \rangle^2 - 10\varepsilon \langle r^2 \rangle)}$$

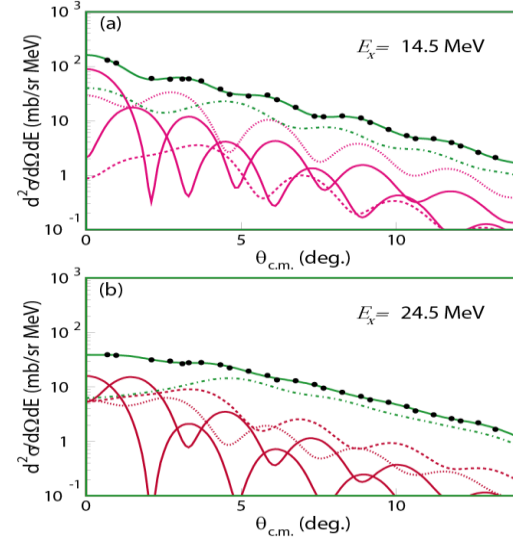
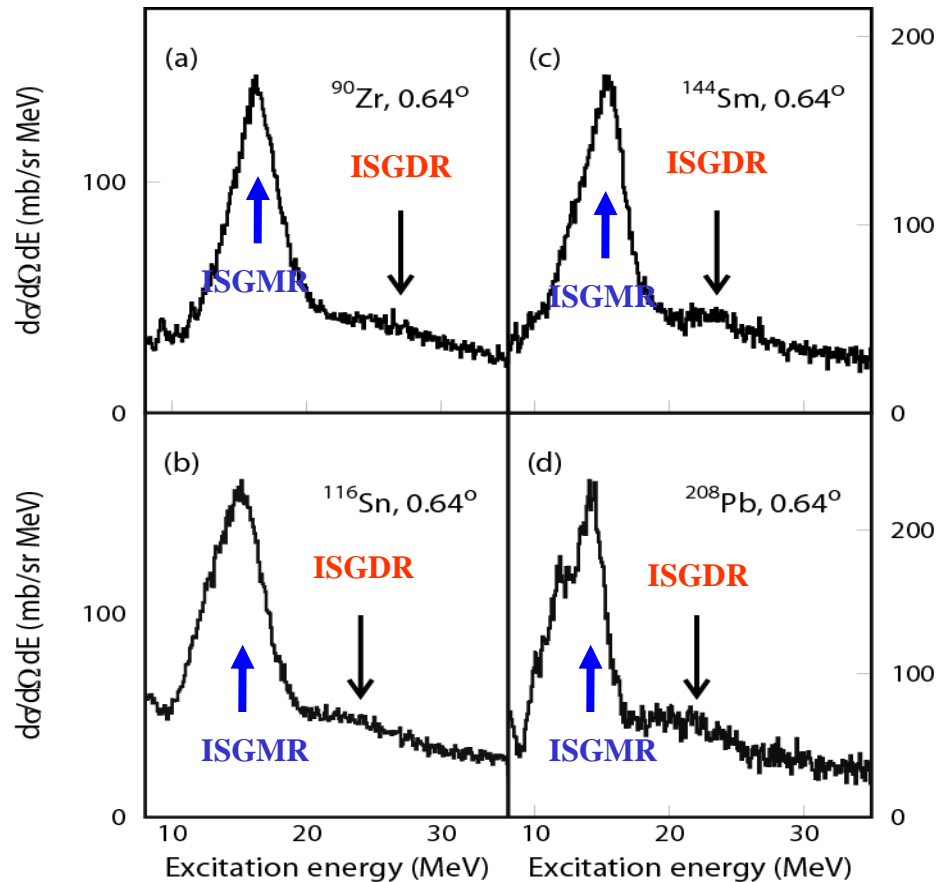
- Other modes Bohr-Mottelson (BM) model

$$\delta\rho_L(r, E) = -\delta_L \frac{d}{dr} \rho_0(r)$$

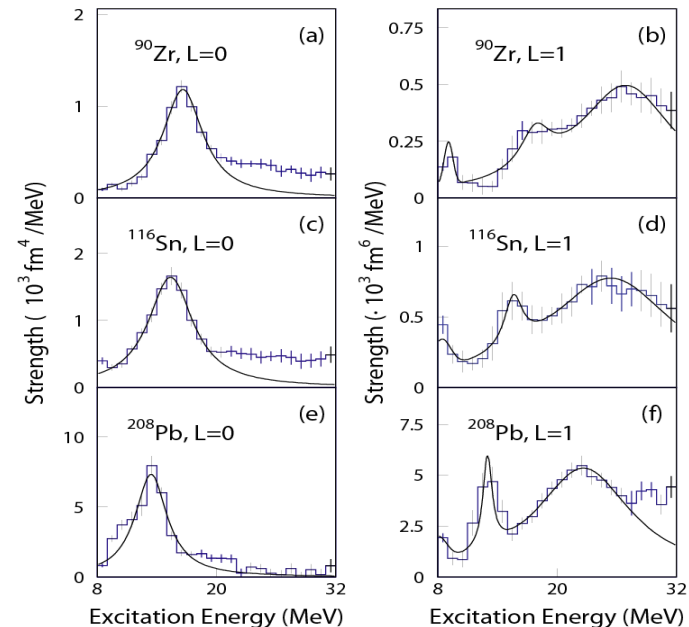
$$\delta_L^2 = (\beta_L c)^2 = \frac{l(2l+1)^2}{(l+2)^2} \frac{2\pi\hbar^2}{mAE} \frac{\langle r^{2l-2} \rangle}{\langle r^{l-2} \rangle^2}$$

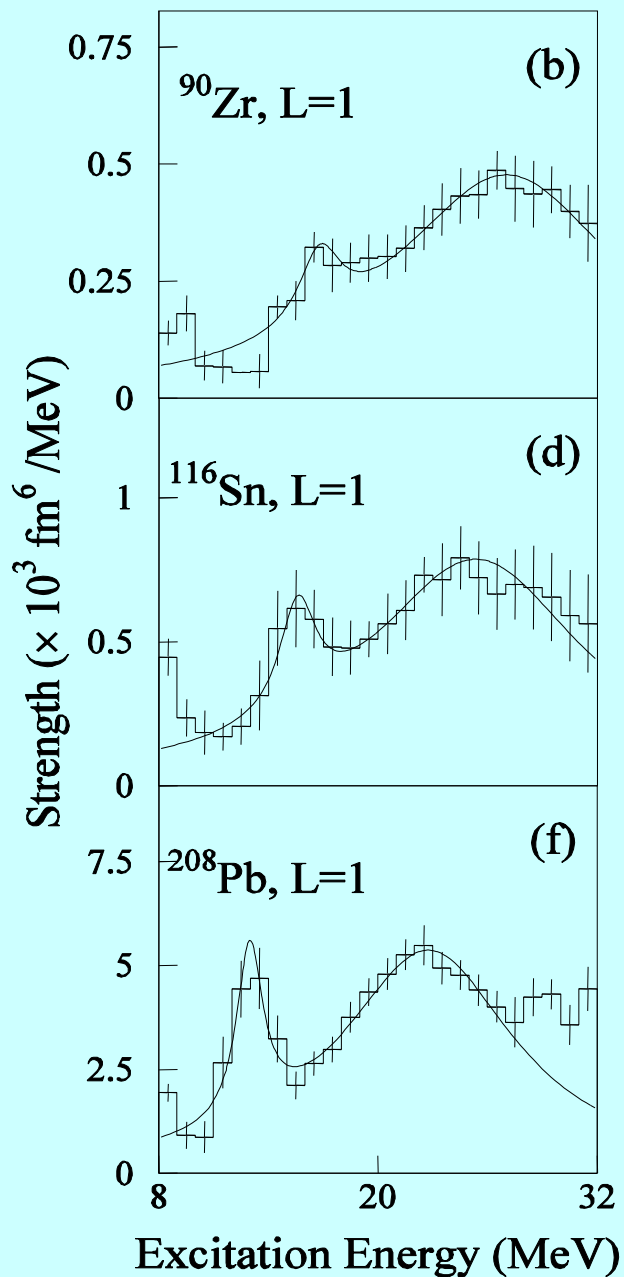
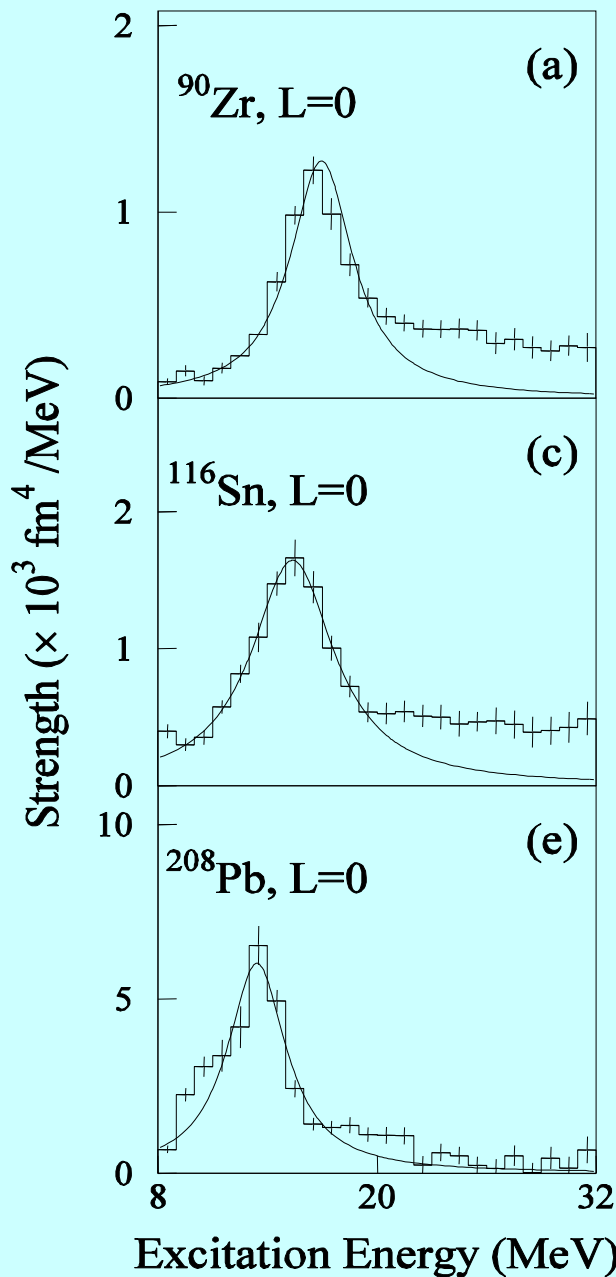
Uchida *et al.*,
Phys. Lett. B557 (2003) 12
Phys. Rev. C69 (2004) 051301
(α, α') spectra at 386
MeV

^{116}Sn



MDA results for L=0 and L=1





In HF+RPA calculations,

$$K_{nm} = \left[9\rho^2 \frac{d^2(E/A)}{d\rho^2} \right]_{\rho = \rho_0}$$

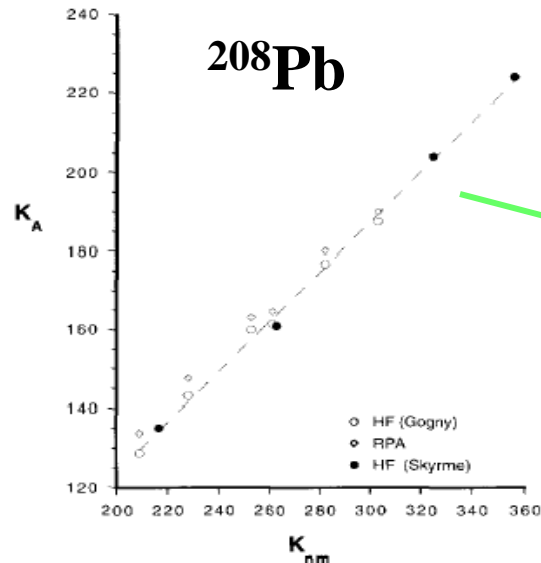
Nuclear matter

E/A : binding energy per nucleon

K_A : incompressibility

ρ : nuclear density

ρ_0 : nuclear density at saturation



K_A is obtained from excitation energy of ISGMR & ISGDR

$$K_A = 0.64K_{nm} - 3.5$$

J.P. Blaizot, NPA591 (1995) 435

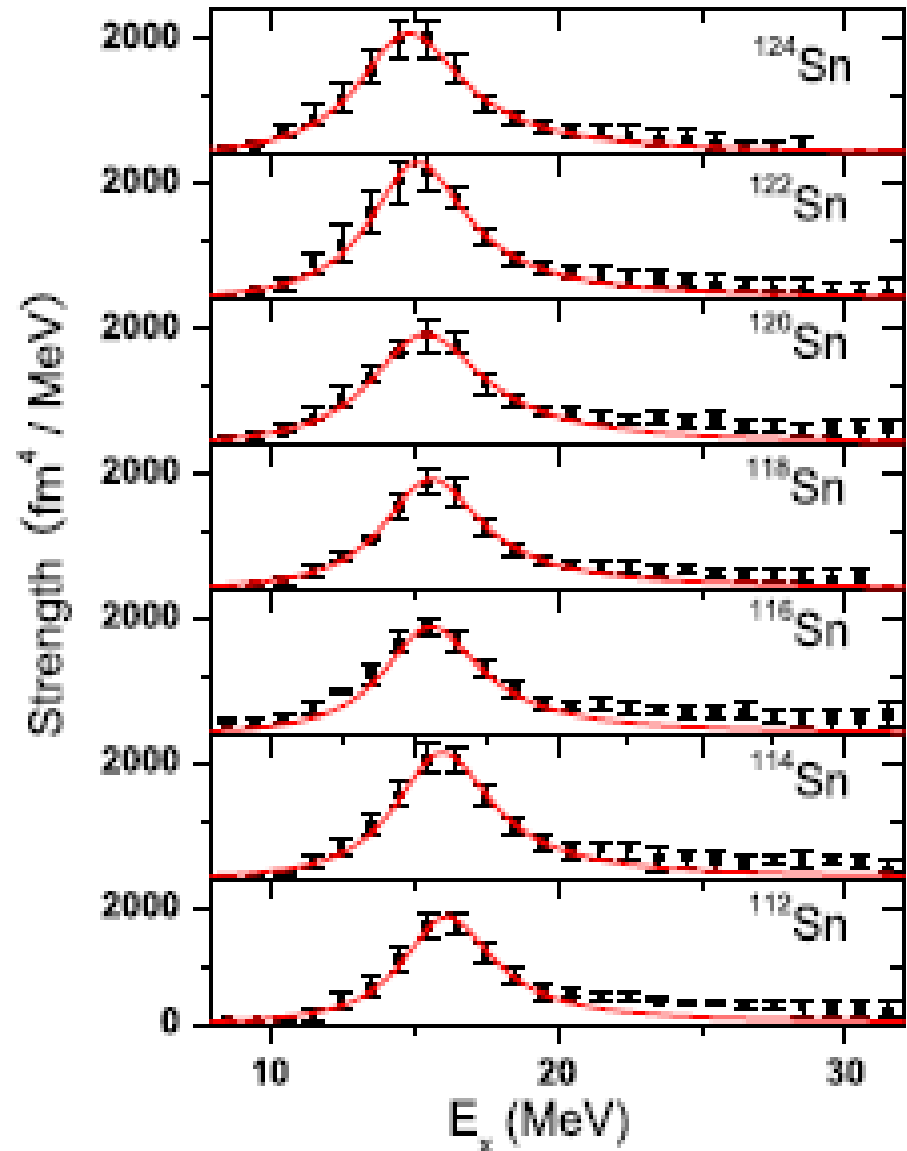
From GMR data on ^{208}Pb and ^{90}Zr ,

$$K_{\infty} = 240 \pm 10 \text{ MeV}$$

[See, *e.g.*, G. Colò *et al.*, Phys. Rev. C 70 (2004) 024307]

**This number is consistent
with both ISGMR and ISGDR Data
and
with non-relativistic and relativistic calculations**

Isoscalar GMR strength distribution in Sn-isotopes obtained by Multipole Decomposition Analysis of singles spectra obtained in $^A\text{Sn}(\alpha, \alpha')$ measurements at incident energy 400 MeV and angles from 0° to 9°



$$K_A \sim K_{vol} (1 + cA^{-1/3}) + K_\tau ((N - Z)/A)^2 + K_{Coul} Z^2 A^{-4/3}$$

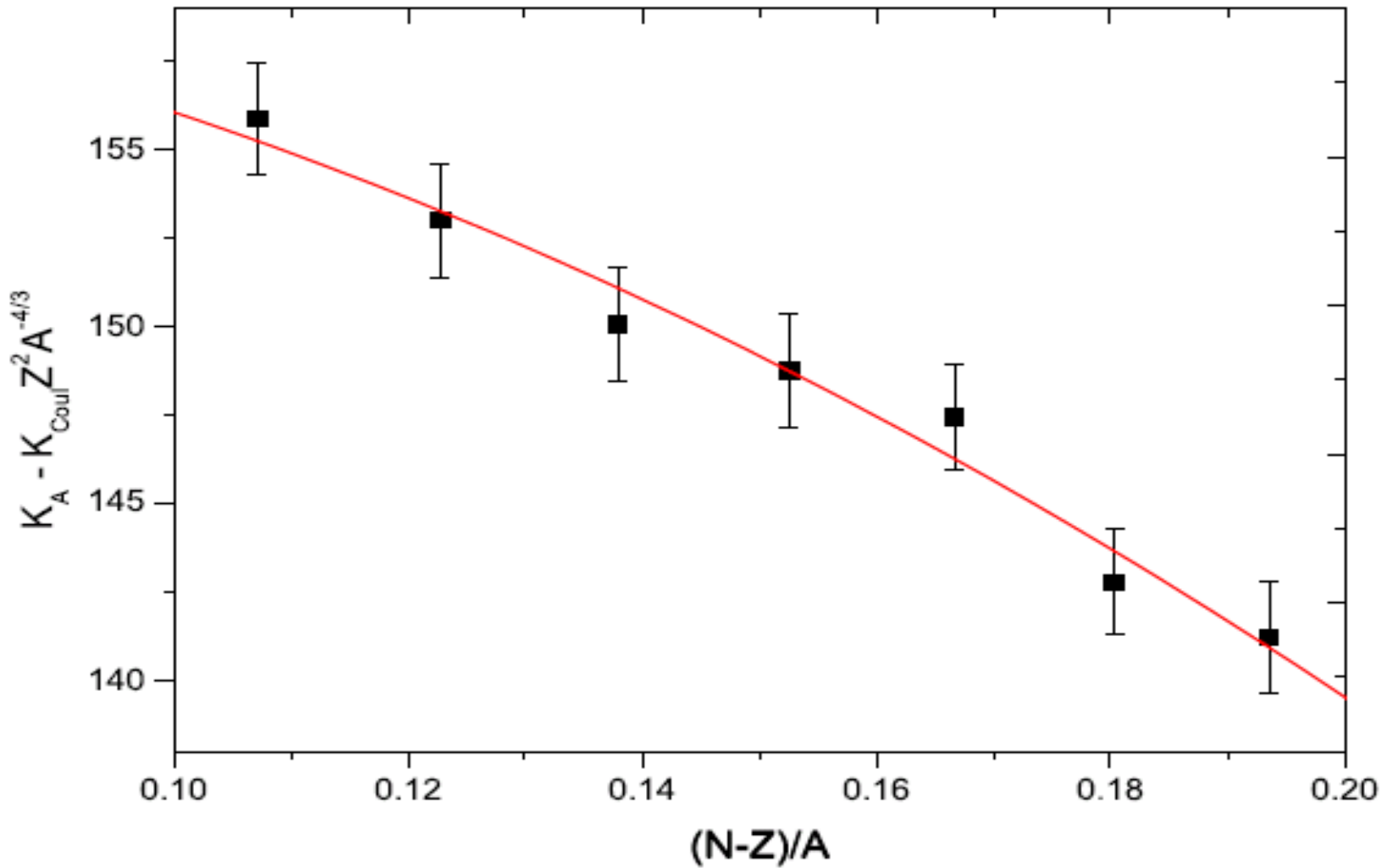
$$K_A - K_{Coul} Z^2 A^{-4/3} \sim K_{vol} (1 + cA^{-1/3}) + K_\tau ((N - Z)/A)^2$$

$$\sim \text{Constant} + K_\tau ((N - Z)/A)^2$$

We use $K_{Coul} = - 5.2 \text{ MeV}$ (from Sagawa)

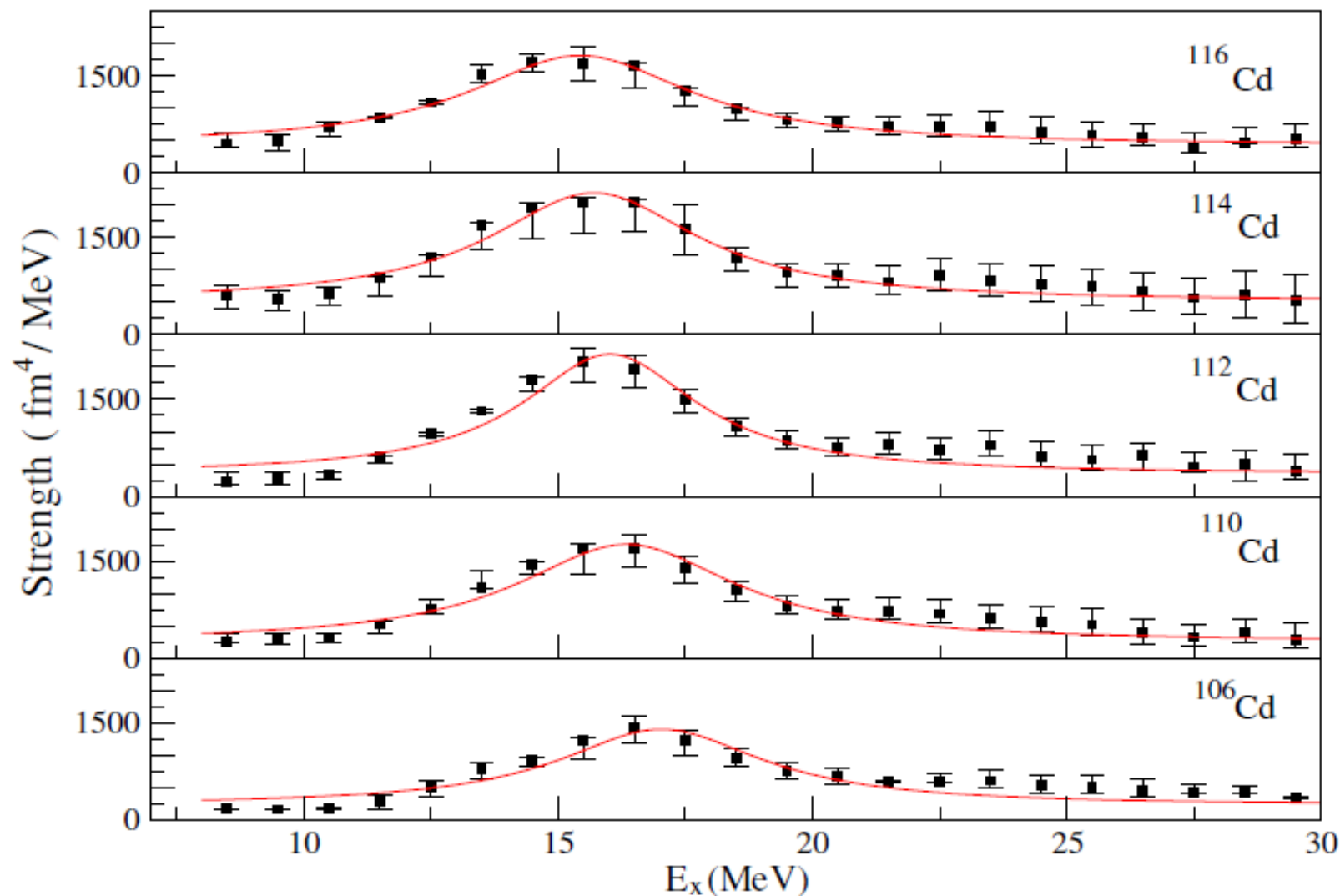
$$N-Z/A$$

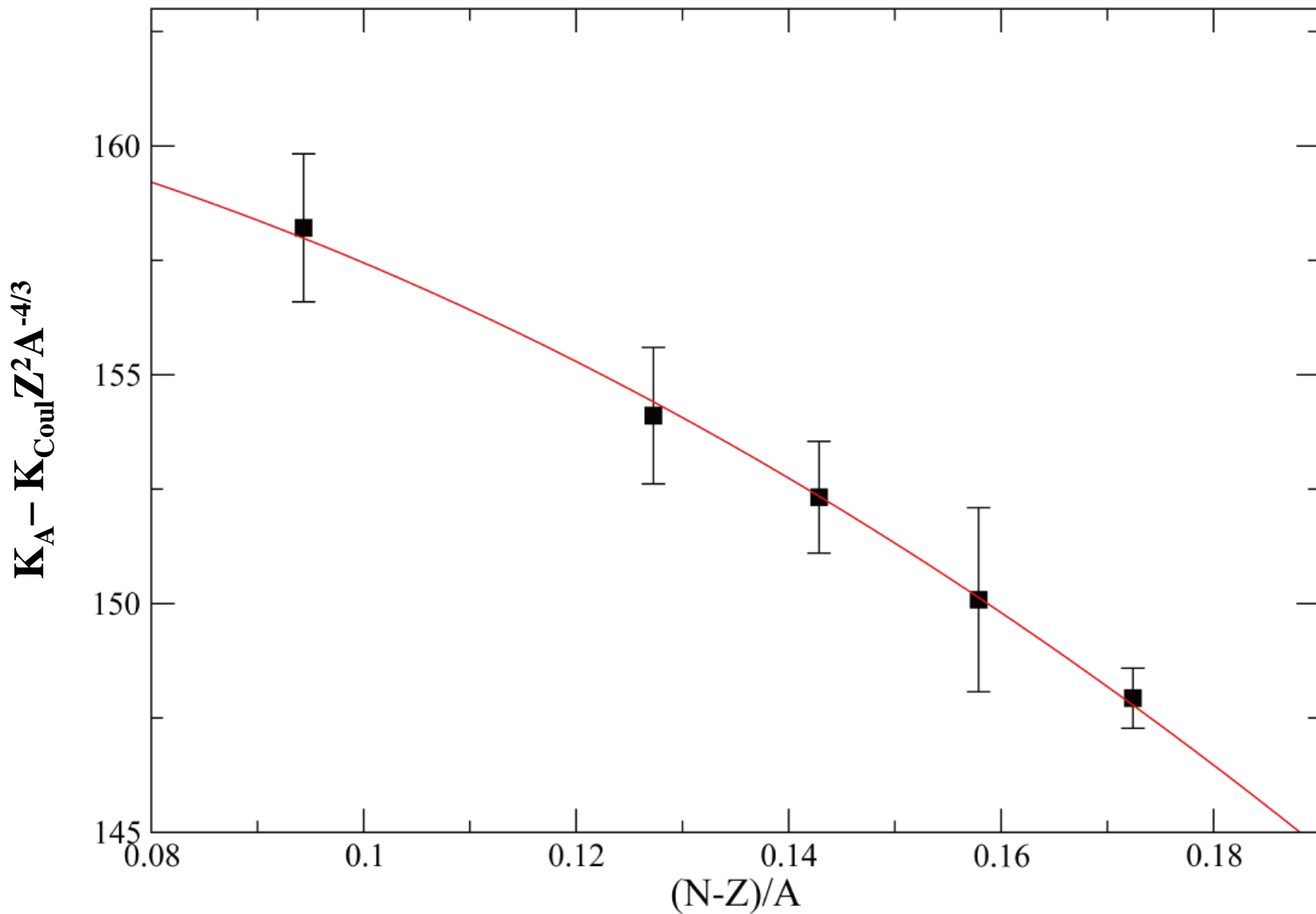
$$^{112}\text{Sn} - ^{124}\text{Sn}: \mathbf{0.107 - 0.194}$$



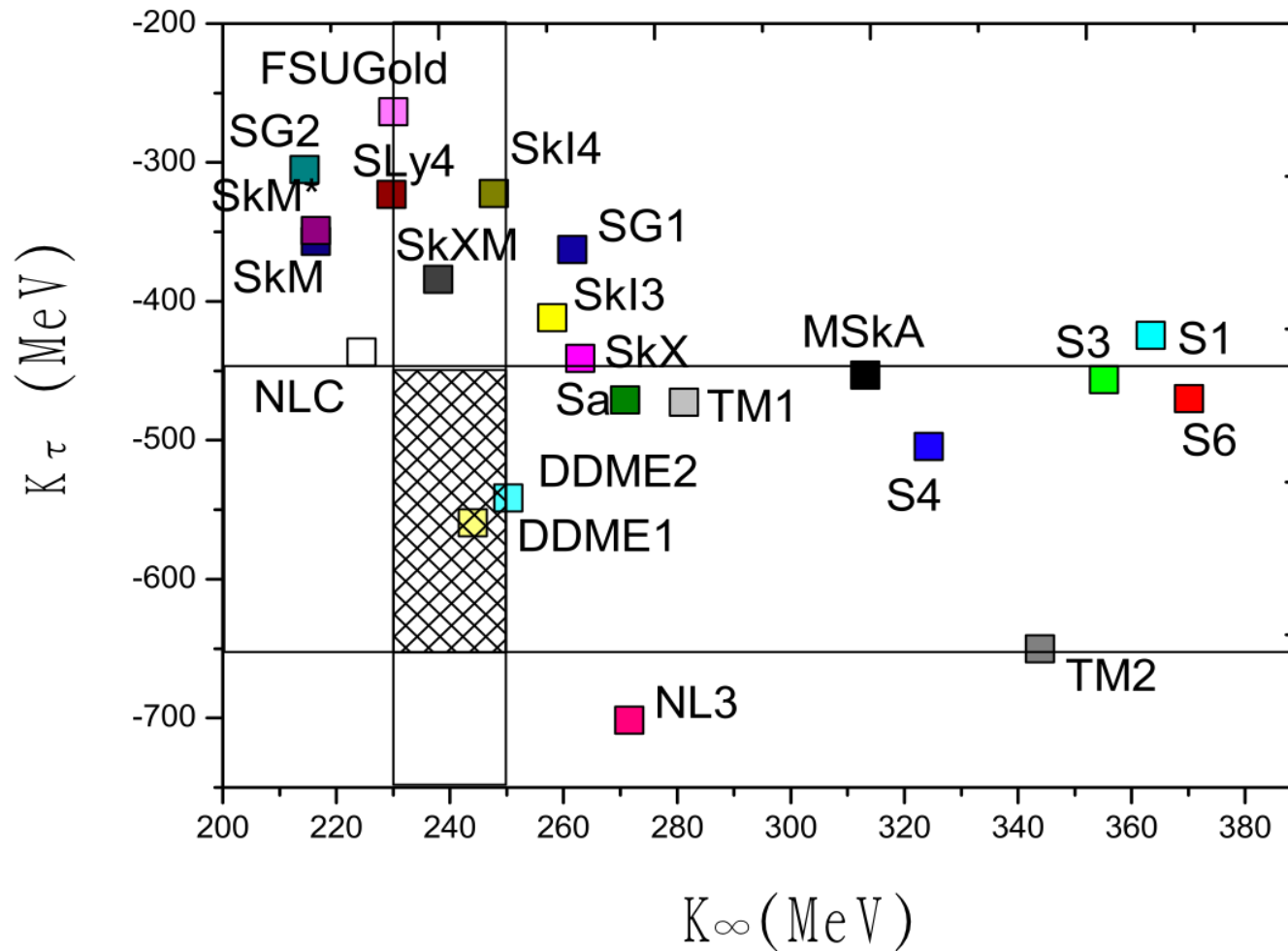
$$K_{\tau} = -550 \pm 100 \text{ MeV}$$

Monopole strength Distribution

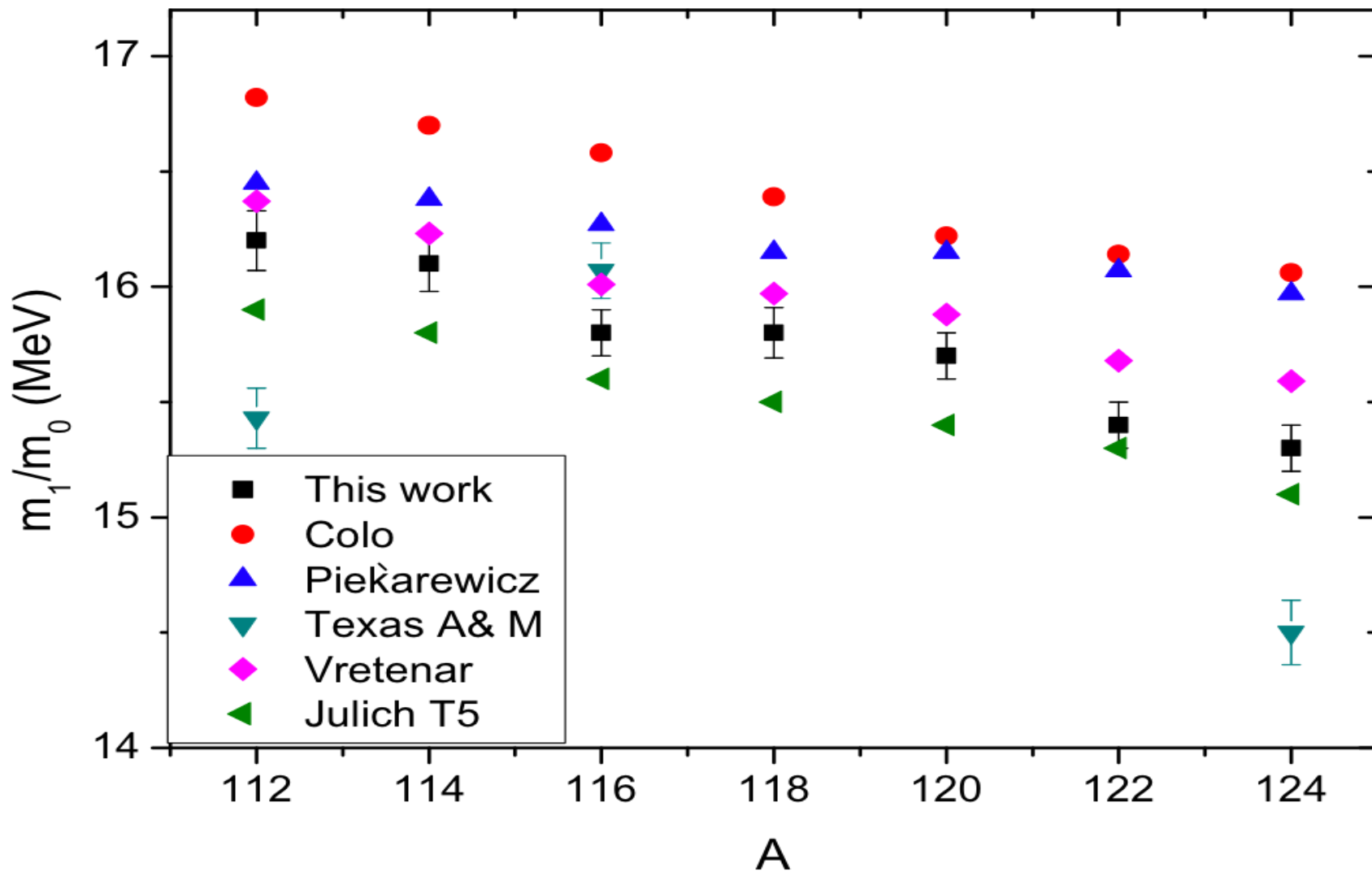




$$K_{\tau} = -480 \pm 100 \text{ MeV}$$



Data from H. Sagawa *et al.*, Phys. Rev. C 76, 034327 (2007)



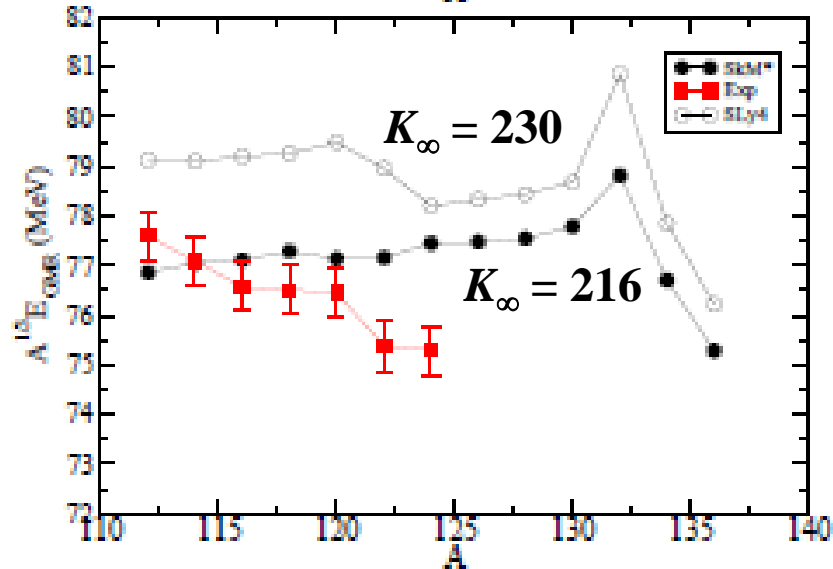
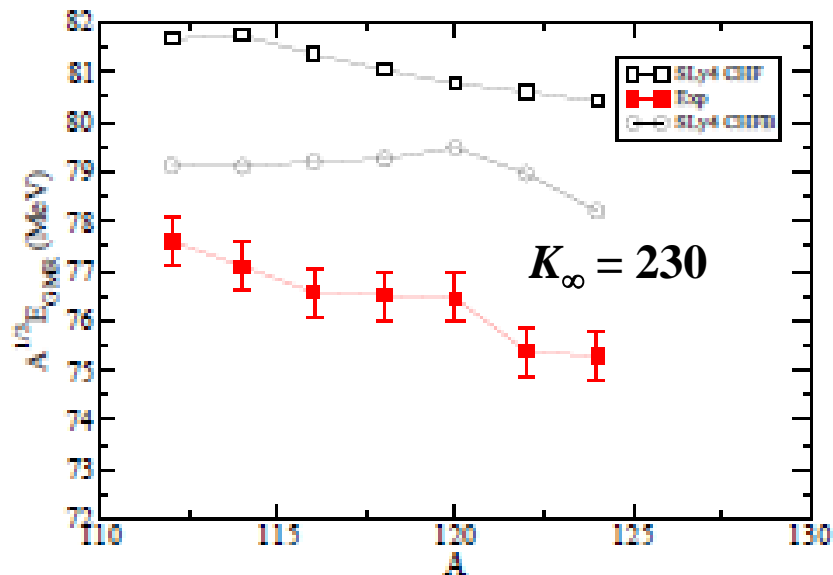
Colò *et al.*: Non-relativistic RPA (without pairing) reproduces ISGMR in ^{208}Pb and ^{90}Zr .

Piekarewicz: Relativistic RPA (FSUGold model) reproduces g.s. observables and ISGMR in ^{208}Pb , ^{144}Sm and ^{90}Zr

**Vretenar: Relativistic mean field (DD-ME2: density-dependent mean-field effective interaction).
Possibly agreement is fortuitous since strength distributions are not much different from those by Colò *et al.* and Piekarewicz.**

**Tselyaev *et al.*: Quasi-particle time-blocking approximation (QTBA) (T5 Skyrme interaction)
 $K_{\infty} = 202 \text{ MeV?!}$**

Softness of Sn-nuclei is still unresolved



The Giant Monopole Resonances in Pb isotopes
 E. Khan, Phys. Rev. C 80, 057302 (2009).

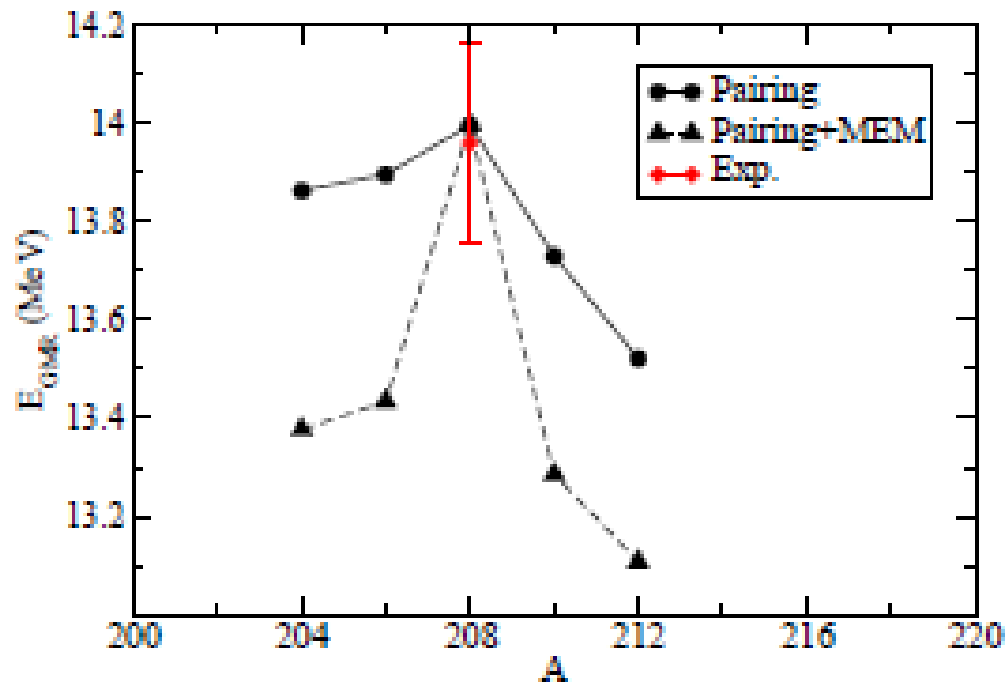
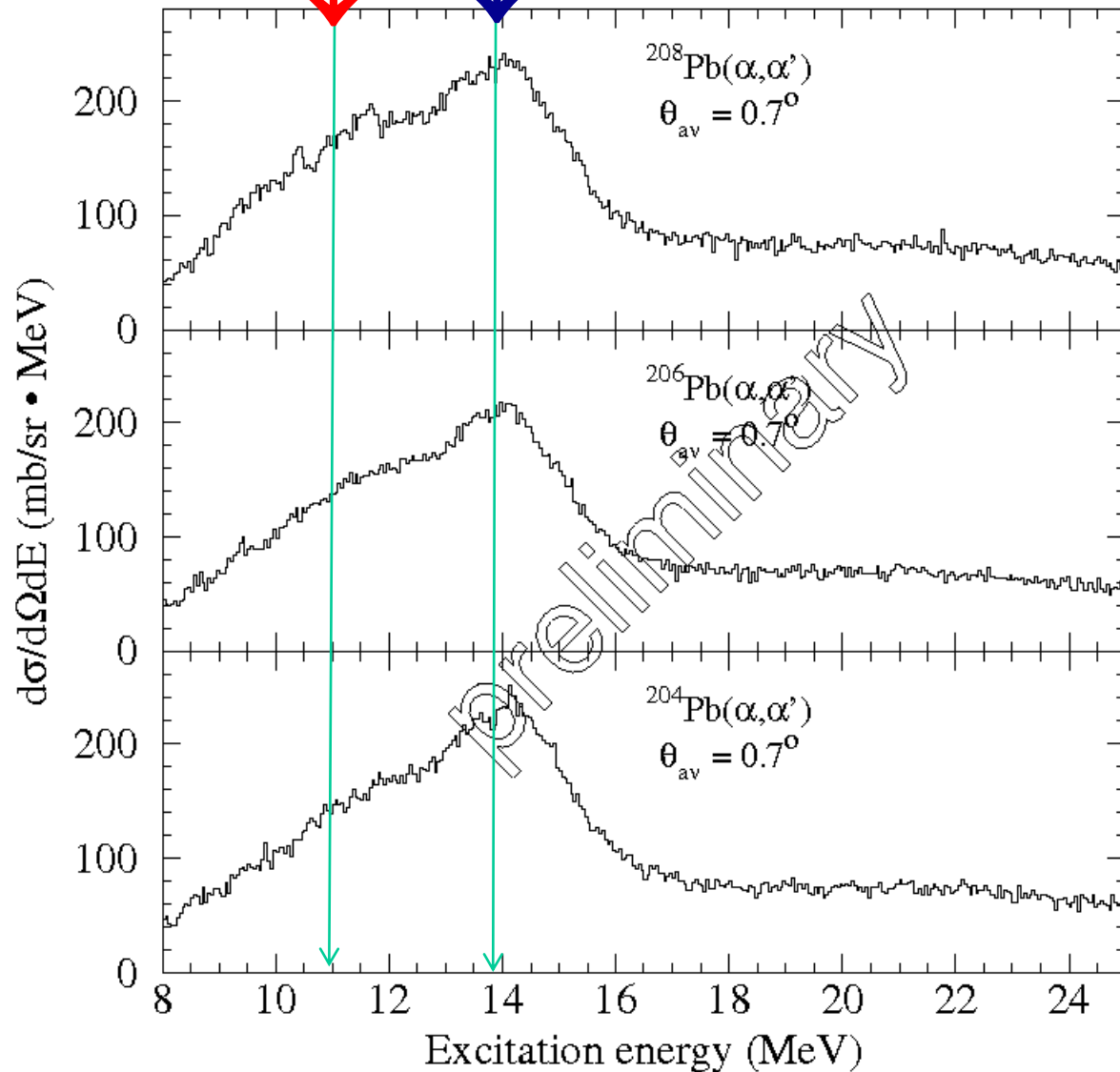


FIG. 2: Excitations energies of the GMR in $^{204-212}\text{Pb}$ isotopes calculated with constrained HFB method, taking into account the MEM effect (see text). The experimental data is taken from Ref. [22]

Mutually Enhanced
 Magicity (MEM)?

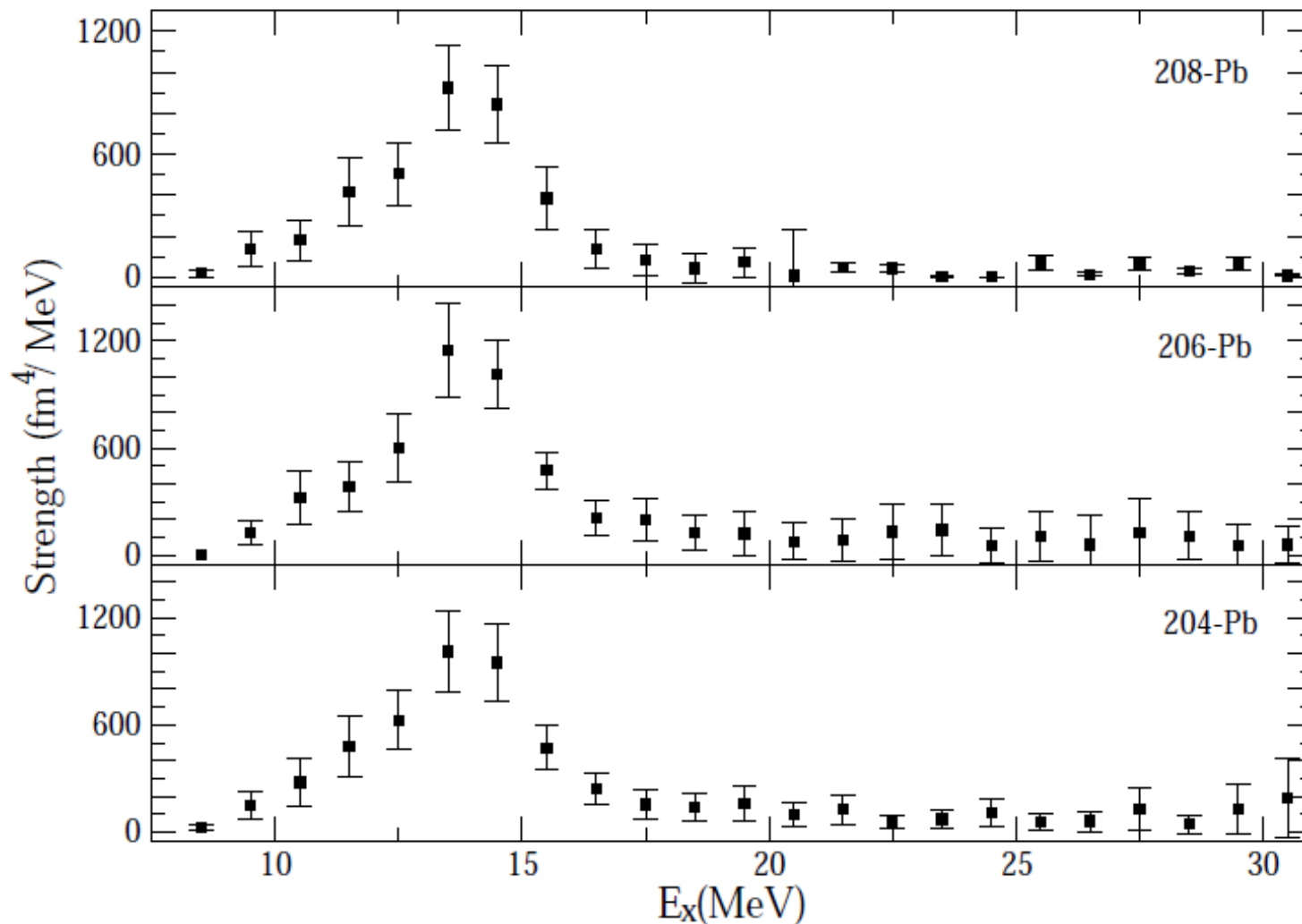
ISGQR ISGMR

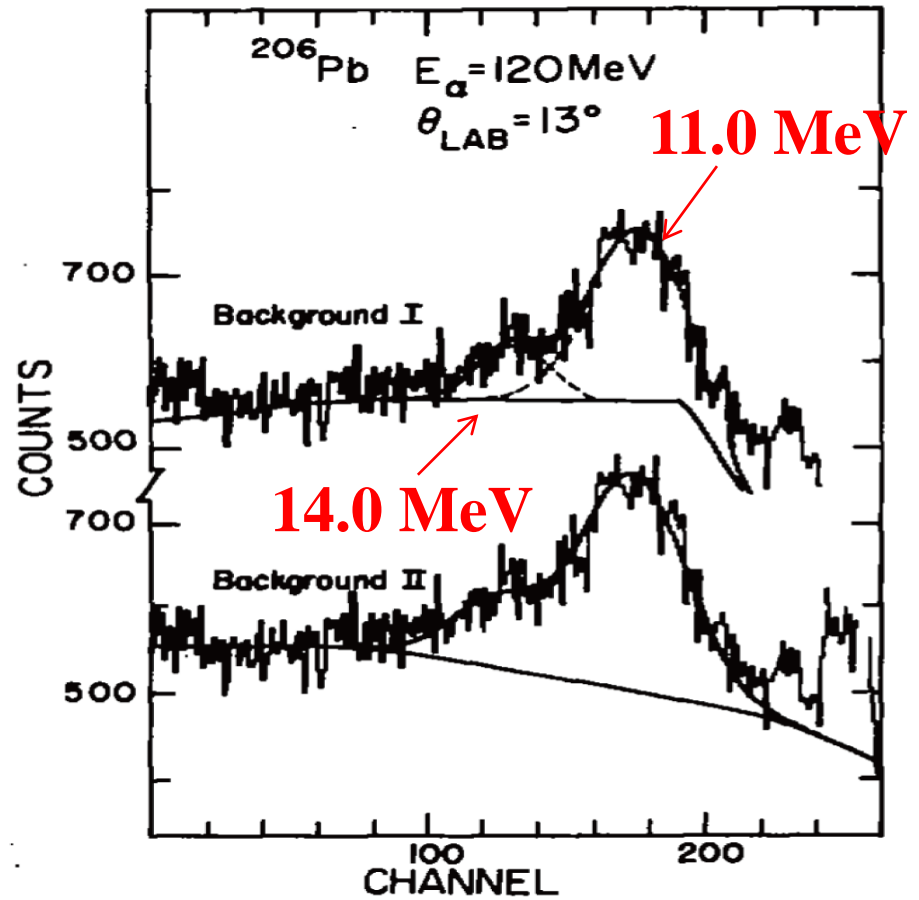
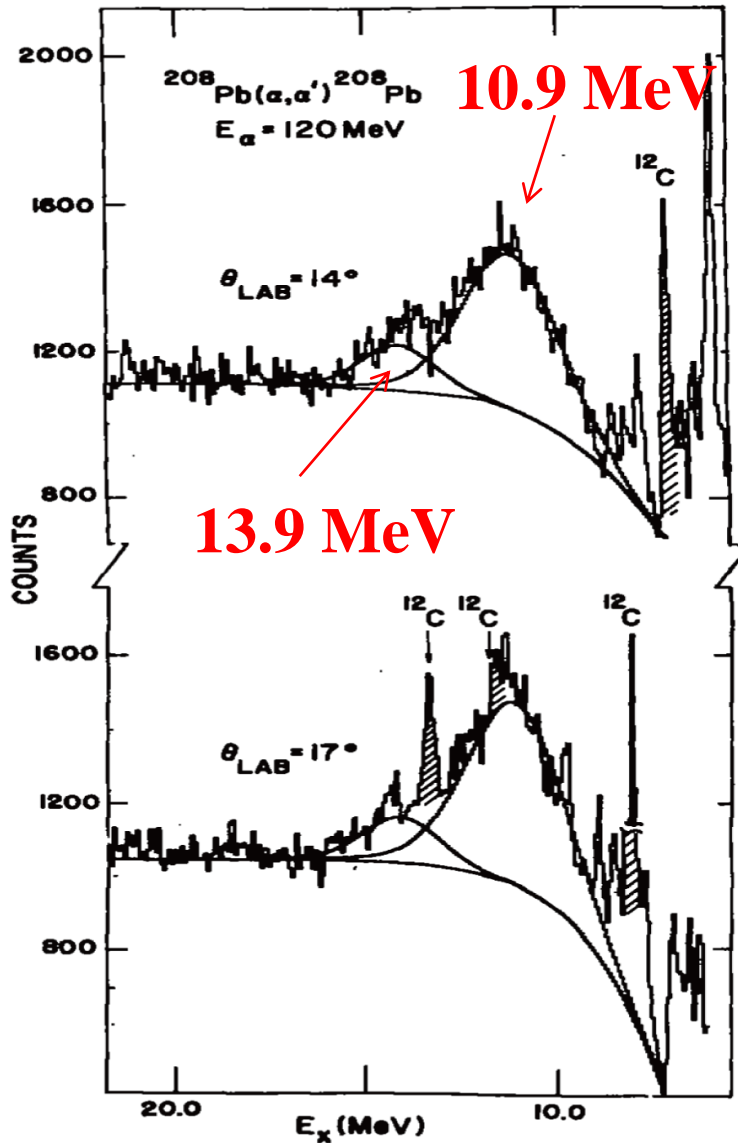
$E_{\alpha} = 400 \text{ MeV}$



208 13.9 MeV
206 13.94 MeV
204 13.98 MeV

Monopole strength Distribution





M.N. Harakeh *et al.*, Nucl. Phys. A327, 373 (1979)

Decay of giant resonances

- Width of resonance

$\Gamma, \Gamma^\uparrow, \Gamma^\downarrow$ ($\Gamma^\downarrow^\uparrow, \Gamma^\downarrow^\downarrow$)

- Γ^\uparrow : direct or escape width

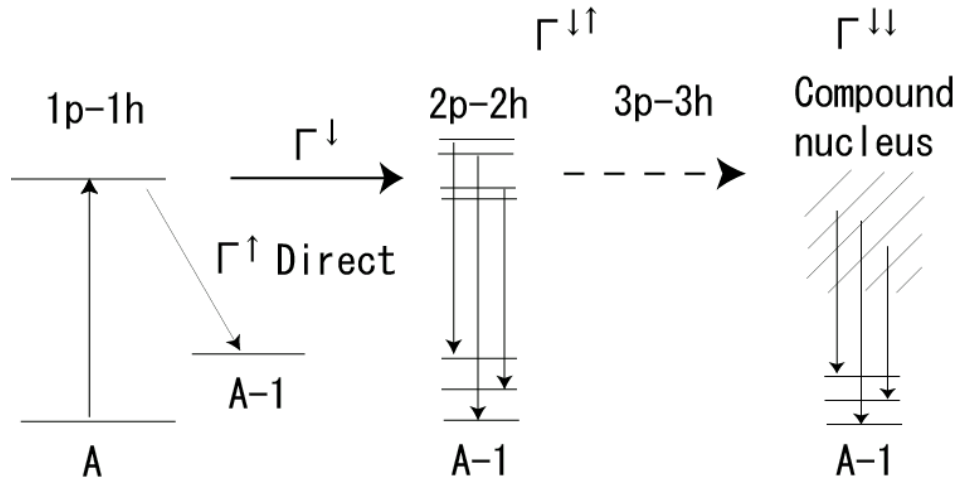
- Γ^\downarrow : spreading width

$\Gamma^\downarrow^\uparrow$: pre-equilibrium, $\Gamma^\downarrow^\downarrow$: compound

- Decay measurements

⇒ Direct reflection of damping processes

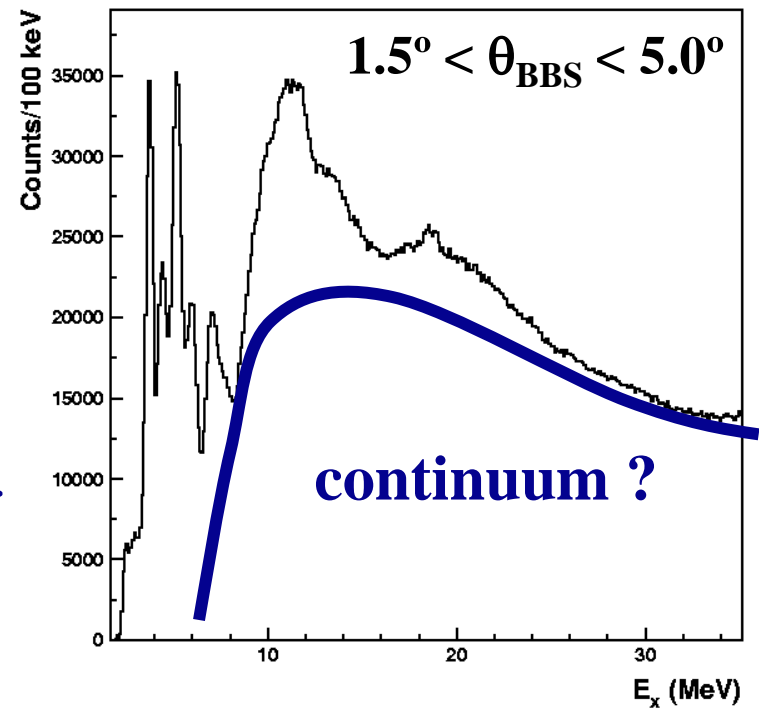
Allows detailed comparison with theoretical calculations



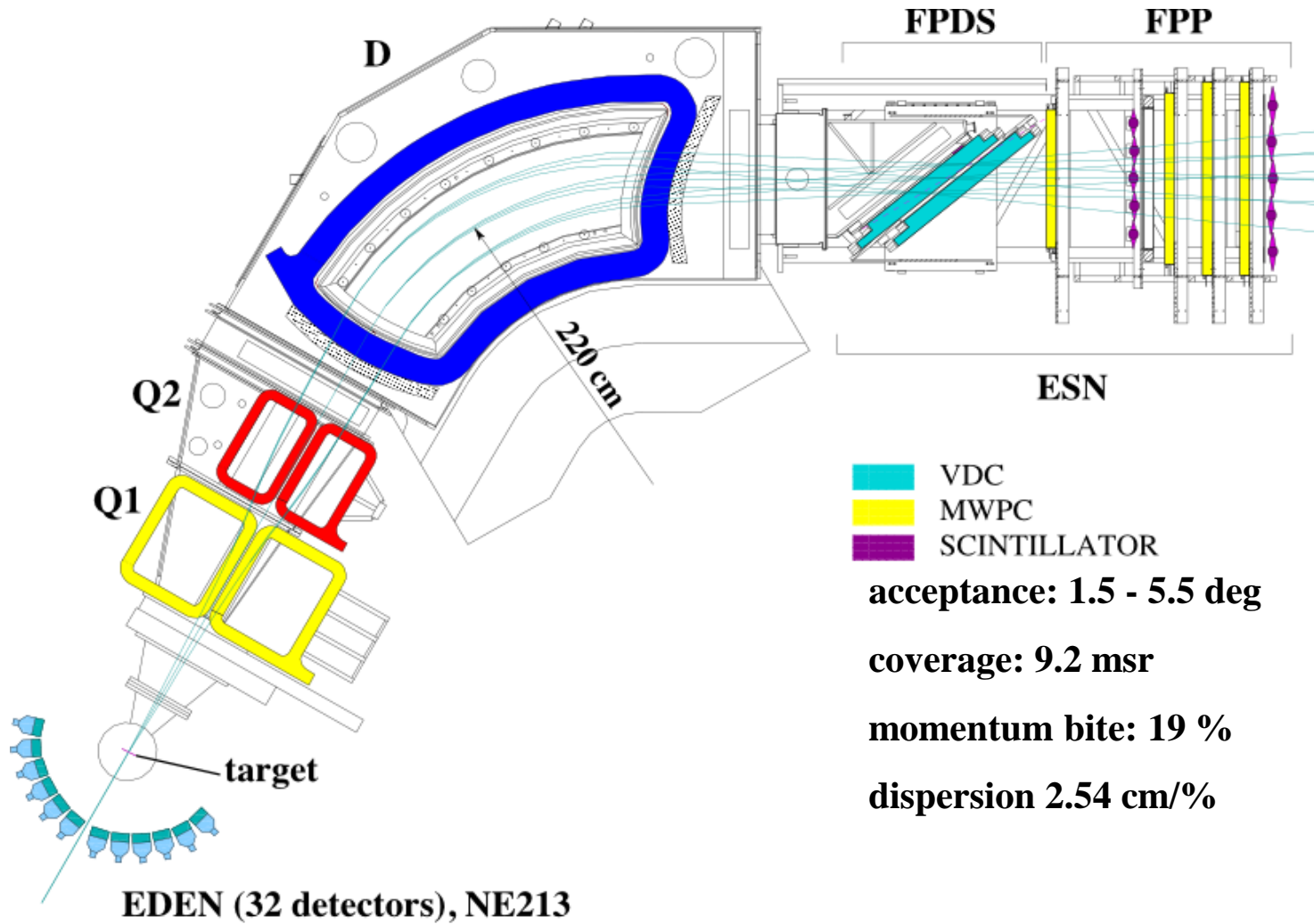
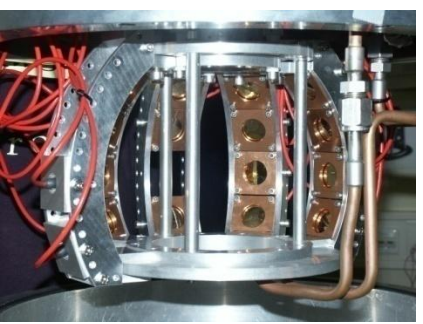
Excitation of ISGDR in ^{208}Pb

- In ^{208}Pb located around 22 MeV and width of 4 MeV
- $L=1$ angular distribution peaks close to a scattering angle of 0°
- Difficult to identify in nuclear continuum and rides on instrumental background

Singles $^{208}\text{Pb}(\alpha, \alpha')$ 200 MeV \Rightarrow



Si-ball
16 Si-detectors at
10 cm from the target
total solid angle: 1 sr



acceptance: 1.5 - 5.5 deg

coverage: 9.2 msr

momentum bite: 19 %

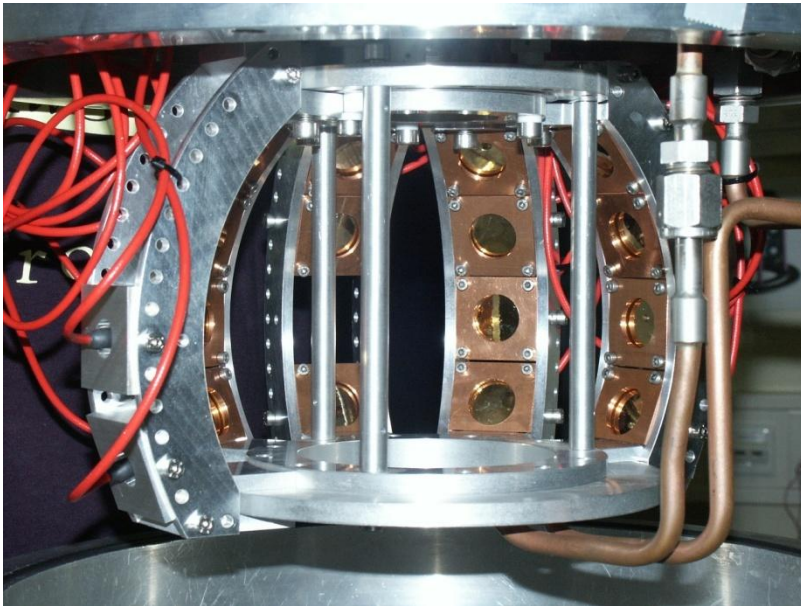
dispersion 2.54 cm/%

EDEN (32 detectors), NE213

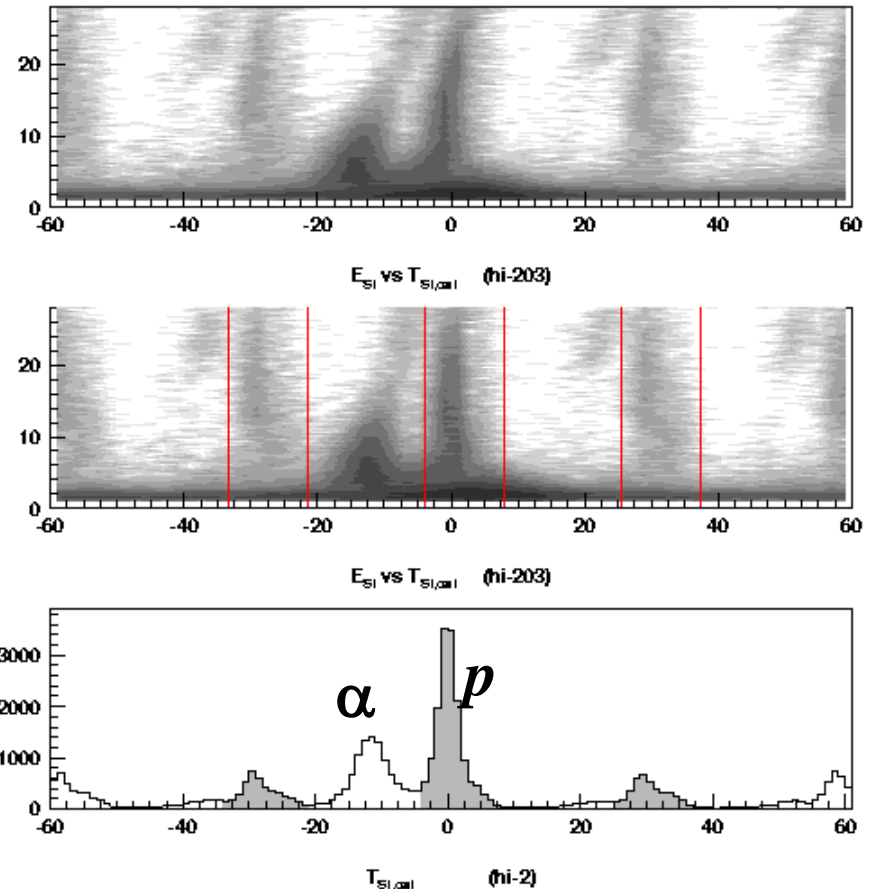
total solid angle: 0.37 sr

KVI Big-Bite Spectrometer (BBS)

Proton-decay detection



α - p separation using
rise time of signal SiLi



Microscopic structure of ISGDR

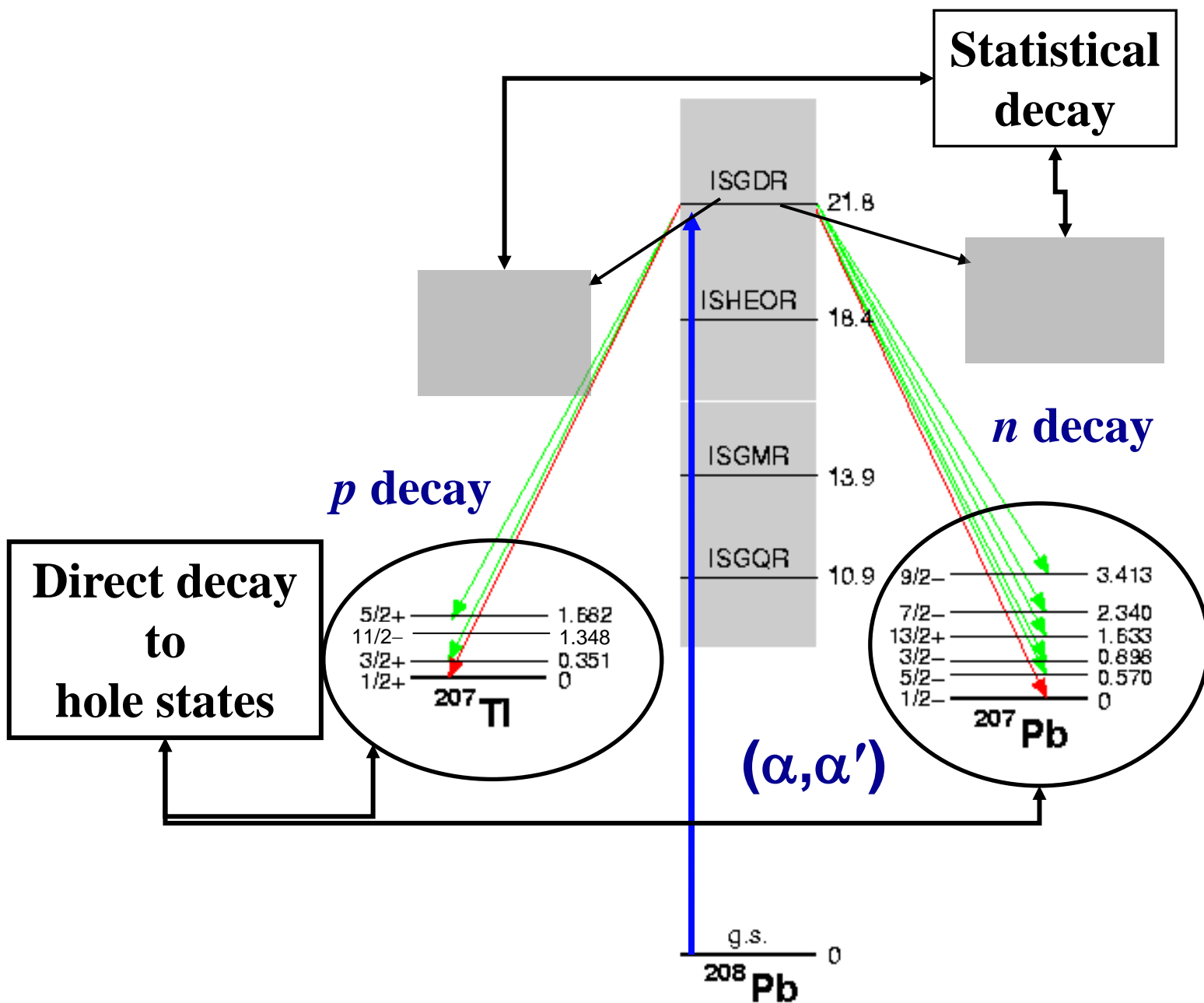
Transition operator

$$O^{L=1} = \cancel{\sum_i r_i^1 Y_0^1} + \frac{1}{2} \sum_i r_i^3 Y_0^1 + \dots$$

Spurious center
of mass motion

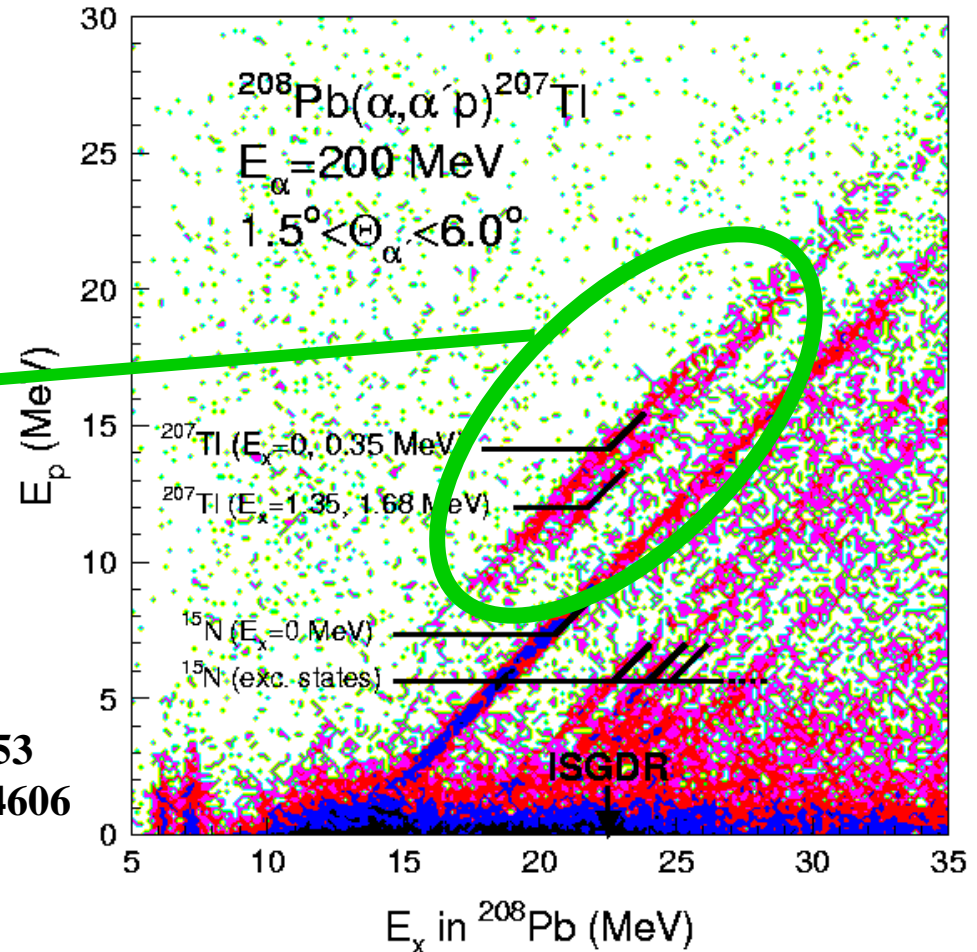
Overtone

$3\hbar\omega$ excitation (overtone of c.o.m. motion)



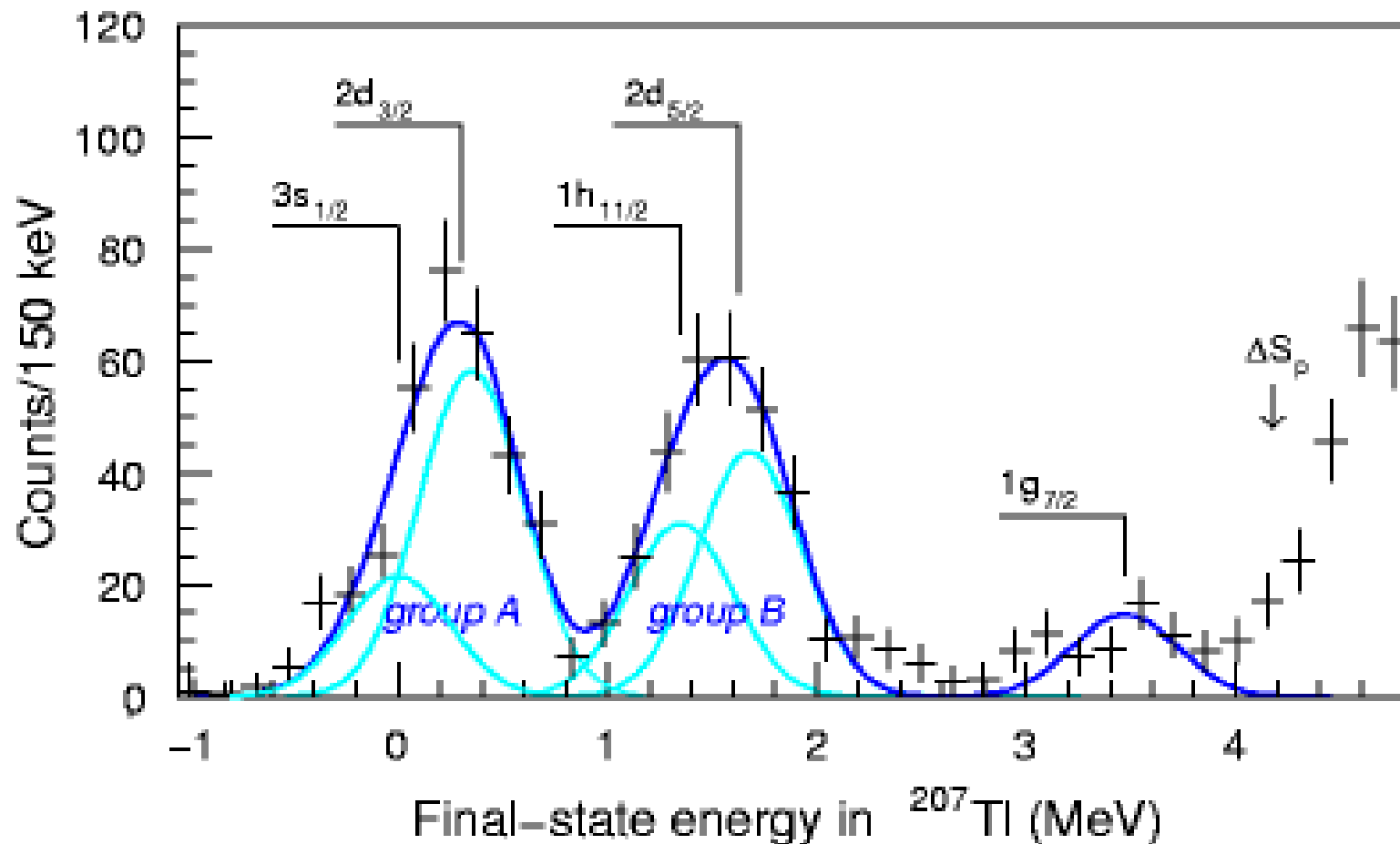
$^{208}\text{Pb}(\alpha, \alpha')$ followed by p decay

Decay to hole states in ^{207}Tl ; branching ratios predicted by Gorelik *et al.*



M. Hunyadi *et al.*, Phys. Lett. B576 (2003) 253
M. Hunyadi *et al.*, Phys. Rev. C75 (2007) 014606

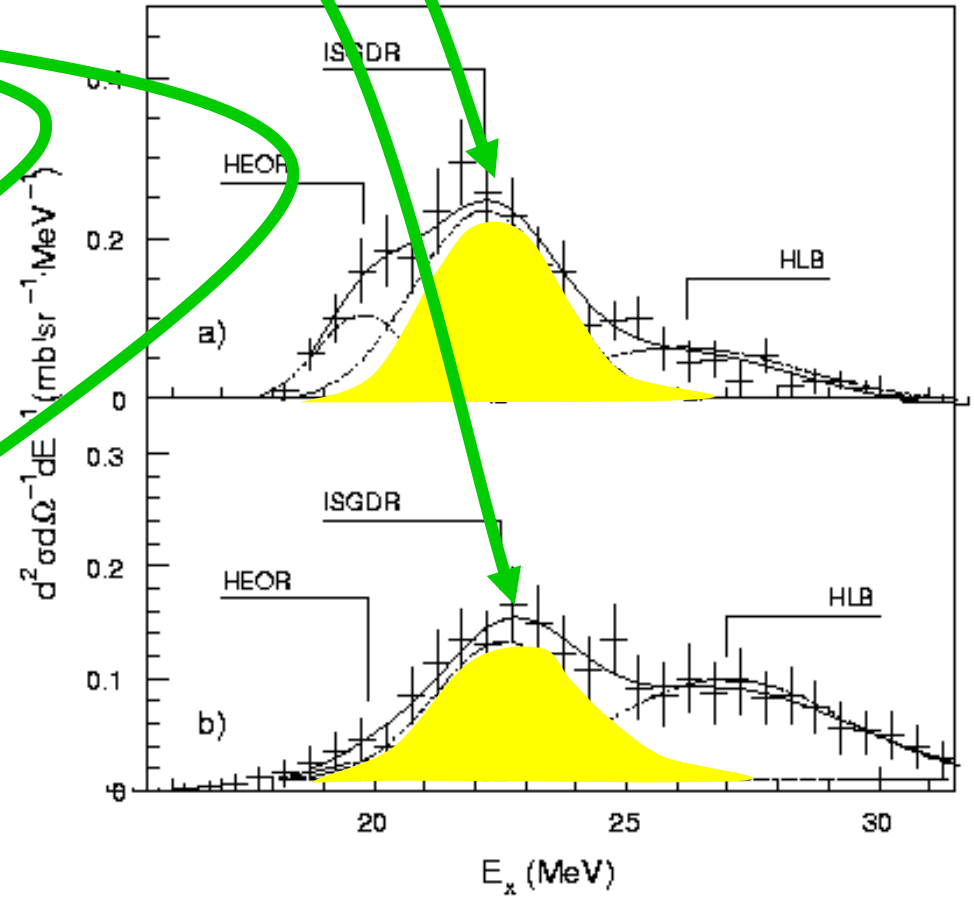
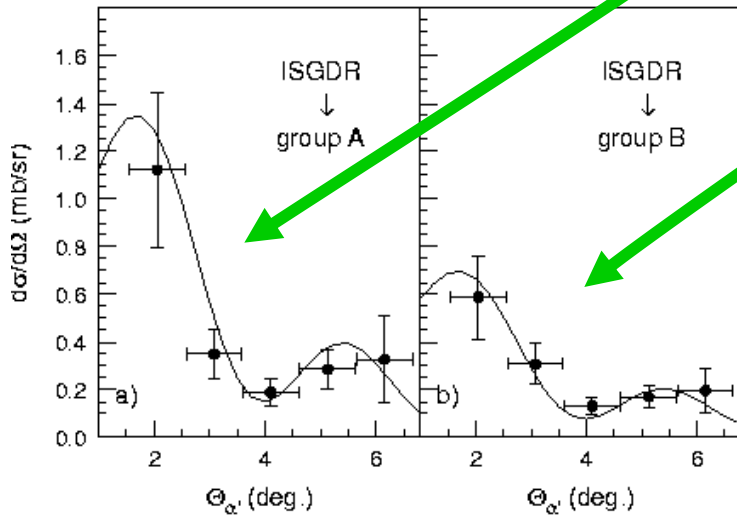
Branching ratios for decay



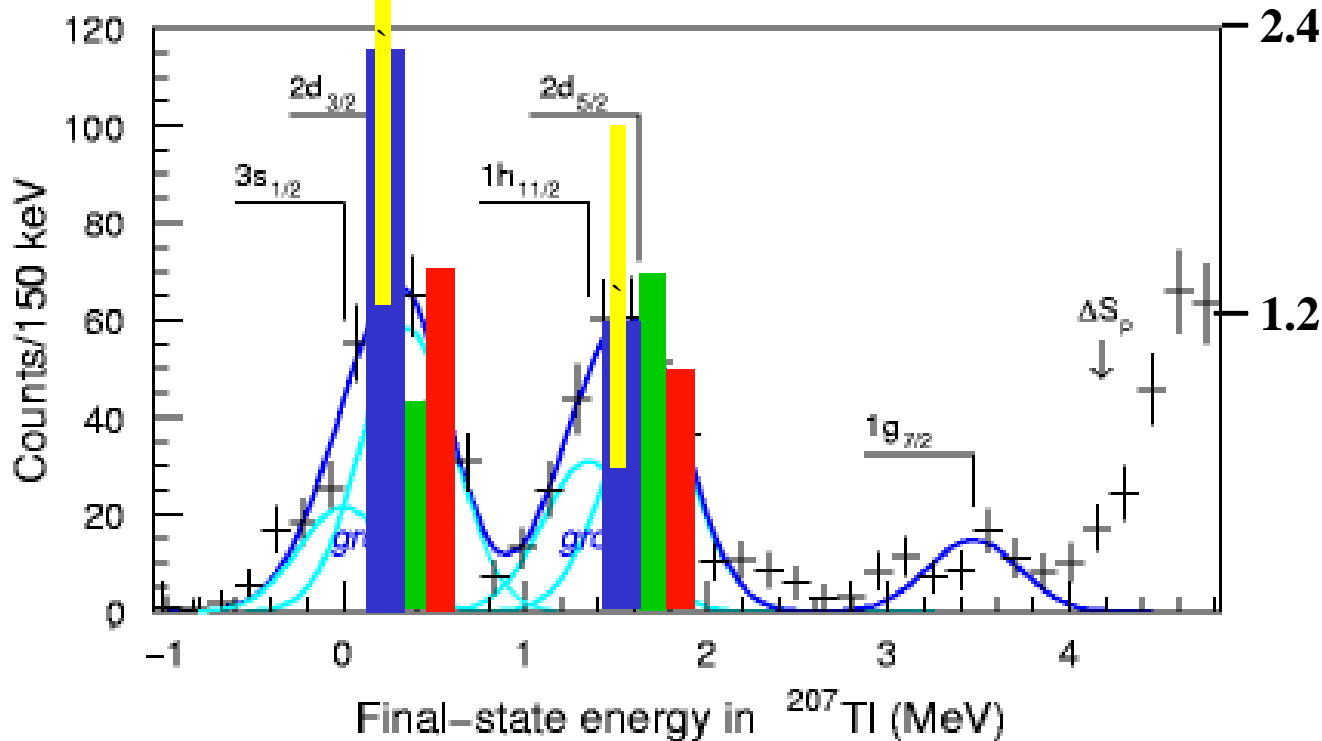
ISGDR in ^{208}Pb in **p** decay

gated on hole states

$E_x = 22.1 \pm 0.3 \text{ MeV}$
 $L = 1$ transition



Branching ratios for decay



This work

Gorelik *et al.*, PRC
62 (2000) 047301;

Continuum RPA;
Landau-Migdal
Parameters: f^{ex} , f' ;
Smearing parameter
 Δ energy-dependent

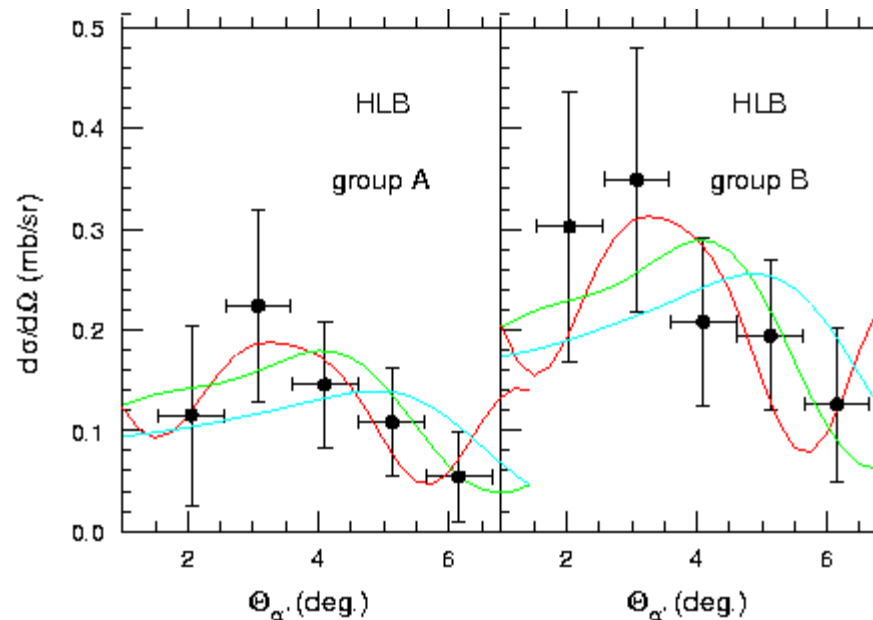
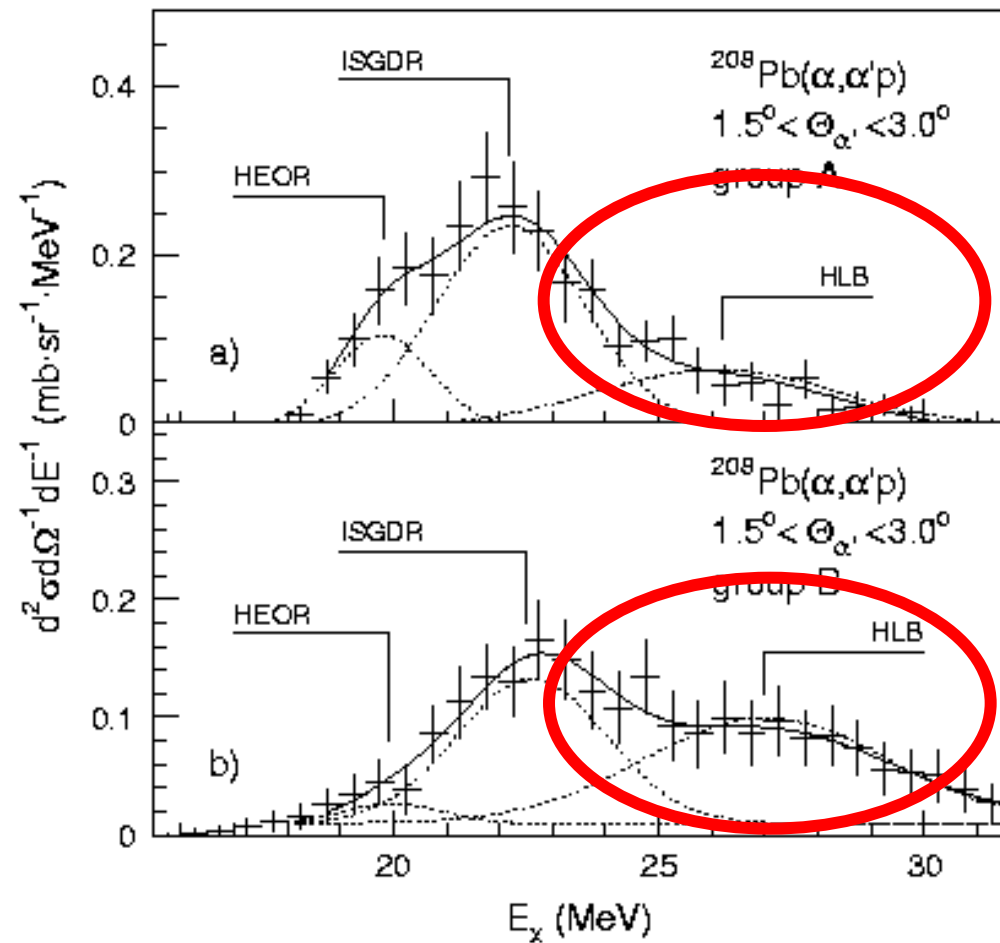
Gorelik *et al.*, PRC 69 (2004) 054322

$1/2^+ + 3/2^+$	2.6%	($S \sim 0.56$)	1.45%	2.3 ± 1.1
$11/2^- + 5/2^+$	1.9%	($S \sim 0.56$)	1.04%	1.2 ± 0.7

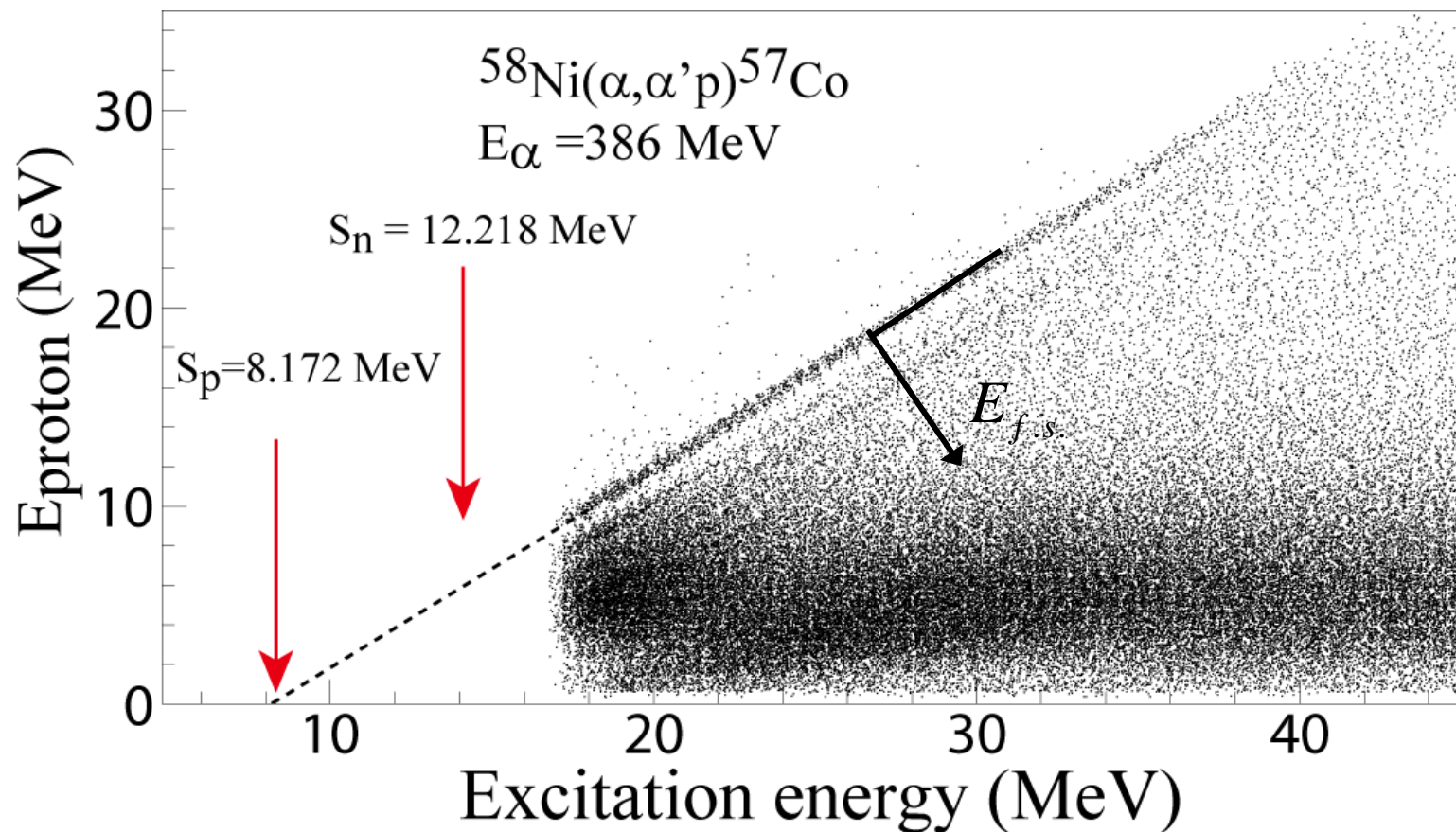
Overtone of the ISGQR? [r^4Y_2]

$$E_x = 26.9 \pm 0.7 \text{ MeV}$$

Muraviev and Urin
 Bull. Acad. Sci. USSR
 Phys. Ser. 52 (1988) 123
 $E_x = 28.3 \text{ MeV}$



Data analysis: Proton decay



Final-state energy

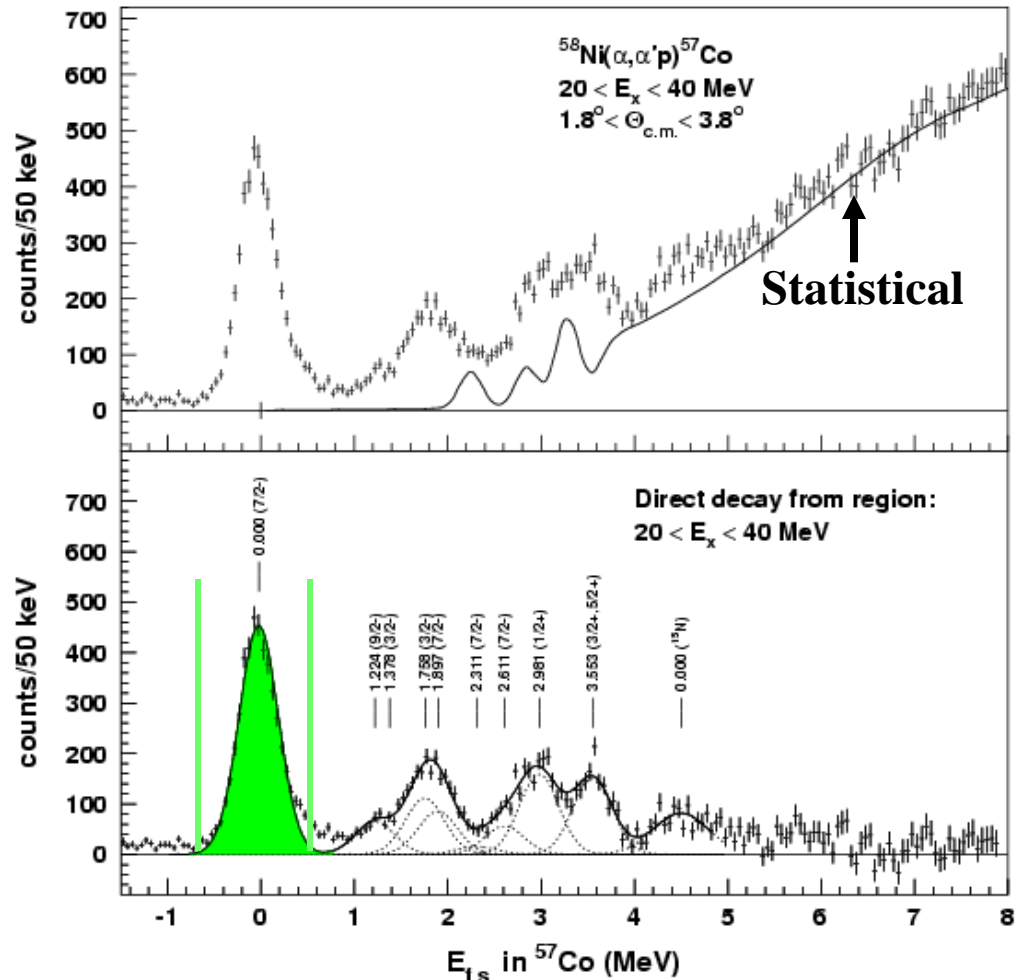
$$E_{f.s.} = E_X - E_p - S_p$$

Experimental results

M. Hunyadi *et al.*, Phys. Rev. C80 (2009) 044317

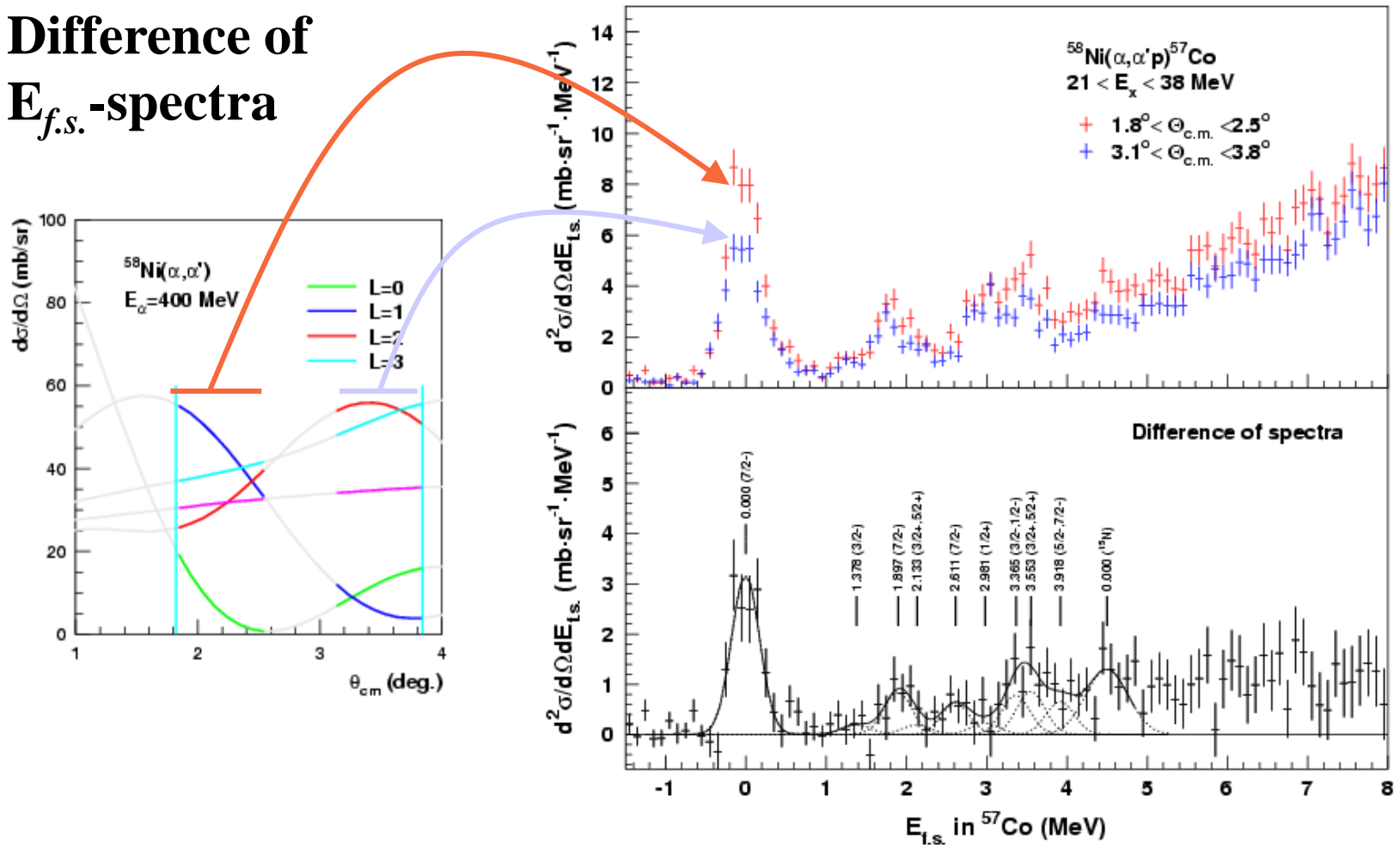
Final-state energy spectra

Final-state energy spectra after subtracting statistical contribution

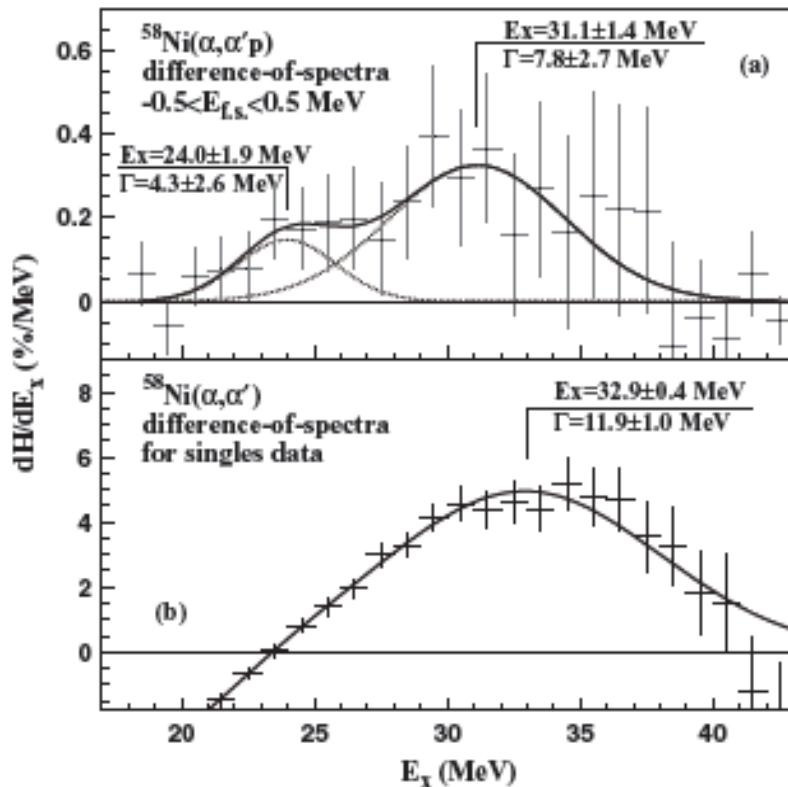


Experimental results

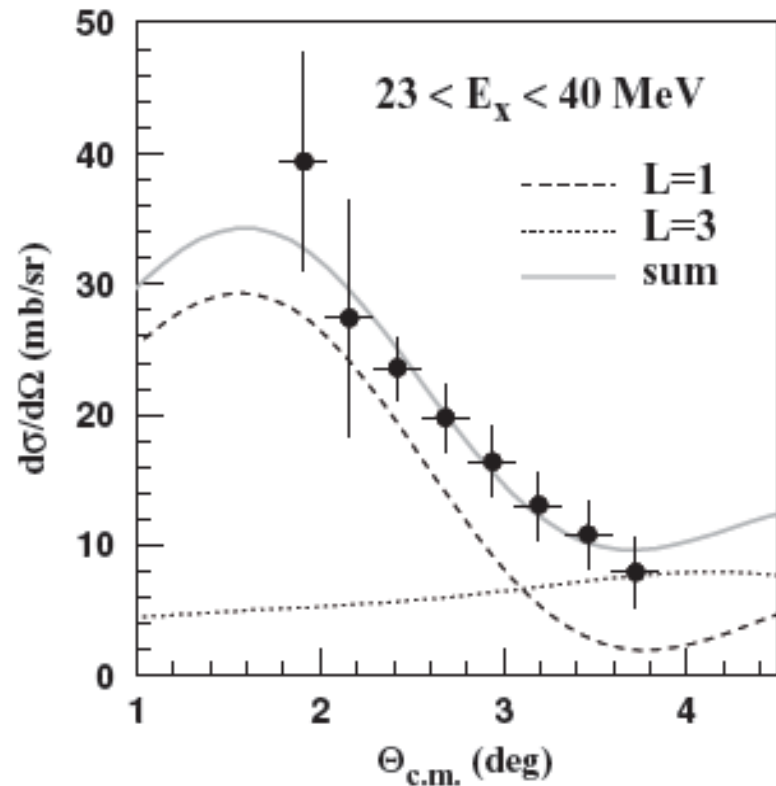
Difference of $E_{f.s.}$ -spectra



Strength distribution of ISGDR in ^{58}Ni



Spectra of $L = 1$ strengths obtained with DOS method in percentage of isoscalar EWSR; a) coincidence data gated on g.s. decay and b) singles data.



Differential cross section of resonance structure fitted with $L = 1$ and $L = 3$ DWBA calculations.

Proton-decay branching ratios Normalized to 100%

	Exp. (%) (24-38 MeV)	Cal. (%) (15-40 MeV)
$7/2^-$	61.3 (with $5/2^-$)	47
$3/2^-$	7.9	3.1
$3/2^-, 1/2^-$	9.9	2.2 (only for $1/2^-$)
$5/2^-$	3.2 ± 3.4	-
$1/2^+$	2.0 ± 4.2	13.4
$3/2^+, 5/2^+$	15.9	34.3
Σ	100 %	100%

**Calculations: M.L. Goerlik, I.V. Safonov, and M.H. Urin,
Phys. Rev. C69 (2004) 054322**

Conclusions!

- There has been much progress in understanding ISGMR & ISGDR macroscopic properties

Systematics: E_x , Γ , %EWSR

$\Rightarrow K_{nm} \approx 240 \text{ MeV}$

$\Rightarrow K_\tau \approx -500 \text{ MeV}$

- Sn nuclei are softer than ^{208}Pb and ^{90}Zr .
- Recently, Microscopic Structure for a few nuclei

CRPA has some success in ^{208}Pb & ^{58}Ni but fails badly in ^{116}Sn & ^{90}Zr .

- Possible observation quadrupole compression mode, i.e. overtone of ISGQR

Outlook

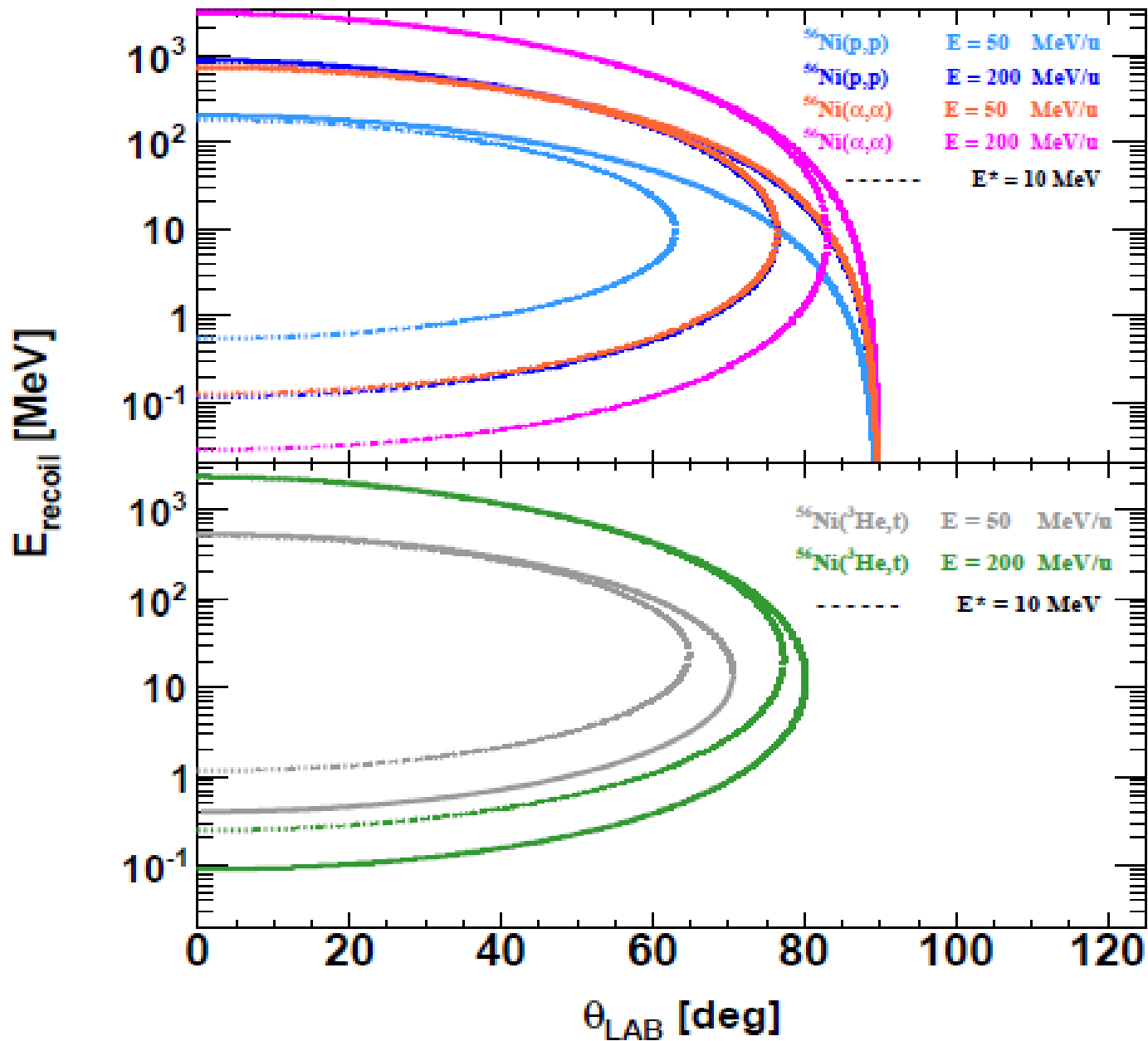
Radioactive ion beams will be available at energies where it will be possible to study excitation of ISGMR and ISGDR

RIKEN, FAIR, SPIRAL2, NSCL, EURISOL

Determine ISGMR and ISGDR in unstable Sn nuclei.

$A = 106$ to 134 possible

\Rightarrow A more precise determination of K_τ



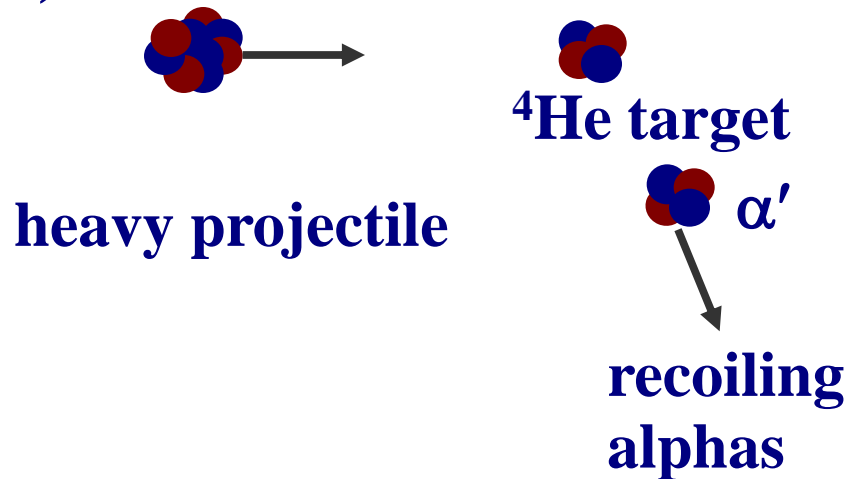
Nuclear structure studies with reactions in inverse kinematics

- Possible at FAIR and RIKEN

(beam energies of 50-100 MeV/u are needed!)

**Approach (at FAIR):
measure the recoiling alphas**

(α, α')



heavy ejectile

**Inconvenience:
difficulty to detect the low-energy alphas**

Detection system @ FAIR

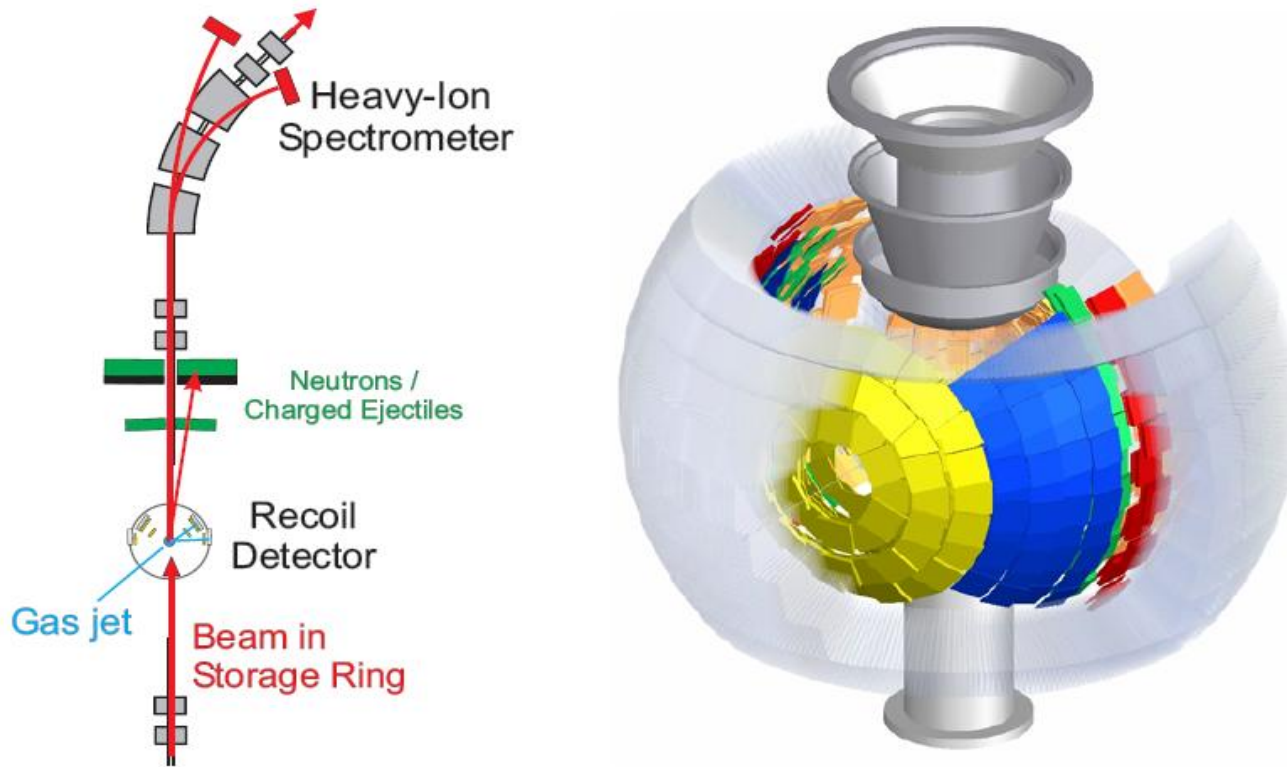
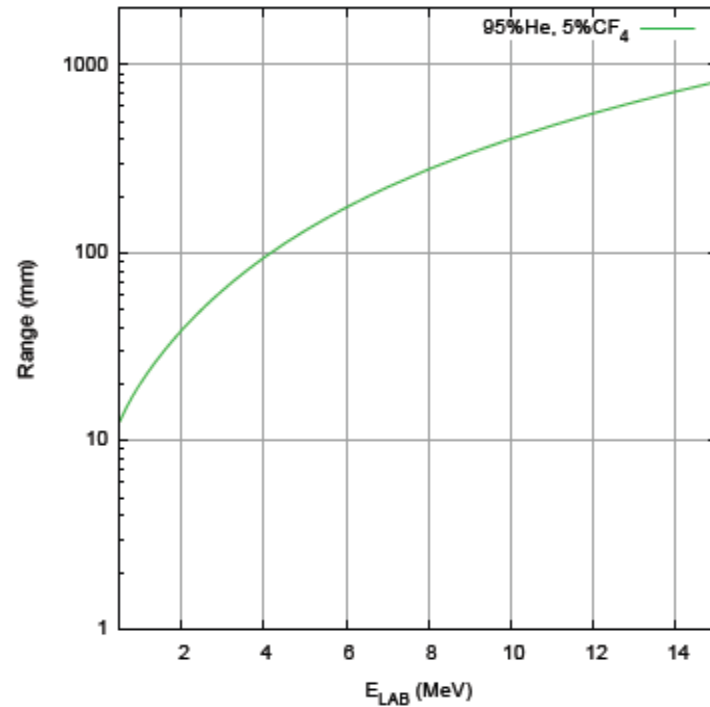
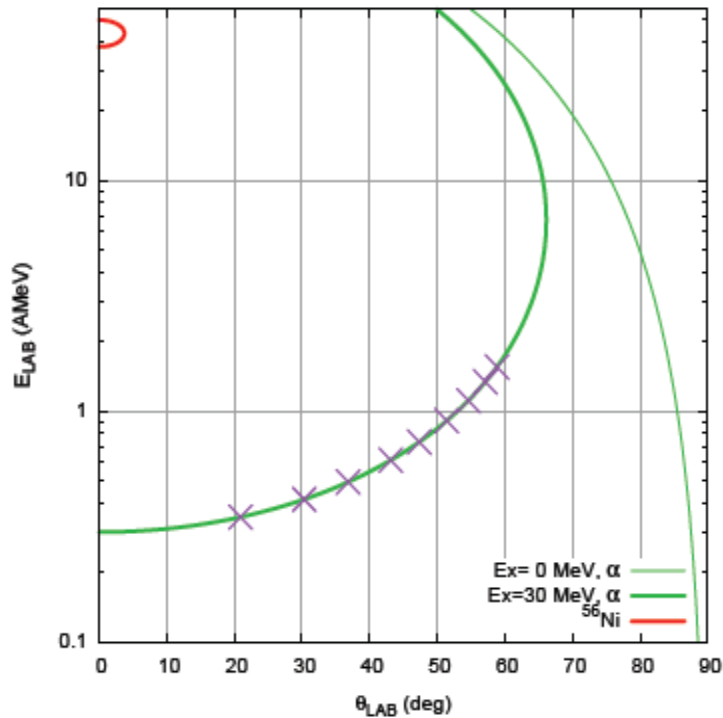


Figure 1: Schematic view of the EXL detection systems. Left: Set-up built into the NESR storage ring. Right: Target-recoil detector surrounding the gas-jet target.

Use of EXL recoil detector is under evaluation

Kinematics: energies



ISGDR in ^{56}Ni : 2nd ISGDR in Ni after ^{58}Ni

Conditions

- $^{56}\text{Ni}(\alpha, \alpha')$ and $^{56}\text{Ni}(\alpha, \alpha'p)$
- LISE beam at the highest energy possible ($\geq 50A$ MeV)

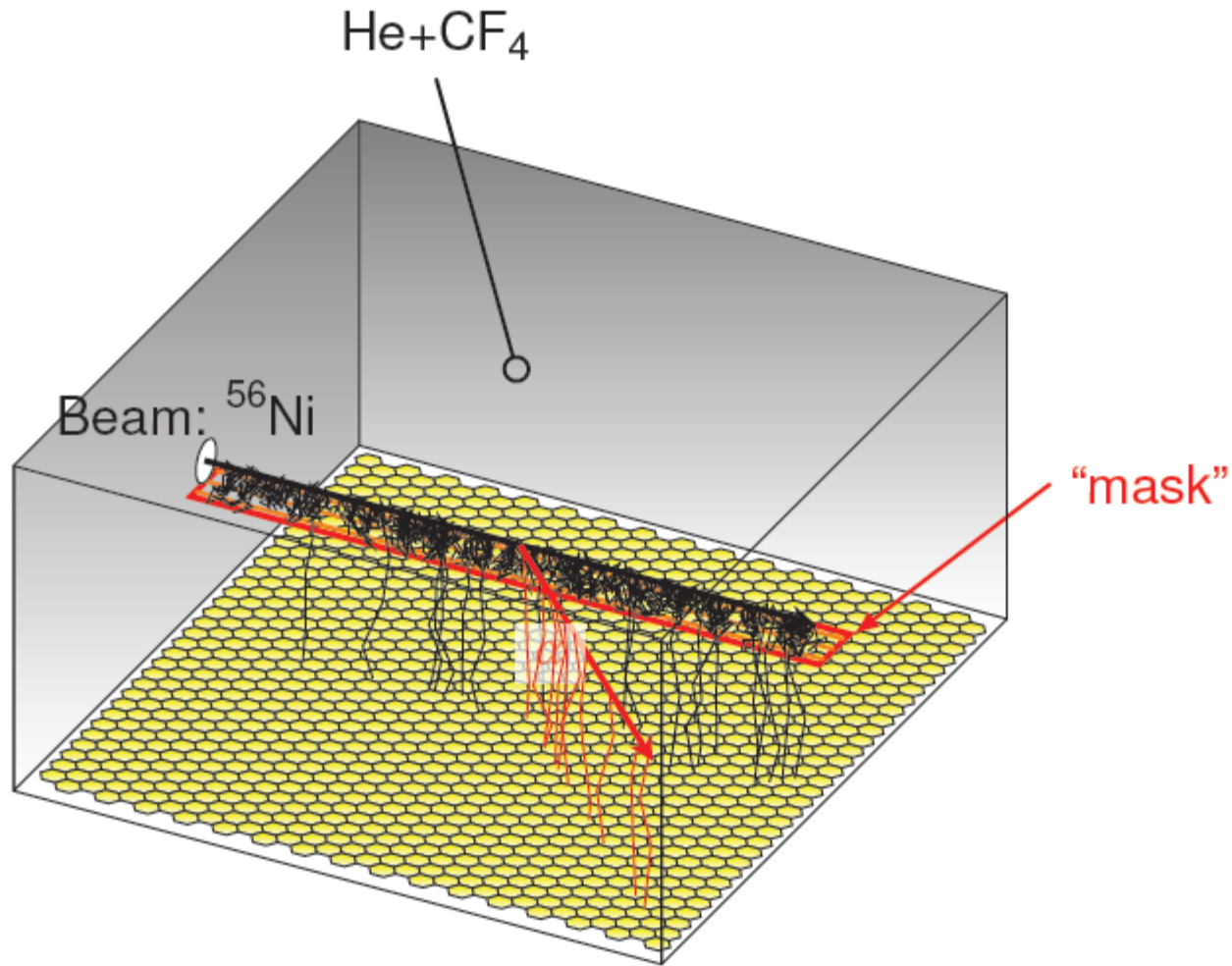
Setup

- MAYA in D6, filled w/ He (>95%), CF_4 mixture.
- All ancillary detectors (Si & CsI + S1)
- “Active” masking of the beam

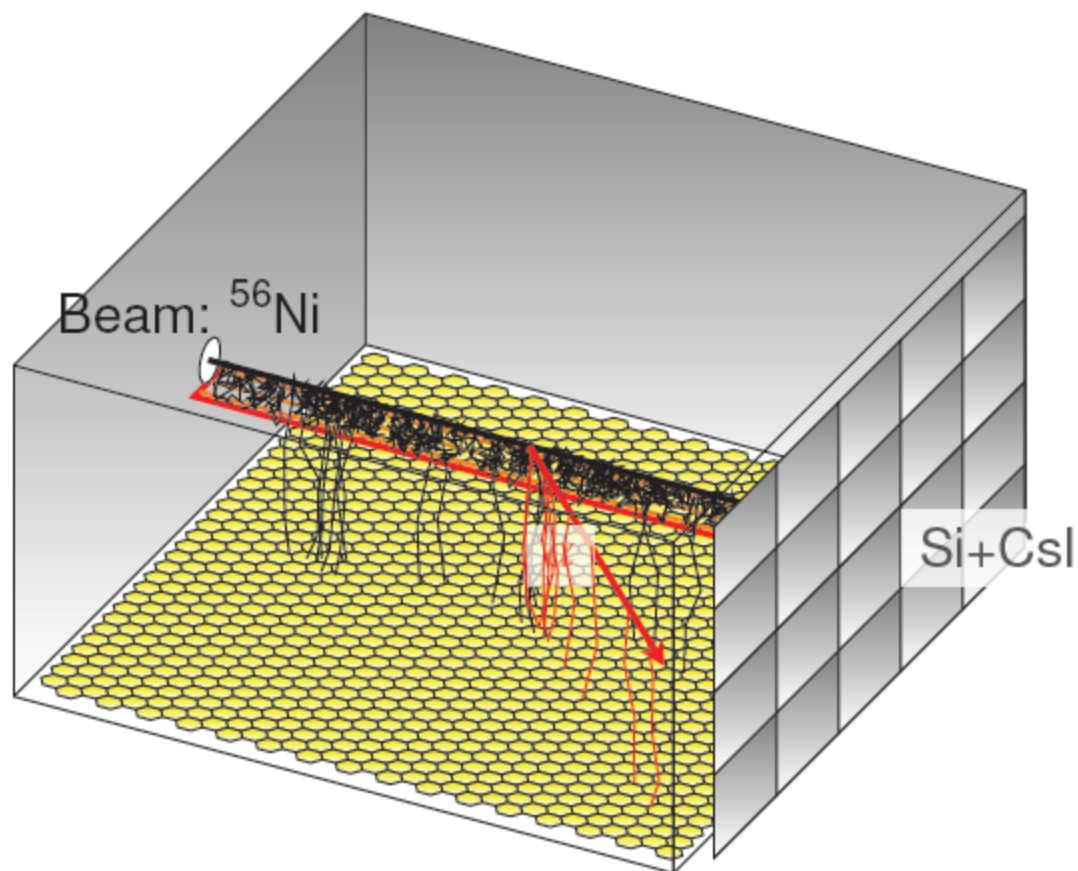
Predictions

- Detect alpha down to ≈ 1 MeV, between $[2^\circ, 10^\circ]$ in C.M.
- Remeasure ISGMR in ^{56}Ni
- Detect protons coming from ISGDR decay

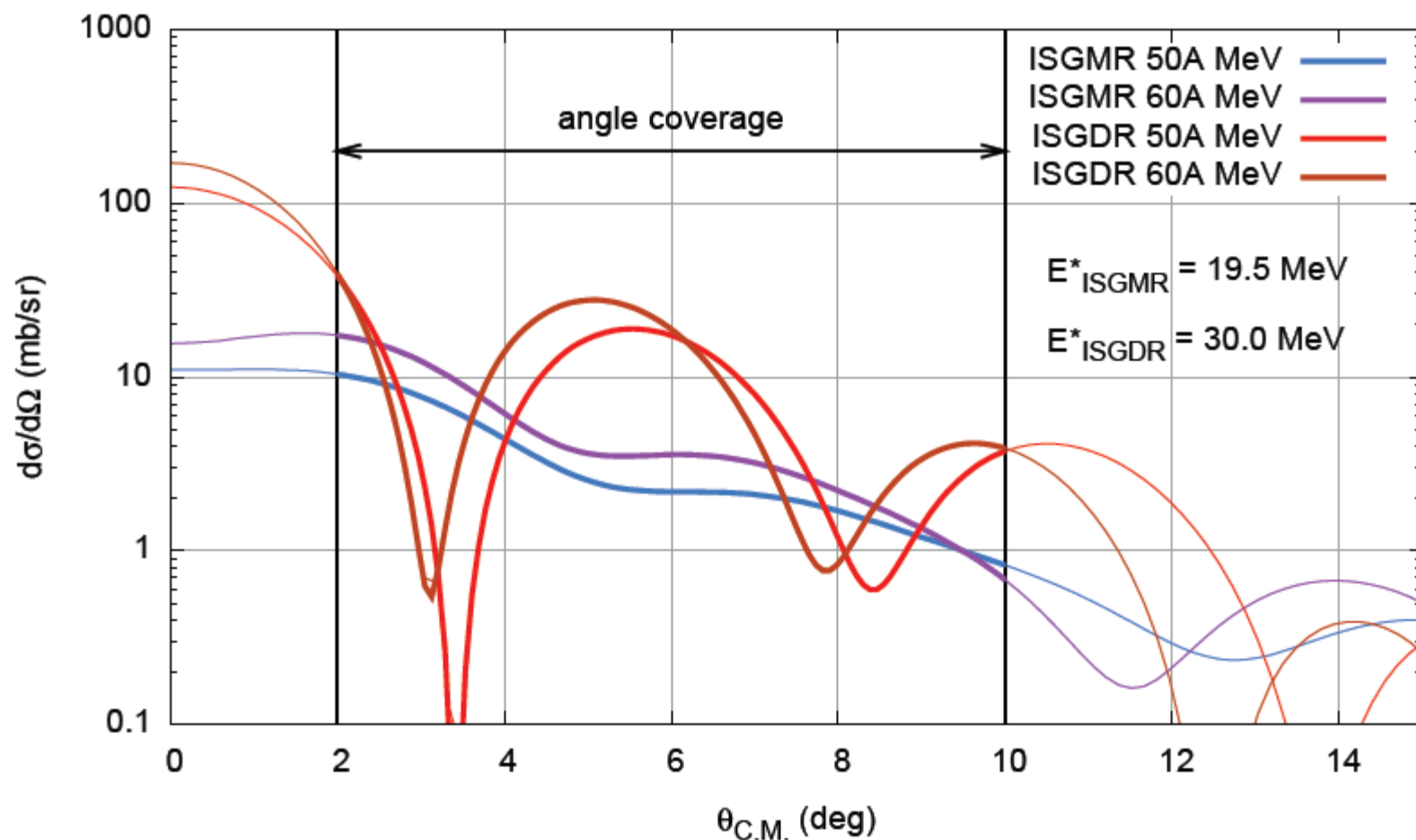
Setup: MAYA (Active target)



Setup: MAYA (Active target)



Predicted angular distribution

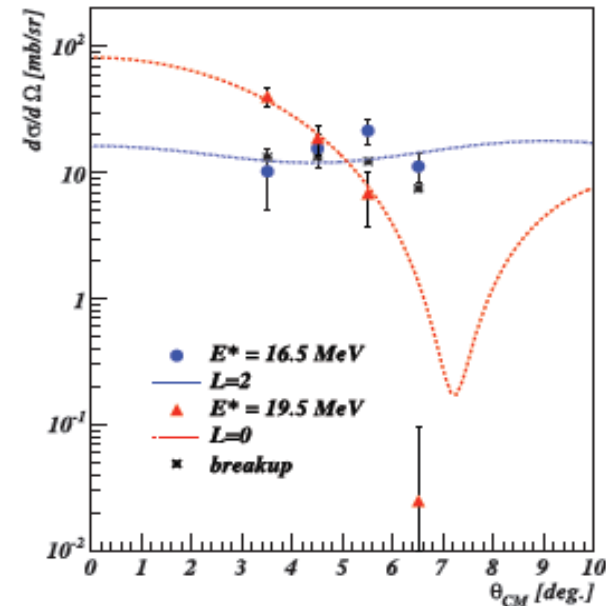
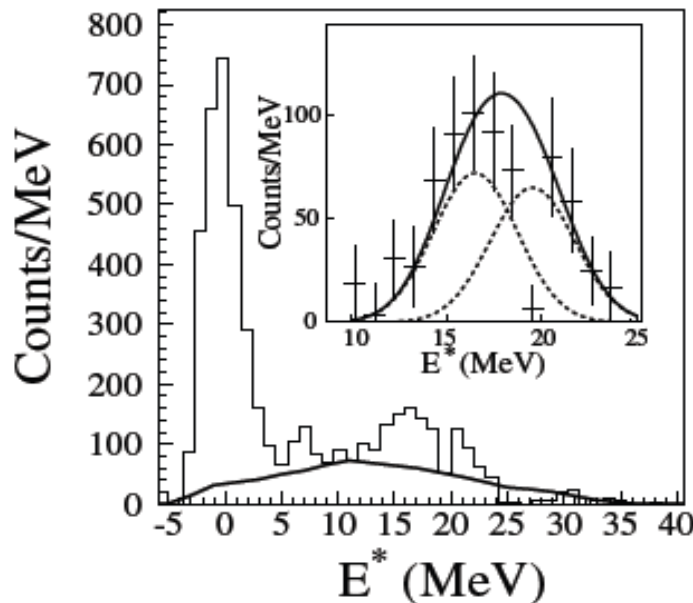


Recent works: ISGMR

ISGMR in unstable nuclei

^{56}Ni : active target MAYA filled with deuterium gas
bombarding energy of 50A MeV

C. Monrozeau *et al.* @ GANIL



*Excitation of the isovector GDR by inelastic α -scattering
as a measure of the neutron skin of nuclei*

A. Krasznahorkay *et al.*,

Nucl. Phys. A567 (1994) 521

**Measuring the cross section of the isovector giant
dipole resonance (IVGDR) for**

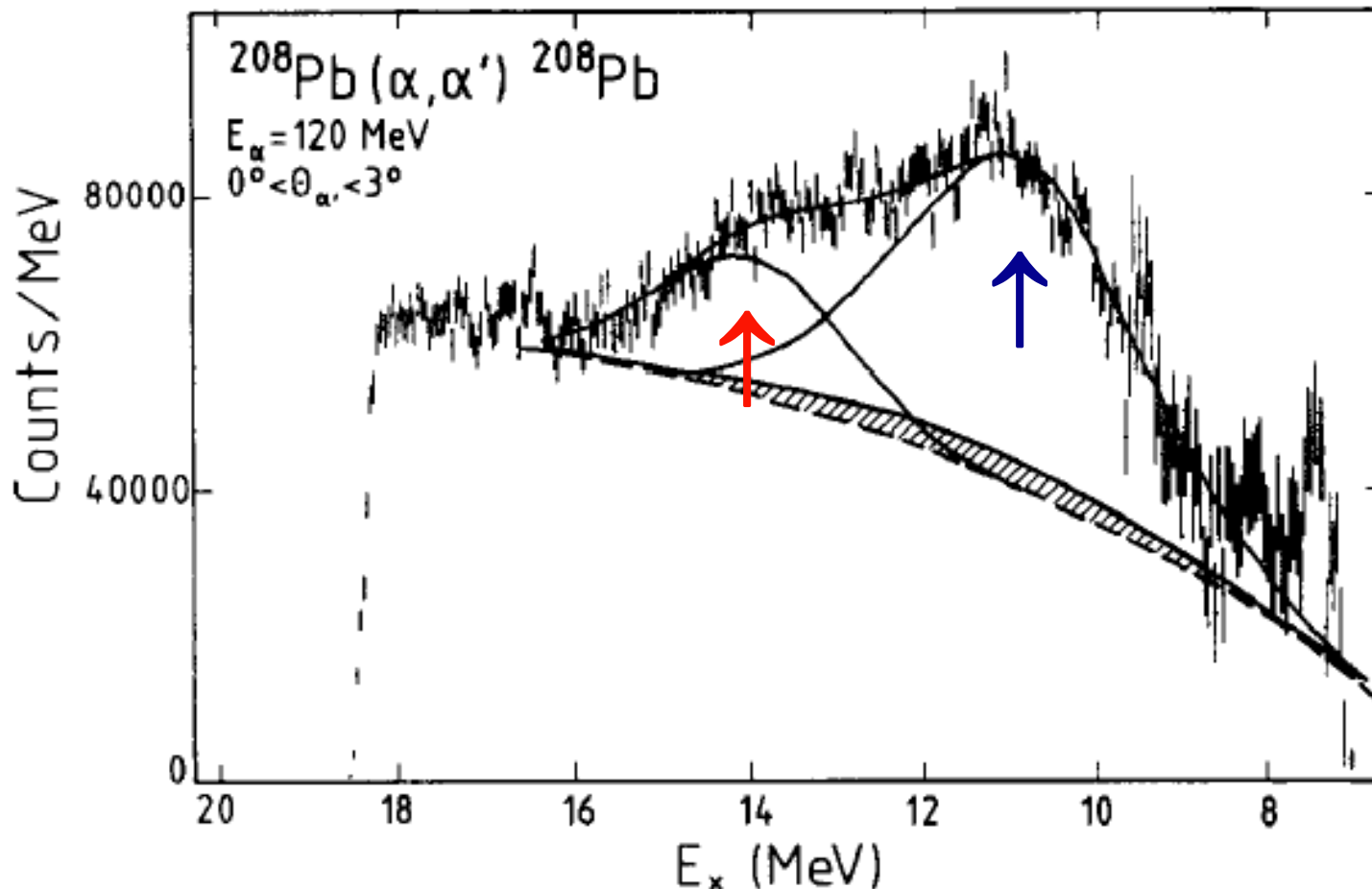
**$^{116,124}\text{Sn}(\alpha, \alpha'\gamma_0)$, $^{150}\text{Nd}(\alpha, \alpha'\gamma_0)$ and $^{208}\text{Pb}(\alpha, \alpha'\gamma_0)$
reactions at $E_\alpha = 120$ MeV and $0^\circ \leq \theta_{\alpha'} \leq 3^\circ$**

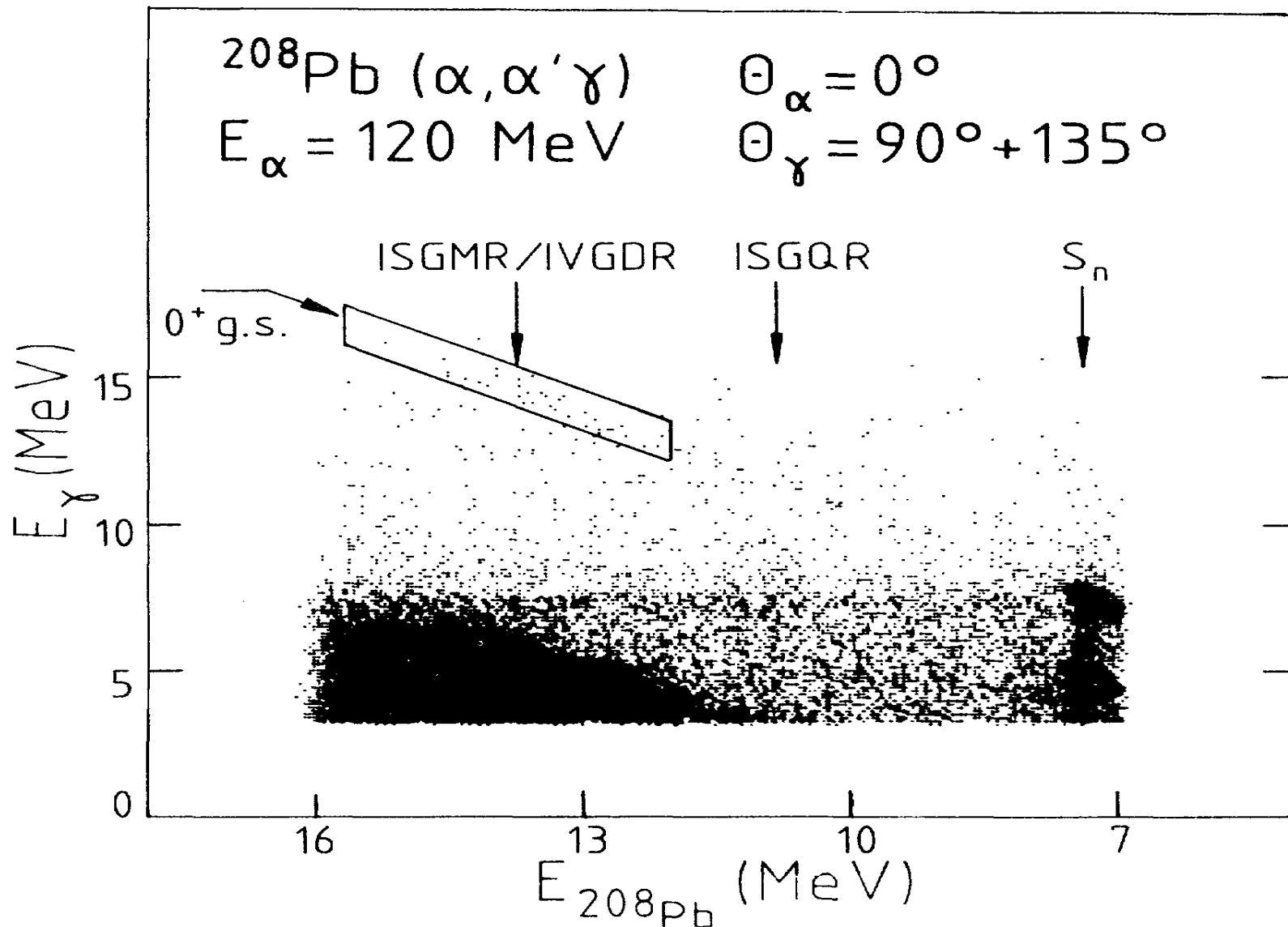
\Rightarrow Determine neutron-skin thickness

ISGQR at 10.9 MeV

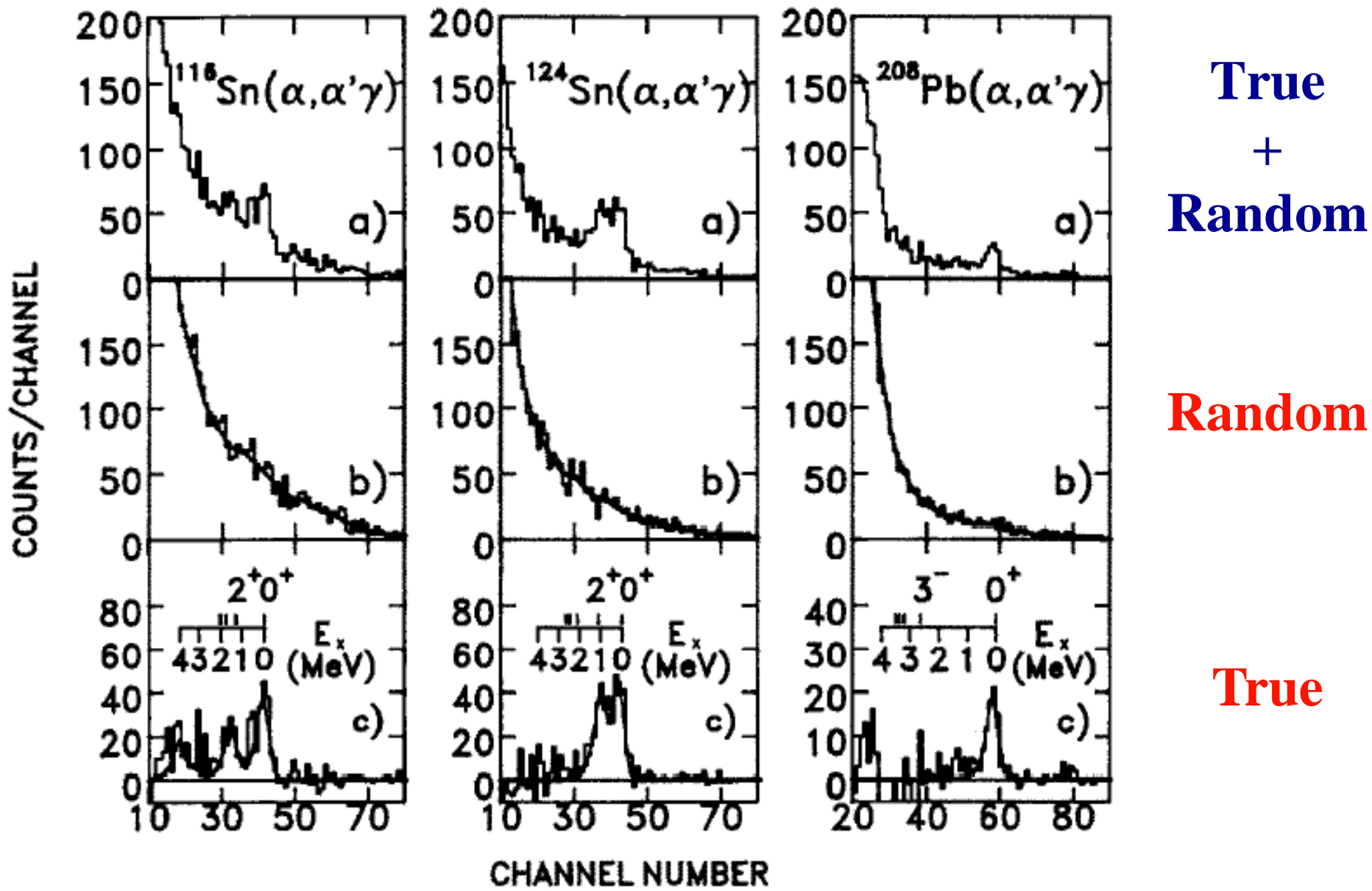
ISGMR at 13.9 MeV

Hatched area \Rightarrow IVGDR contribution (Coulomb + nuclear)





Two-dimensional spectrum showing inelastic α -scattering in coincidence with γ -decay



Isoscalar transition density in the Goldhaber-Teller model for excitation of IVGDR in inelastic α -scattering.

$$g_1^{10}(r) = g_1^n(r) - g_1^p(r) = \alpha_1 \gamma \left(\frac{N-Z}{A} \right) \left(\frac{d\rho(r)}{dr} + \frac{1}{3}c \frac{d^2\rho(r)}{dr^2} \right).$$

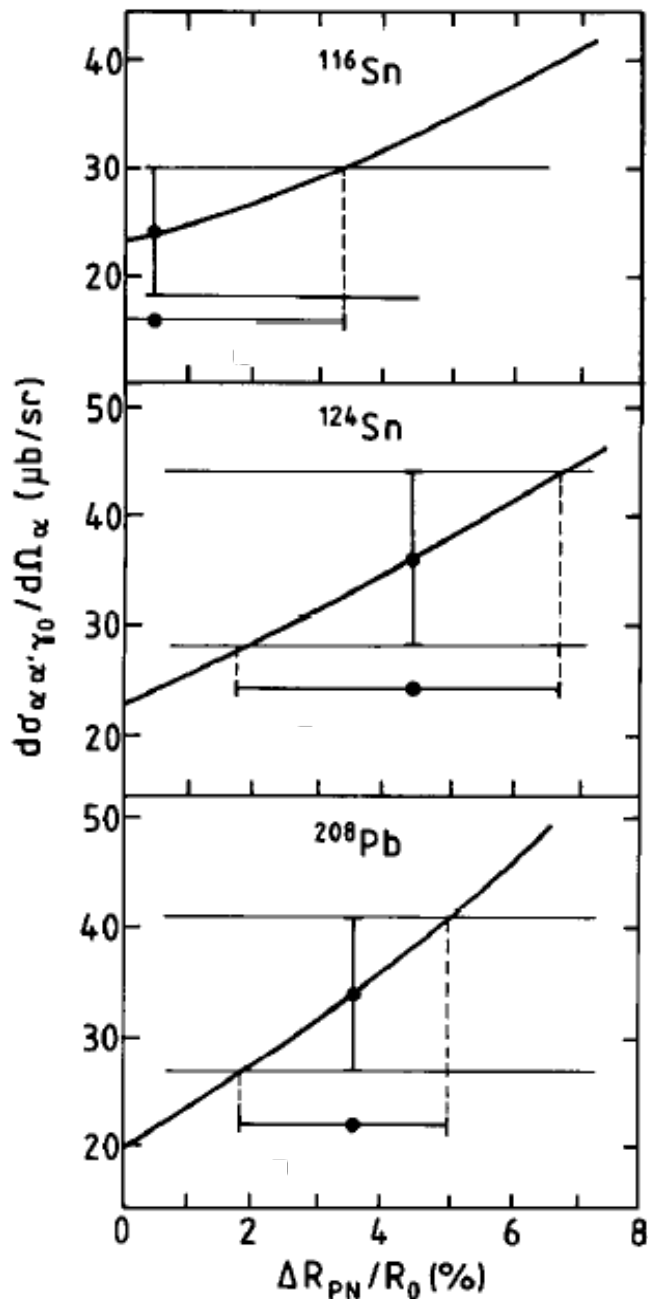
$$\frac{\Delta R_{pN}}{R_0} = \frac{R_n - R_p}{\frac{1}{2}(R_n + R_p)} = \gamma \frac{2(N-Z)}{3A}.$$

Therefore, DWBA cross sections can be calculated as function of $\Delta R_{pn}/R_0$ for the Goldhaber-Teller model and similarly for the Steinwedel-Jensen model.

γ -decay branching ratios are known from photoabsorption experiments.

Full line is the calculated $\alpha\gamma_0$ coincidence cross section, averaged over the solid angle of the α -particle and integrated over the full γ -ray solid angle (4π) and over the ΔE energy range as function of $\Delta R_{pn}/R$.

The experimental $\alpha\gamma_0$ cross sections for the IVGDR are shown as full circles with vertical error bars. The deduced values for $\Delta R_{pn}/R$ with the associated uncertainty (full circles with horizontal error bars) are also indicated.



Isotope	Present work $\Delta R_{PN}/R_0$ (%)	Present work ΔR_{PN} (fm)	Batty et al. [2] ΔR_{PN} (fm)	Angeli et al. [6] ΔR_{PN} (fm)
^{116}Sn	0.5 ± 2.7	0.02 ± 0.12	0.15 ± 0.05	0.13
^{124}Sn	4.4 ± 2.4	0.21 ± 0.11	0.25 ± 0.05	0.22
^{208}Pb	$3.5^{+1.5}_{-1.6}$	0.19 ± 0.09	0.14 ± 0.04	0.22

Participants

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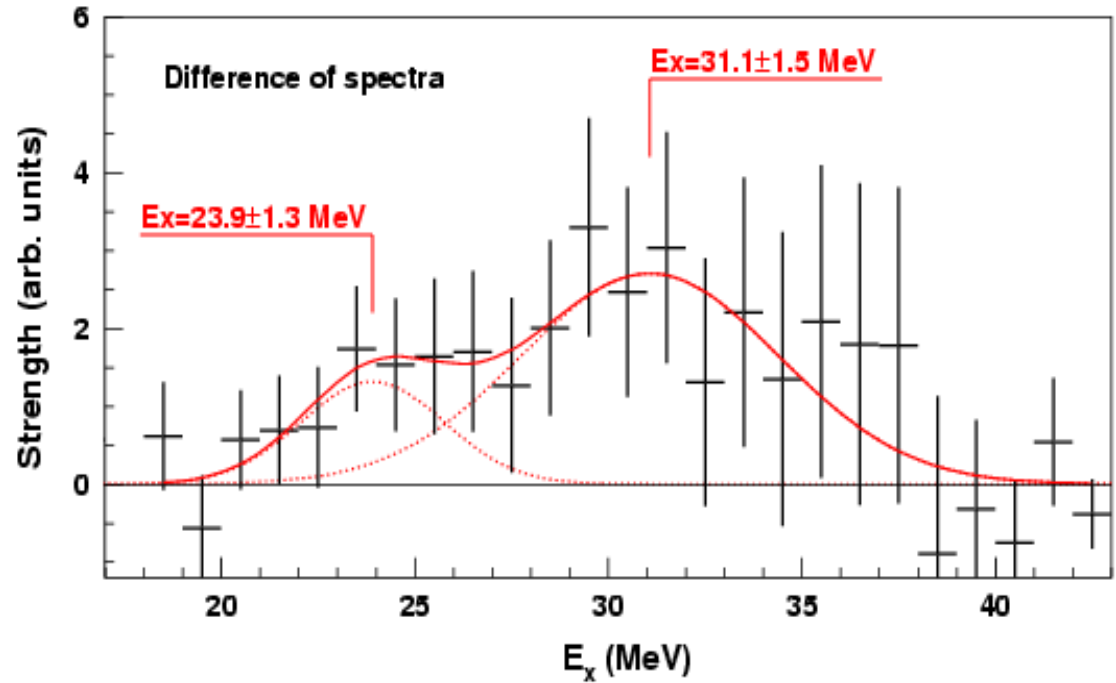
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E605: ISGDR in ^{58}Ni

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Konstanze Boretzky	Haïfa Bouzomita	Lucia Caceres
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Geoff Grinyer	Muhsin N. Harakeh	Nasser Kalantar
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Thomas Roger	Sara Sambhi	Hervé Savajols
Christelle Stodel	Laura Suen	Jean Charles Thomas
Marine Vandebrouck	Jarno van de Walle	

Strength distribution of ISGDR in ^{58}Ni

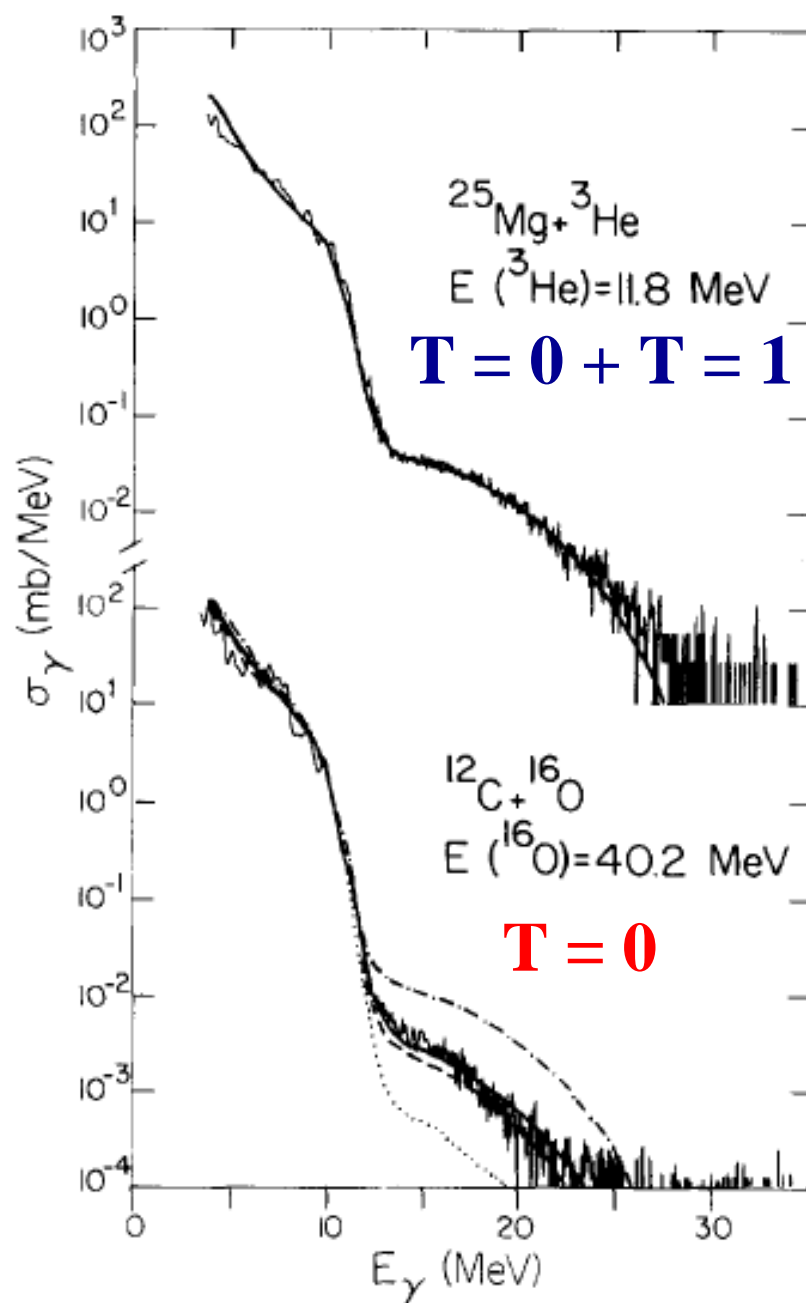
Double differential cross section of DOS divided by double differential cross section calculated by DWBA in 1.8 ~2.5 degree (dipole favoring angle region)



Centroid energies:

$\langle E \rangle = 31.1 \pm 1.5 \text{ MeV}$ higher-lying peak

$\langle E \rangle = 29.7 \pm 0.8 \text{ MeV}$ for $20 < E_x < 40 \text{ MeV}$



Role of isospin in the statistical decay of the giant dipole resonance built on excited states
M.N. Harakeh, D.H. Dowell, G. Feldman, E.F. Garman, R. Loveman, J.L. Osborne and K.A. Snover
Phys. Lett. B176 (1986) 297

Dotted: pure ISGQR
Dashed: pure isospin
Dash-dotted: complete isospin mixing
Solid: isospin mixing (~ 5%)

